

حمل الآن

مجاناً وحصرياً

# امتحانات رقم (1)

## الترم الاول



1

Cairo Governorate

Shoubra Educational Zone  
Mathematics Supervision

First

Multiple choice questions

Interactive  
test ①

Choose the correct answer from the given ones :

(1) If  $7^X = 4$ , then  $X = \dots\dots\dots$ 

(a)  $\frac{4}{7}$

(b)  $\frac{7}{4}$

(c)  $\log_7 4$

(d)  $\log_4 7$

(2) The point of symmetry of the curve of the function  $f : f(X) = X^3$  is  $\dots\dots\dots$ 

(a) (1, 1)

(b) (0, 0)

(c) (1, 0)

(d) (0, 1)

(3) If  $2^{X-5} = 3^{5-X}$ , then  $X = \dots\dots\dots$ 

(a)  $\frac{2}{3}$

(b)  $\frac{3}{2}$

(c) 0

(d) 5

(4) The curve of the function  $g : g(X) = |X + 3|$  is the same curve of the function  $f : f(X) = |X|$  by a translation 3 units in the direction of  $\dots\dots\dots$ 

(a)  $\overrightarrow{OX}$

(b)  $\overrightarrow{OX}$

(c)  $\overrightarrow{OY}$

(d)  $\overrightarrow{OY}$

(5) If  $f(X) = 5^X$ , then  $\frac{f(X+2)}{f(X+1)} = \dots\dots\dots$ 

(a) 25

(b) 5

(c) 1

(d)  $\frac{1}{5}$

(6)  $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x^2 + 1} = \dots\dots\dots$ 

(a) 0

(b) 1

(c) 2

(d) doesn't exist.

(7)  $\lim_{x \rightarrow 3} \frac{x^2 - 8x + 15}{x - 3} = \dots\dots\dots$ 

(a) 7

(b) 3

(c) 2

(d) -2

(8) The measure of the greatest angle of  $\Delta ABC$  where :  $a = 3$  cm. ,  $b = 4$  cm. ,  $c = 5$  cm. equals  $\dots\dots\dots$ 

(a)  $90^\circ$

(b)  $60^\circ$

(c)  $30^\circ$

(d)  $120^\circ$

(9) In  $\Delta ABC$  : if  $a = 7$  cm. , then  $b = \dots\dots\dots$ 

(a)  $\frac{\sin A}{7 \sin B}$

(b)  $\frac{\sin C}{7 \sin B}$

(c)  $\frac{7 \sin B}{\sin A}$

(d)  $\frac{7 \sin A}{\sin B}$

(10) If  $f$  is an even function on the interval  $]a, b[$ , then  $b = \dots\dots\dots$ 

(a)  $a$

(b)  $-a$

(c)  $2a$

(d)  $a^2$

- (11) The domain of the function  $f(x) = \frac{x-3}{x^2-5x+6}$  is .....
- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{3\}$  (c)  $\mathbb{R} - \{-2, -3\}$  (d)  $\mathbb{R} - \{2, 3\}$
- (12) If  $f(x) = 2^x$ , then  $f(-1) = \dots\dots\dots$
- (a) 1 (b) -1 (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
- (13) If  $\left(\frac{1}{2}\right)^x = 8$ , then  $x = \dots\dots\dots$
- (a) -3 (b) 3 (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
- (14)  $\lim_{x \rightarrow 1} \frac{x^5 - 1}{x - 1} = \dots\dots\dots$
- (a) 20 (b) 5 (c) 4 (d) 1
- (15)  $\lim_{x \rightarrow 4} \frac{x-4}{\sqrt{5+x}-3} = \dots\dots\dots$
- (a) 4 (b) 2 (c) 6 (d) 3
- (16) If  $\lim_{x \rightarrow 3} \frac{a}{x+1} = 2$ , then  $a = \dots\dots\dots$
- (a) 2 (b) 4 (c) 6 (d) 8
- (17) The radius length of the circumcircle of  $\Delta ABC$  in which :  $m(\angle A) = 30^\circ$ ,  $a = 10$  cm. equals ..... cm.
- (a) 5 (b) 10 (c) 20 (d) 40
- (18) In  $\Delta ABC$  if  $a^2 = b^2 + c^2 + bc$ , then  $m(\angle A) = \dots\dots\dots$
- (a)  $60^\circ$  (b)  $90^\circ$  (c)  $120^\circ$  (d)  $150^\circ$
- (19)  $\log 25 + \frac{\log 8 \times \log 16}{\log 64} = \dots\dots\dots$
- (a) 2 (b) 4 (c) 10 (d) 100
- (20) The solution set of the equation :  $|2x - 1| = 5$  in  $\mathbb{R}$  is .....
- (a)  $\mathbb{R}$  (b)  $[-2, 3]$  (c)  $\{3\}$  (d)  $\{-2, 3\}$
- (21) If  $\log 3 = x$ ,  $\log 4 = y$ , then  $\log 12 = \dots\dots\dots$
- (a)  $\log x + \log y$  (b)  $x - y$  (c)  $x + y$  (d)  $xy$
- (22) If  $\log_2 x = \frac{1}{3}$ , then  $\log_2 (8x^3) = \dots\dots\dots$
- (a) 1 (b) 4 (c) 2 (d) 3
- (23)  $\lim_{x \rightarrow \infty} \left(3 - \frac{7}{x} + \frac{4}{x^2}\right) = \dots\dots\dots$
- (a)  $\infty$  (b) 0 (c) -7 (d) 3
- (24)  $\lim_{x \rightarrow 7} \frac{x^3 - 343}{x^2 - 49} = \dots\dots\dots$
- (a)  $\frac{21}{2}$  (b)  $\frac{2}{21}$  (c)  $\frac{3}{2}$  (d) 14



- (25)  $\lim_{x \rightarrow \infty} \frac{2x^2 + 5x - 3}{7 - 3x^2} = \dots\dots\dots$   
 (a)  $-\frac{3}{7}$  (b)  $-\frac{2}{3}$  (c) 0 (d)  $\infty$
- (26) In  $\Delta ABC$  : if  $a = 3$  cm. ,  $b = 4$  cm. ,  $c = 6$  cm. , then  $\cos C = \dots\dots\dots$   
 (a)  $-\frac{11}{24}$  (b)  $\frac{11}{24}$  (c)  $-\frac{11}{12}$  (d)  $\frac{11}{12}$
- (27) If  $r$  is the radius length of the circumcircle of  $\Delta ABC$  , then  $\frac{2b}{\sin B} = \dots\dots\dots$   
 (a)  $\frac{1}{2}r$  (b)  $r$  (c)  $2r$  (d)  $4r$

## Second Essay questions

Answer the following questions :

- 1 Graph the function  $f(x) = x^2 - 3$  , then from the graph deduce the range of the function , its monotony and its type whether it is even , odd or otherwise.
- 2 Find :  $\lim_{x \rightarrow \infty} \frac{16x^{-4} - 7x^{-1} - 27}{8x^{-4} - 9}$

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Zeitoun Educational Zone

## First Multiple choice questions



Interactive test 2

Choose the correct answer from the given ones :

- (1) The domain of the function  $f(x) = \frac{7}{x^3 - x}$  is .....  
 (a)  $\mathbb{R} - \{3\}$  (b)  $\mathbb{R} - \{7\}$  (c)  $\mathbb{R} - \{0, 1\}$  (d)  $\mathbb{R} - \{0, -1, 1\}$
- (2) All the following are unspecified quantities except .....  
 (a) zero  $\div$  zero (b)  $\infty - \infty$  (c)  $\infty + \infty$  (d)  $\infty \div \infty$
- (3) The exponential function of base "a" is increasing function if .....  
 (a)  $a > 0$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = 1$
- (4)  $\lim_{x \rightarrow 3} \frac{2x - 6}{7x - 21} = \dots\dots\dots$   
 (a)  $\frac{2}{3}$  (b)  $\frac{2}{7}$  (c)  $\frac{3}{7}$  (d) 3
- (5) XYZ is an equilateral triangle the length of its side is  $10\sqrt{3}$  cm. , then the length of the diameter of its circumcircle is ..... cm.  
 (a) 5 (b) 10 (c) 15 (d) 20
- (6) If  $2^{x+1} = 5^{x+1}$  , then  $3^{x+1} = \dots\dots\dots$   
 (a) 0 (b) 1 (c) -1 (d) 3



- (7)  $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2}}{x} = \dots\dots\dots$   
 (a) zero (b) 1 (c) 2 (d) -1
- (8) If  $\log_3 X = 2$ , then  $X = \dots\dots\dots$   
 (a) 3 (b) 5 (c) 8 (d) 9
- (9)  $\lim_{x \rightarrow 4} (3x - \sqrt{x}) = \dots\dots\dots$   
 (a) 8 (b) 10 (c) 14 (d) 16
- (10) The domain of the function  $f : f(x) = \sqrt{x-3}$  is  $\dots\dots\dots$   
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{3\}$  (c)  $[3, \infty[$  (d)  $]-\infty, 3[$
- (11) If "r" is the length of the radius of the circumcircle of the triangle XYZ, then  $\frac{y}{2 \sin Y} = \dots\dots\dots$   
 (a) r (b) 2r (c)  $\frac{1}{2}r$  (d) 4r
- (12) If  $\log_3 (2X + 3) = 2$ , then  $X = \dots\dots\dots$   
 (a) 3 (b) 2 (c) 9 (d) 4
- (13)  $\lim_{x \rightarrow 0} \frac{7+2x}{\cos x} = \dots\dots\dots$   
 (a) 7 (b) 8 (c) 9 (d) 1
- (14) The function  $f : f(x) = x \cos x \dots\dots\dots$   
 (a) even. (b) odd.  
 (c) neither even nor odd. (d) linear.
- (15)  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^3 - 8} = \dots\dots\dots$   
 (a) 4 (b)  $\frac{5}{3}$  (c) zero (d)  $6\frac{2}{3}$
- (16) If  $\angle A$  supplement of  $\angle C$ , then  $\cos A + \cos C = \dots\dots\dots$   
 (a) zero (b) 1 (c) -1 (d)  $\frac{1}{2}$
- (17) If  $2^x = 4^y = 64$ , then  $x + y = \dots\dots\dots$   
 (a) 3 (b) 4 (c) 6 (d) 9
- (18)  $\lim_{x \rightarrow 0} \frac{\sqrt[3]{x+1} - 1}{x} = \dots\dots\dots$   
 (a) 1 (b)  $\frac{1}{3}$  (c) zero (d)  $-\frac{2}{3}$
- (19) The solution set of  $\sqrt{4x^2 - 12x + 9} \leq 9$  is  $\dots\dots\dots$   
 (a)  $[-6, 12]$  (b)  $[-3, 6]$  (c)  $\mathbb{R} - [-3, 6]$  (d)  $\mathbb{R} - ]-3, 6[$
- (20) In  $\Delta XYZ : y^2 + z^2 - x^2 = 2yz \times \dots\dots\dots$   
 (a)  $\cos X$  (b)  $\sin Z$  (c)  $\cos Z$  (d)  $\sin X$

- (21)  $\log_2 5 \times \log_5 2 = \dots\dots\dots$   
 (a) 1 (b) 10 (c)  $\log_2 10$  (d)  $\log_5 10$
- (22)  $\lim_{x \rightarrow \infty} \left( \frac{3}{x^2} - 2 \right) = \dots\dots\dots$   
 (a) 3 (b) 2 (c) -3 (d) -2
- (23) The symmetric point of the curve of the function  $f : f(x) = \frac{1}{x-3} + 4$  is  $\dots\dots\dots$   
 (a) (3, -4) (b) (-3, -4) (c) (3, 4) (d) (-3, 4)
- (24) In triangle ABC if  $a = 5$  cm,  $b = 7$  cm. and  $m(\angle C) = 65^\circ$ , then  $c \approx \dots\dots\dots$  cm.  
 (a) 44.4 (b) 32.1 (c) 6.7 (d) 8.2
- (25)  $\frac{1}{\log_2 14} + \frac{1}{\log_7 14} = \dots\dots\dots$   
 (a) 1 (b) 2 (c) 7 (d) 14
- (26) If the function  $f : f(x) = a^x$  passing through the point (1, 3), then  $a = \dots\dots\dots$   
 (a) zero (b) 1 (c) -1 (d) 3
- (27) In any triangle XYZ,  $XY : YZ = \dots\dots\dots$   
 (a)  $\sin X : \sin Y$  (b)  $\sin Y : \sin Z$  (c)  $\sin Z : \sin X$  (d)  $\sin Z : \sin Y$

## Second

## Essay questions

Answer the following questions :

- 1 Find algebraically in  $\mathbb{R}$  the solution set of :  $\sqrt{x^2 - 4x + 4} = 10$
- 2 Find the value of :  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 5x + 6}$

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Nozha Educational Zone  
Mathematics Inspection

First

## Multiple choice questions

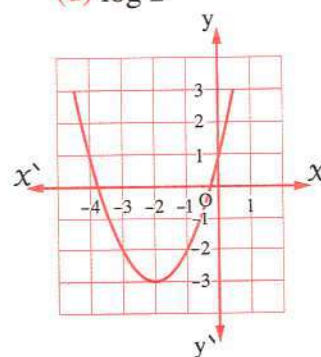
Choose the correct answer from the given ones :

- (1) The numerical value of the expression  $\frac{\log 64}{\log 8} = \dots\dots\dots$   
 (a) 2 (b) 8 (c) 80 (d) 72
- (2)  $\lim_{h \rightarrow 0} \frac{(x+h)^7 - x^7}{h} = \dots\dots\dots$   
 (a)  $x^7$  (b)  $7x^6$  (c) zero (d) 1



Interactive  
test 3

- (3) In  $\triangle ABC : a^2 + b^2 - c^2 = \dots\dots\dots$   
 (a)  $\cos A$  (b)  $ab \cos C$  (c)  $\cos C$  (d)  $2 ab \cos C$
- (4) If  $5^X = 17$ , then the value of  $X$  to the nearest two decimals =  $\dots\dots\dots$   
 (a) 1.34 (b) 1.32 (c) 1.76 (d) 1.67
- (5)  $\lim_{x \rightarrow \infty} \frac{2X-1}{3X+1} = \dots\dots\dots$   
 (a)  $\frac{2}{3}$  (b)  $\frac{3}{2}$  (c)  $\infty$  (d)  $-\infty$
- (6) The radius length of the circumcircle of  $\triangle XYZ$  in which  $X = (20 \sin X)$  cm. equals  $\dots\dots\dots$  cm.  
 (a) 5 (b) 10 (c) 20 (d) 40
- (7) If  $f(X) = 5^X$ , then  $f(-2) = \dots\dots\dots$   
 (a) -2 (b) 5 (c)  $\frac{1}{25}$  (d)  $\frac{1}{5}$
- (8) The range of the function  $f : f(X) = \frac{X-2}{2-X}$  equals  $\dots\dots\dots$   
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{2\}$  (c)  $\mathbb{R} - \{-2\}$  (d)  $\{-1\}$
- (9) All the following relations represent function  $y$  in terms of  $X$  except  $\dots\dots\dots$   
 (a)  $y = 3X + 1$  (b)  $y = X^2 - 4$  (c)  $X = y^2 - 2$  (d)  $y = \sin X$
- (10) The value of  $\log_5 49 \times \log_8 5 \times \log_9 8 \times \log_7 9 = \dots\dots\dots$   
 (a)  $\log 100$  (b)  $\log 7$  (c)  $\log 5$  (d)  $\log 2$
- (11) The rule of the function represented in the opposite figure is  $f(X) = \dots\dots\dots$   
 (a)  $(X+2)^2 + 3$   
 (b)  $-(X-2)^2 + 3$   
 (c)  $(X-1)^2 + 3$   
 (d)  $(X+2)^2 - 3$
- (12) the logarithmic form that is equivalent to the exponential form :  $2^7 = 128$  is  $\dots\dots\dots$   
 (a)  $\log_2 128 = 7$  (b)  $\log_2 7 = 128$  (c)  $\log_7 128 = 2$  (d)  $\log_7 2 = 128$
- (13) The function  $f : f(X) = a^X$  is increasing if  $\dots\dots\dots$   
 (a)  $a > 0$  (b)  $a > 1$  (c)  $a = 1$  (d)  $0 < a < 1$
- (14) The solution set in  $\mathbb{R}$  of the equation :  $|X - 7| = 2$  is  $\dots\dots\dots$   
 (a)  $\{9, 5\}$  (b)  $\{7, 3\}$  (c)  $\emptyset$  (d)  $\{3, -3\}$
- (15) In  $\triangle ABC$ ,  $m(\angle C) = 61^\circ$ ,  $m(\angle B) = 71^\circ$ ,  $b = 91$  cm., then  $a \approx \dots\dots\dots$  cm.  
 (a) 71 (b) 72 (c) 84 (d) 92





- (16)  $\lim_{x \rightarrow 1} \frac{x^5 - 1}{x - 1} = \dots\dots\dots$   
 (a) 5 (b) 1 (c) 4 (d) 20
- (17) The curve of the even function is symmetric about the straight line .....  
 (a)  $y = x$  (b)  $\overleftrightarrow{yy}$  (c)  $\overleftrightarrow{xx}$  (d)  $y = -x$
- (18) If  $\lim_{x \rightarrow 16} \frac{\sqrt{x} - 1}{x - 16} = \dots\dots\dots$   
 (a) zero (b)  $\frac{1}{2}$  (c) 1 (d) does not exist.
- (19) If the perimeter of  $\triangle ABC = 33$  cm,  $\sin A + \sin C = \frac{2}{3}$ ,  $\sin B = \frac{1}{4}$ , then  $AC = \dots\dots\dots$  cm.  
 (a) 6 (b) 9 (c) 12 (d) 15
- (20) If  $\log 3 = x$ ,  $\log 5 = y$ , then  $\log 15 = \dots\dots\dots$   
 (a)  $xy$  (b)  $\frac{x}{y}$  (c)  $x + y$  (d)  $x - y$
- (21) In  $\triangle ABC$ ,  $\frac{a}{a + b} = \frac{\sin A}{\dots\dots\dots}$   
 (a)  $\sin B$  (b)  $\sin C$  (c)  $\sin A + \sin B$  (d)  $\sin A + \sin C$
- (22) The solution set of the equation :  $\log_2 x \times \log_3 2 = 1$  in  $\mathbb{R}$  is .....  
 (a)  $\{6\}$  (b)  $\{5\}$  (c)  $\{4\}$  (d)  $\{3\}$
- (23)  $\lim_{x \rightarrow 0} \frac{x^7 - 1}{x + 1} = \dots\dots\dots$   
 (a) -2 (b) 5 (c) 1 (d) -1
- (24) The solution set of the following equation in  $\mathbb{R}$  :  $\log_x 81 = 4$  equals .....  
 (a)  $\{-3\}$  (b)  $\{3\}$  (c)  $\{3, -3\}$  (d)  $\{9\}$
- (25)  $\lim_{x \rightarrow a} \frac{ax}{3} = 12$ , then  $a = \dots\dots\dots$   
 (a)  $\pm 12$  (b)  $\pm 6$  (c) 3 (d) -3
- (26) In  $\triangle ABC$ ,  $m(\angle A) : m(\angle B) : m(\angle C) = 3 : 5 : 4$ , then  $c^2 : a^2 = \dots\dots\dots$   
 (a)  $\sqrt{6} : 2$  (b)  $2 : 3$  (c)  $4 : 3$  (d)  $3 : 2$
- (27)  $\lim_{x \rightarrow a} \frac{2x - 4}{x - 2} = \dots\dots\dots$   
 (a) 1 (b) 2 (c) -2 (d) zero

**Second**

**Essay questions**

**Answer the following questions :**

- 1** Graph the function  $f : f(x) = x^2 + 1$ , from the graph, deduce the range and it's monotony determine it's type whether it is even, odd or otherwise.
- 2** Find the value of :  $\lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x - 2}$



## First

## Multiple choice questions

Interactive  
test ④

Choose the correct answer from the given ones :

(1) The domain of the function  $f(x) = \sqrt{x-5}$  in  $\mathbb{R}$  is .....

- (a)  $[5, \infty[$  (b)  $]5, \infty[$  (c)  $]-\infty, 5]$  (d)  $]-\infty, 5[$

(2) XYZ is a triangle in which  $x = 4$  cm. ,  $y = 8$  cm. ,  $m(\angle Z) = 75^\circ$  , then  $z \approx$  ..... cm.

- (a) 6 (b) 7 (c) 8 (d) 9

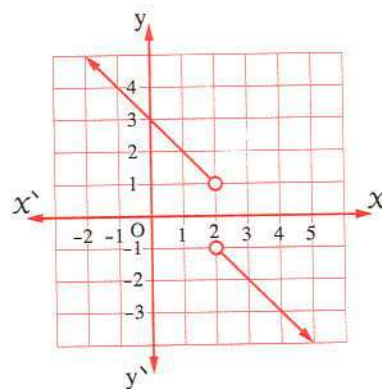
(3) The solution set of the equation :  $|x| + 5 = 0$  in  $\mathbb{R}$  is .....

- (a)  $\{5\}$  (b)  $\{-5\}$  (c)  $\{0\}$  (d)  $\emptyset$

(4) In the opposite figure :

 $\lim_{x \rightarrow 2} f(x) =$  .....

- (a) -3  
(b) 2  
(c) -1  
(d) does not exist.

(5) If  $2^{x+1} = 5^{x+1}$  , then  $7^{x+1} =$  .....

- (a) 1 (b) 49 (c) 7 (d) zero

(6) The vertex of the function  $f(x) = (x+1)^2 - 3$  is .....

- (a) (1, -3) (b) (-1, -3) (c) (1, 3) (d) (-1, 3)

(7) If  $\lim_{x \rightarrow \infty} \frac{ax^2 - 5x}{3x + 2x^2} = 4$  , then  $a =$  .....

- (a) 4 (b) 2 (c) 6 (d) 8

(8) The solution set of the equation :  $\log_x 81 = 4$  in  $\mathbb{R}$  is .....

- (a)  $\{-3\}$  (b)  $\{3\}$  (c)  $\{3, -3\}$  (d)  $\{9\}$

(9) The radius length of the circle passing through the vertices of triangle XYZ in which  $y = 10$  cm. ,  $m(\angle Y) = 30^\circ$  equals ..... cm.

- (a) 40 (b) 20 (c) 10 (d) 5

(10)  $\lim_{x \rightarrow 1} \frac{x^7 - 1}{x - 1} =$  .....

- (a) 7 (b) 1 (c) 4 (d) 42

- (11) The axis of symmetry of the function  $f(x) = x^2 + 3$  is the straight line .....
- (a)  $x = 3$  (b)  $x = 0$  (c)  $y = 3$  (d)  $y = 0$
- (12) If  $\log 2 = x$ ,  $\log 5 = y$ , then  $\log 10 = \dots\dots\dots$
- (a)  $x + y$  (b)  $x - y$  (c)  $xy$  (d)  $\frac{x}{y}$
- (13) If  $a \in \mathbb{R}$  and  $\lim_{x \rightarrow \infty} \frac{(a+3)x^3 - 4x^2 + 4}{2x^2 + 5x - 1} = -2$ , then  $a = \dots\dots\dots$
- (a)  $-7$  (b)  $-3$  (c) zero (d)  $3$
- (14) In triangle ABC if  $3 \sin A = 4 \sin B = 6 \sin C$ , then  $a : b : c = \dots\dots\dots$
- (a)  $2 : 3 : 4$  (b)  $3 : 4 : 6$  (c)  $4 : 3 : 2$  (d)  $6 : 4 : 3$
- (15) The S.S. of the equation :  $x^{\frac{2}{3}} = 25$  in  $\mathbb{R}$  is .....
- (a)  $\{5\}$  (b)  $\{-5, 5\}$  (c)  $\{125\}$  (d)  $\{-125, 125\}$
- (16)  $\log_5 125 + \log 10 + \log_3 (25 + 2) = \dots\dots\dots$
- (a)  $3$  (b)  $5$  (c)  $7$  (d)  $9$
- (17) In triangle ABC if  $a = 3$  cm. ,  $b = 5$  cm. ,  $m(\angle C) = 100^\circ$ , then the area of triangle ABC  $\approx \dots\dots\dots$  cm<sup>2</sup>
- (a)  $5$  (b)  $6$  (c)  $7$  (d)  $8$
- (18)  $\lim_{x \rightarrow 3} \frac{x^2 + 2x - 1}{3x^2 + 1} = \dots\dots\dots$
- (a)  $\frac{2}{3}$  (b)  $\frac{3}{2}$  (c)  $\frac{1}{2}$  (d)  $2$
- (19) If  $y = f(x)$  is the curve of a real function, then its image by a translation of magnitude 2 units to the left is  $g(x) = \dots\dots\dots$
- (a)  $f(x+2)$  (b)  $f(x-2)$  (c)  $f(x)+2$  (d)  $f(x)-2$
- (20)  $\lim_{x \rightarrow 3} \frac{x^2 - 6x + 9}{x - 3} = \dots\dots\dots$
- (a) zero (b)  $3$  (c)  $6$  (d) does not exist.
- (21) In triangle ABC, if  $m(\angle B) = 30^\circ$ ,  $c = 12\sqrt{3}$  cm. ,  $m(\angle C) = 60^\circ$ , then  $b = \dots\dots\dots$
- (a)  $6\sqrt{3}$  (b)  $6$  (c)  $9$  (d)  $12$
- (22) The function  $f(x) = a^x$  is increasing if .....
- (a)  $a > 0$  (b)  $a > 1$  (c)  $a = 1$  (d)  $0 < a < 1$
- (23)  $\lim_{h \rightarrow 0} \frac{(3+h)^4 - 81}{h} = \dots\dots\dots$
- (a)  $4$  (b)  $81$  (c)  $108$  (d) does not exist.
- (24) If ABCD is a cyclic quadrilateral, then  $\cos B + \cos D = \dots\dots\dots$
- (a) zero (b)  $1$  (c)  $\frac{1}{2}$  (d)  $-1$



(25) If  $\log_3 (2X + 3) = 2$ , then  $X = \dots\dots\dots$

- (a) 2 (b) 3 (c) 4 (d) 9

(26) If  $\lim_{x \rightarrow \infty} (2X^{-3} + 3X^{-4} + a) = 3$ , then  $a = \dots\dots\dots$

- (a) 6 (b) 5 (c) 3 (d)  $\infty$

(27) The S.S. of the equation :  $3^{X+1} + 3^X = 12$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\{0\}$  (b)  $\{1\}$  (c)  $\{1, 0\}$  (d)  $\{2\}$

## Second Essay questions

Answer the following questions :

1 Draw the graph of the function  $f(X) = (X - 1)^2 + 2$  and from the graph find range of the function and discuss its type for being even, odd or neither.

2 If  $\lim_{x \rightarrow a} \frac{X^6 - a^6}{X^5 - a^5} = \frac{18}{5}$ , then find the value of  $a$

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Giza Governorate



Aguzza Educational Zone

## First Multiple choice questions

Choose the correct answer from the given ones :

(1) The domain of the function  $f(X) = \sqrt{X + 2}$  is  $\dots\dots\dots$

- (a)  $[-2, \infty[$  (b)  $] - \infty, -2[$  (c)  $\mathbb{R} - \{-2\}$  (d)  $\mathbb{R}$

(2) If  $\log_a (X - 3) + \log_a (X) = \log_a 4$ , then  $X = \dots\dots\dots$

- (a) -1 (b) 3 (c) 4 (d) -1, 4

(3) All the functions defined by the following rules are even except  $\dots\dots\dots$

- (a)  $X|X|$  (b)  $X^2 \sec X$  (c)  $7X^2 + 5$  (d)  $\cos X$

(4) The solution set of the equation :  $X^{\frac{6}{5}} - 64 = 0$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\{-32, 32\}$  (b)  $\{32\}$  (c)  $\{-8, 8\}$  (d)  $\emptyset$

(5) If  $f(X) = 3^X$ , then the solution set in  $\mathbb{R}$  of the equation :  $f(X - 2) + f(X - 1) = 36$  is  $\dots\dots\dots$

- (a)  $\{9\}$  (b)  $\{4\}$  (c)  $\{2\}$  (d)  $\{3\}$

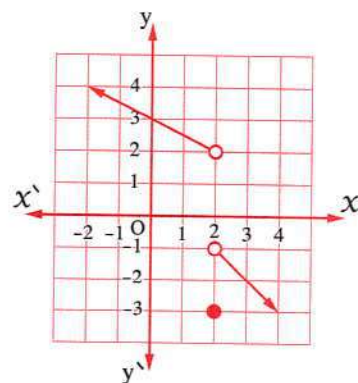
(6) The curve  $g(X) = |X + 3|$  is the same as the curve  $f(X) = |X|$  by translation 3 units in the direction of  $\dots\dots\dots$

- (a)  $\overrightarrow{OX}$  (b)  $\overrightarrow{OX}$  (c)  $\overrightarrow{OY}$  (d)  $\overrightarrow{OY}$

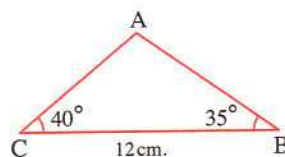


Interactive test 5

- (7) The solution set of the inequality :  $|3 - 2x| \leq 1$  in  $\mathbb{R}$  is .....
- (a)  $[1, 2]$  (b)  $]1, 2[$  (c)  $\mathbb{R} - ]1, 2[$  (d)  $\mathbb{R} - [1, 2]$
- (8) The range of the function  $f : f(x) = x^2$  is .....
- (a)  $[0, \infty[$  (b)  $]0, \infty[$  (c)  $] - \infty, 0]$  (d)  $] - \infty, 0[$
- (9) The point of symmetry of the function  $f : f(x) = \frac{2x-1}{x}$  is .....
- (a) (1, 1) (b) (2, 1) (c) (1, 2) (d) (0, 2)
- (10) If  $5^{x-7} = 4^{7-x}$ , then  $x =$  .....
- (a)  $\frac{5}{4}$  (b) 7 (c)  $\frac{4}{5}$  (d) zero
- (11) The numerical value of the expression  $\frac{\log a^b}{\log a^c} =$  .....
- (a)  $\frac{b}{c}$  (b) a (c)  $a \frac{b}{c}$  (d)  $b - c$
- (12) If  $\sqrt[3]{x^2} = 9$ , then  $x =$  .....
- (a) 27 (b) 9 (c)  $\pm 3$  (d)  $\pm 27$
- (13) If  $3^{2x} = 5$ , then  $9^x =$  .....
- (a) 10 (b) 25 (c) 5 (d) -5
- (14) If  $\lim_{x \rightarrow 1} \frac{2x+a}{x+1} = 5$ , then  $a =$  .....
- (a) 2 (b) 5 (c) 8 (d) 10
- (15) In the opposite figure :
- $\lim_{x \rightarrow 2} f(x) =$  .....
- (a) 2 (b) -3 (c) 1 (d) does not exist.
- (16)  $\lim_{x \rightarrow 1} \frac{2x-4}{x-2} =$  .....
- (a) 1 (b) 2 (c) -2 (d) zero
- (17) If  $\lim_{x \rightarrow \infty} \frac{10x^m - 2x + 3}{7x - 2x^3 + 1} = -5$ , then  $m =$  .....
- (a) 4 (b) 3 (c) 1 (d) -5
- (18)  $\lim_{x \rightarrow 1} \frac{b}{x+1} = 5$ , then  $b =$  .....
- (a) 5 (b) -1 (c) 1 (d) 10



- (19)  $\lim_{x \rightarrow 1} \frac{2x+1}{\sqrt{x+3}-1} = \dots\dots\dots$   
 (a) 3 (b) -3 (c) 2 (d) does not exist.
- (20)  $\lim_{x \rightarrow 0} \frac{\pi}{4} = \dots\dots\dots$   
 (a) 0 (b) 45 (c)  $\frac{\pi}{4}$  (d) does not exist.
- (21)  $\lim_{x \rightarrow \infty} (2)^{\frac{3}{x}} = \dots\dots\dots$   
 (a) zero (b)  $\infty$  (c) 1 (d) 2
- (22) In  $\triangle XYZ$ ,  $3 \sin X = 4 \sin Y = 2 \sin Z$ , then  $X : y : z = \dots\dots\dots$   
 (a) 2 : 3 : 6 (b) 6 : 2 : 3 (c) 4 : 3 : 6 (d) 3 : 4 : 2
- (23) In triangle ABC,  $m(\angle A) = 45^\circ$ , then length of the radius of its circumcircle = 6 cm., then  $a = \dots\dots\dots$  cm.  
 (a) 13 (b)  $6\sqrt{2}$  (c) 12 (d)  $\sqrt{2}$
- (24) In triangle ABC,  $\frac{a}{a+b} = \frac{\sin A}{\dots\dots\dots}$   
 (a)  $\sin B$  (b)  $\sin C$  (c)  $\sin A + \sin B$  (d)  $\sin A + \sin C$
- (25) In  $\triangle ABC$ ,  $\frac{b}{2r} = \dots\dots\dots$  where  $r$  is the length of the radius of the circumcircle of  $\triangle ABC$   
 (a)  $\sin B$  (b)  $\sin(A+B)$  (c)  $\sin A + \sin B$  (d)  $\sin A$
- (26) In  $\triangle ABC$ ,  $m(\angle A) = 112^\circ$ ,  $m(\angle B) = 33^\circ$ ,  $c = 19$  cm., then  $b \approx \dots\dots\dots$  to the nearest cm.  
 (a) 16 (b) 17 (c) 18 (d) 20
- (27) In the opposite figure :  
 The length of  $\overline{AB} \approx \dots\dots\dots$  to the nearest cm.  
 (a) 6 (b) 7  
 (c) 8 (d) 9



## Second

## Essay questions

Answer the following questions :

1 Find :  $\lim_{x \rightarrow -3} \frac{x^6 - 729}{x^3 + 27}$

- 2 Draw the curve of the function :  $f(x) = 3 - (x-1)^2$ , from the curve : determine the domain and the range, discuss its monotonicity, determine the type of the function (even, odd or otherwise)



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Math Inspection

**First Multiple choice questions**



Interactive test 6

Choose the correct answer from the given ones :

- (1) The domain of the function  $f : f(x) = \sqrt{x-3}$  is .....
- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{3\}$  (c)  $[3, \infty[$  (d)  $] -\infty, 3[$
- (2) The range of the function  $f : f(x) = \begin{cases} 0 & , x \leq 0 \\ 1 & , x > 0 \end{cases}$  is .....
- (a)  $\{1\}$  (b)  $\{0\}$  (c)  $\mathbb{R}$  (d)  $\{0, 1\}$
- (3) The type the function  $f : f(x) = \frac{\sin x}{x}$  is .....
- (a) even. (b) odd.  
(c) neither even nor odd. (d) linear.
- (4) The point of symmetry of the curve of the function  $f : f(x) = \frac{1}{x-3} + 4$  is .....
- (a)  $(3, -4)$  (b)  $(-3, -4)$  (c)  $(3, 4)$  (d)  $(-3, 4)$
- (5) The solution set of the equation :  $|2x-4| = |x+1|$  is .....
- (a)  $\{1, 5\}$  (b)  $\{5, -1\}$  (c)  $\{1, -5\}$  (d)  $\{-5, -1\}$
- (6) If  $3^{x-5} = 9$ , then  $x =$  .....
- (a)  $-7$  (b)  $-3$  (c)  $2$  (d)  $7$
- (7)  $\sqrt[4]{x^4 y^8} =$  .....
- (a)  $x y^2$  (b)  $|x| y^2$  (c)  $\pm x y^2$  (d)  $x |y^2|$
- (8) If  $f(x) = (5)^{-x}$ , then  $\frac{f(x-1)}{f(x+1)} =$  .....
- (a)  $5$  (b)  $\frac{1}{5}$  (c)  $25$  (d)  $\frac{1}{25}$
- (9) An amount of 5000 pounds is deposited in a bank gives a yearly compound interest 5 % for 7 years  $\approx$  ..... pounds.
- (a) 6750 (b) 7035.5 (c) 5350 (d) 8500
- (10) The solution set of the equation  $\log_x (3x-2) = 2$  in  $\mathbb{R}$  is .....
- (a)  $\{1, 2\}$  (b)  $\{1\}$  (c)  $\{2\}$  (d)  $\emptyset$
- (11) The curve of the function  $f : f(x) = \log_2 x$  is passing through the point  $(8, \dots)$
- (a) 2 (b) 3 (c)  $\log_2 3$  (d) 256

- (12) If  $x = 5 + 2\sqrt{6}$ , then  $\log\left(x + \frac{1}{x}\right) = \dots\dots\dots$   
 (a) 1 (b)  $5 - 2\sqrt{6}$  (c) 10 (d)  $5 + 2\sqrt{6}$
- (13) If  $3^x = 5$ , then  $x = \dots\dots\dots$   
 (a) 3 (b)  $\log_3 5$  (c)  $\log_5 3$  (d)  $\frac{5}{3}$
- (14)  $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x^2 - 4} = \dots\dots\dots$   
 (a)  $\frac{4}{5}$  (b)  $\frac{5}{4}$  (c)  $\frac{2}{5}$  (d)  $-\frac{2}{5}$
- (15)  $\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - 1}{x} = \dots\dots\dots$   
 (a) zero (b)  $\sqrt{2}$  (c)  $\frac{1}{2}$  (d) not exist.
- (16) If  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$  exist, then  $a = \dots\dots\dots$   
 (a) -1 (b) 1 (c) 2 (d) 4
- (17)  $\lim_{x \rightarrow -2} \frac{x^7 + 128}{x^4 - 16} = \dots\dots\dots$   
 (a) 9 (b) -9 (c) -14 (d) 14
- (18) If  $\lim_{x \rightarrow k} \frac{x^5 - k^5}{x - k} = 80$ , then  $k = \dots\dots\dots$   
 (a) 2 (b) -2 (c)  $\pm 2$  (d) 16
- (19) The  $\lim_{x \rightarrow \infty} \frac{x^7 - 2x^3}{2x^4 - 3x^2 - 1} = \dots\dots\dots$   
 (a) zero (b) 3 (c)  $\infty$  (d)  $\frac{1}{2}$
- (20)  $\lim_{x \rightarrow \infty} \frac{\sqrt{8 + 9x^2}}{x} = \dots\dots\dots$   
 (a)  $2\sqrt{2}$  (b) 3 (c)  $-2\sqrt{2}$  (d) -3
- (21)  $\lim_{x \rightarrow \pi} \frac{\cos 2x}{x} = \dots\dots\dots$   
 (a) 2 (b) 1 (c)  $\frac{1}{\pi}$  (d) zero
- (22) DEF is a triangle in which  $m(\angle D) = 80^\circ$  and  $m(\angle E) = 60^\circ$ , if  $f = 12$  cm., then  $d = \dots\dots\dots$  cm.  
 (a)  $\frac{12 \sin 80^\circ}{\sin 40^\circ}$  (b)  $\frac{12 \sin 80^\circ}{\sin 60^\circ}$  (c)  $\frac{12 \sin 40^\circ}{\sin 80^\circ}$  (d)  $\frac{12 \cos 80^\circ}{\cos 40^\circ}$
- (23) ABC is a triangle in which  $\frac{\sin A}{3} = \frac{\sin B}{5} = \frac{\sin C}{4}$ , then  $a : b : c = \dots\dots\dots$   
 (a) 6 : 5 : 8 (b) 8 : 5 : 6 (c) 7 : 2 : 4 (d) 3 : 5 : 4
- (24) In  $\triangle LMN$ ,  $l = 5$  cm.,  $m = 7$  cm.,  $m(\angle N) = 60^\circ$ , then  $n = \dots\dots\dots$  cm. (to the nearest tenth)  
 (a) 6.2 (b) 5 (c) 4.3 (d) 3.5

(25) In  $\Delta XYZ$ ,  $y^2 + z^2 - x^2 = 2yz \times \dots\dots\dots$

- (a)  $\cos X$  (b)  $\sin Z$  (c)  $\cos Z$  (d)  $\sin X$

(26) The number of possible solutions of  $\Delta XYZ$  in which  $x = 5$  cm,  $y = 6$  cm,  $m(\angle X) = 70^\circ$  equals  $\dots\dots\dots$

- (a) zero (b) 2 (c) 1 (d) 3

(27) If ABC is a triangle in which  $\frac{2}{\sin A} = \frac{3}{\sin B} = \frac{4}{\sin C}$ , then the measure of the smallest angle in the triangle  $\approx \dots\dots\dots$

- (a)  $57^\circ 28'$  (b)  $41^\circ 12'$  (c)  $28^\circ 57'$  (d)  $36^\circ 52'$

## Second Essay questions

Answer the following questions :

1 Find the following limit (show your steps) :  $\lim_{x \rightarrow -3} \frac{x^3 - 10x - 3}{x^2 + 2x - 3}$

2 Find algebraically in  $\mathbb{R}$  the solution set of the following inequality :  $|x - 5| > 3$

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Math Inspection

## First Multiple choice questions

Choose the correct answer from the given ones :

(1) The solution set of the equation  $|x| + 4 = 0$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\{-4\}$  (b)  $\{2\}$  (c)  $\{-2, 2\}$  (d)  $\emptyset$

(2) The domain of the function  $f(x) = \frac{5}{\sqrt{x-1}}$  is  $\dots\dots\dots$

- (a)  $\mathbb{R}^+$  (b)  $\mathbb{R} - \{1\}$  (c)  $\mathbb{R} - \{0\}$  (d)  $]1, \infty[$

(3) The point of symmetry of the function  $f(x) = \frac{-1}{x-3} + 4$  is  $\dots\dots\dots$

- (a)  $(3, 4)$  (b)  $(-3, 4)$  (c)  $(3, -4)$  (d)  $(-3, -4)$

(4) The solution set of the inequality :  $\sqrt{x^2} - 9 < 0$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $] -3, 3[$  (b)  $] -9, 9[$  (c)  $\{3\}$  (d)  $\{9\}$

(5) The range of the function  $f(x) = |x - 2| + 3$  is  $\dots\dots\dots$

- (a)  $] -\infty, 2[$  (b)  $[2, \infty[$  (c)  $[3, \infty[$  (d)  $] -2, \infty[$



Interactive test 7



- (6) If  $\left(\frac{2}{5}\right)^{x-3} = \frac{5\sqrt{5}}{2\sqrt{2}}$ , then  $x = \dots\dots\dots$   
 (a)  $\frac{3}{2}$  (b)  $\frac{9}{2}$  (c) 6 (d) 3
- (7)  $\log_{\sqrt{2}} 4 \times \log_{\sqrt{2}} 2 = \log_{\sqrt{2}} \dots\dots\dots$   
 (a) 8 (b) 16 (c) 32 (d) 64
- (8) If  $\log 3 = x$  and  $\log 4 = y$ , then  $\log 12 = \dots\dots\dots$   
 (a)  $x + y$  (b)  $xy$  (c)  $x - y$  (d)  $\log x + \log y$
- (9) If  $f(x) = b^x$  is passes through the point  $(2, 4)$ , then  $b = \dots\dots\dots$   
 (a) 2 (b)  $\frac{1}{2}$  (c) 4 (d)  $\frac{1}{4}$
- (10) If  $\log_2 x = 3$ , then  $\log_8 x = \dots\dots\dots$   
 (a)  $\frac{3}{2}$  (b)  $\frac{2}{3}$  (c) 6 (d) 1
- (11) If  $\sqrt[3]{x^2} = 4$ , then  $x = \dots\dots\dots$   
 (a) 8 (b) 16 (c)  $\pm 8$  (d)  $\pm 16$
- (12)  $\log_2 12 + \log_2 \frac{2}{3} = \dots\dots\dots$   
 (a) 2 (b) 3 (c) 5 (d) 8
- (13) If  $4^{x-2} = 3^{2x-4}$ , then  $x = \dots\dots\dots$   
 (a) 2 (b) 3 (c) 4 (d) 5
- (14)  $\lim_{x \rightarrow 2} 5 = \dots\dots\dots$   
 (a) 10 (b) 7 (c) 5 (d) 2
- (15)  $\lim_{x \rightarrow -2} \frac{1}{x} = \dots\dots\dots$   
 (a) 1 (b) -1 (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
- (16)  $\lim_{x \rightarrow 1} \frac{x^5 - 1}{x^3 - 1} = \dots\dots\dots$   
 (a)  $\frac{5}{3}$  (b)  $-\frac{5}{3}$  (c) 15 (d) -15
- (17)  $\lim_{x \rightarrow \infty} \frac{3 - x}{x} = \dots\dots\dots$   
 (a) -1 (b) 0 (c) 3 (d) undefined.
- (18)  $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1} = \dots\dots\dots$   
 (a) 0 (b) 1 (c) 2 (d) 3
- (19)  $\lim_{x \rightarrow \infty} \frac{(a-2)x^4 + bx^3 - 5}{3x^3 + 7} = \frac{1}{3}$ , then  $a + b = \dots\dots\dots$   
 (a) 2 (b) 3 (c) 4 (d) 5

- (20)  $\lim_{x \rightarrow -3} \frac{x^3 + 27}{x^2 - 9} = \dots\dots\dots$   
 (a)  $\frac{3}{2}$  (b)  $\frac{-9}{2}$  (c)  $\frac{2}{3}$  (d)  $\frac{1}{2}$
- (21)  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\sin x}{x} = \dots\dots\dots$   
 (a) 1 (b)  $\frac{\pi}{2}$  (c)  $\frac{2}{\pi}$  (d)  $\frac{1}{90^\circ}$
- (22) In  $\triangle ABC$ , if  $\frac{a^2 + b^2 - c^2}{2ab} = 0$ , then  $\dots\dots\dots$   
 (a)  $m(\angle A) = 60^\circ$  (b)  $m(\angle B) = 90^\circ$   
 (c)  $m(\angle C) = 120^\circ$  (d)  $m(\angle A) + m(\angle B) = 90^\circ$
- (23) In  $\triangle XYZ$ , if  $X = y = 8$  cm. and the perimeter of  $\triangle XYZ = 26$  cm., then  $m(\angle Z) \approx \dots\dots\dots$   
 (a)  $35.3^\circ$  (b)  $52.3^\circ$  (c)  $77.4^\circ$  (d)  $108^\circ$
- (24) In  $\triangle ABC$ , if  $a = 3$  cm.,  $b = 4$  cm.,  $c = 6$  cm., then  $\cos C = \dots\dots\dots$   
 (a)  $\frac{-11}{24}$  (b)  $\frac{-11}{12}$  (c)  $\frac{11}{24}$  (d)  $\frac{11}{12}$
- (25) In  $\triangle ABC$ , if  $a = 6$  cm.,  $m(\angle B) = 2m(\angle A) = 80^\circ$ , then  $c = \dots\dots\dots$   
 (a)  $\frac{6 \sin 40^\circ}{\sin 60^\circ}$  (b)  $\frac{\sin 60}{6 \sin 40^\circ}$  (c)  $\frac{\sin 40^\circ}{6 \sin 60^\circ}$  (d)  $\frac{6 \sin 60^\circ}{\sin 40^\circ}$
- (26) If the length of the radius of the circumcircle of  $\triangle ABC = 4$  cm.,  $m(\angle A) = 30^\circ$ , then  $a = \dots\dots\dots$  cm.  
 (a) 2 (b) 4 (c)  $2\sqrt{3}$  (d)  $4\sqrt{3}$
- (27) In  $\triangle ABC$ ,  $\frac{\dots\dots\dots}{\sin B + \sin C} = \frac{a}{\sin A}$   
 (a)  $b$  (b)  $b + c$   
 (c) area of  $\triangle ABC$  (d) The perimeter of  $\triangle ABC$

## Second Essay questions

**Answer the following questions :**

- 1** Use the curve of  $f(x) = \frac{1}{x}$  to represent the curve of  $g(x) = 2 + f(x - 1)$ , from the graph determine the domain and the range.

**2** Find :

- (1)  $\lim_{x \rightarrow 5} \frac{x - 5}{\sqrt{x - 1} - 2}$   
 (2)  $\lim_{x \rightarrow \infty} \frac{x + 2}{\sqrt{9x^2 + 25}}$

Interactive  
test 8**First Multiple choice questions**

Choose the correct answer from the given ones :

- (1) The domain of the function  $f(x) = \sqrt{x-4}$  is .....
- (a)  $[4, \infty[$  (b)  $]-\infty, 4[$  (c)  $]4, \infty[$  (d)  $]-\infty, 4]$
- (2) The function which is even from the functions defined by the following rules  
 $f(x) = \dots\dots\dots$
- (a)  $x \cos x$  (b)  $x \sin x$  (c)  $x^3 + 1$  (d)  $\tan x$
- (3) The range of function  $f(x) = -|x|$  is .....
- (a)  $\mathbb{R}$  (b)  $]0, \infty[$  (c)  $]-\infty, 0[$  (d)  $]-\infty, 0]$
- (4) The symmetric point of the function  $f : f(x) = x^3 - 1$  is .....
- (a)  $(0, 1)$  (b)  $(0, -1)$  (c)  $(-1, 1)$  (d)  $(0, 0)$
- (5) The function  $f(x) = (x-2)^2 + 3$  is increasing on the interval .....
- (a)  $\mathbb{R}$  (b)  $]2, \infty[$  (c)  $[-2, 2]$  (d)  $]-\infty, 2[$
- (6) If  $3^{x-5} = 9$ , then  $x = \dots\dots\dots$
- (a) 2 (b) 3 (c) 5 (d) 7
- (7) The solution set of the equation  $3^{x+1} + 3^x = 12$  in  $\mathbb{R}$  is .....
- (a)  $\{0\}$  (b)  $\{1\}$  (c)  $\{3\}$  (d)  $\{0, 1\}$
- (8) The exponential function of base  $a$  is increasing if .....
- (a)  $a > 0$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = 1$
- (9) An amount of 5000 pounds is deposited in a bank gives a yearly compound interest 5 % for 7 years  $\approx \dots\dots\dots$  pounds.
- (a) 5350 (b) 6750 (c) 7035.5 (d) 8500
- (10) If  $\log_3 x = 2$ , then  $x = \dots\dots\dots$
- (a) 3 (b) 5 (c) 8 (d) 9
- (11)  $\log_2 5 \times \log_5 2 = \dots\dots\dots$
- (a) 1 (b) 10 (c)  $\log 10$  (d)  $\log 7$
- (12) If  $\log x + \log 5 = 2$ , then  $x = \dots\dots\dots$
- (a) 3 (b) 8 (c) 17 (d) 20



- (13) The solution set of the equation  $\log_X (64 X) = 4$  in  $\mathbb{R}$  is .....
- (a)  $\{2\}$  (b)  $\{4\}$  (c)  $\{0, 4\}$  (d)  $\{6\}$
- (14)  $\lim_{x \rightarrow 4} (3x - \sqrt{x}) = \dots\dots\dots$
- (a) 8 (b) 10 (c) 14 (d) 16
- (15)  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 4} = \dots\dots\dots$
- (a) 2 (b) 3 (c) 4 (d) 6
- (16)  $\lim_{x \rightarrow 3} \frac{\sqrt{x+1} - 2}{x-3} = \dots\dots\dots$
- (a)  $\frac{1}{4}$  (b) 4 (c)  $\frac{1}{6}$  (d) 6
- (17)  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^3 - 8} = \dots\dots\dots$
- (a) zero (b)  $\frac{5}{3}$  (c) 4 (d)  $6\frac{2}{3}$
- (18)  $\lim_{x \rightarrow 0} \frac{(x^2 + 2)^2 - 4}{4x} = \dots\dots\dots$
- (a) zero (b) 2 (c) 4 (d) 8
- (19)  $\lim_{x \rightarrow 0} \frac{(x+1)^9 - 1}{x} = \dots\dots\dots$
- (a) zero (b) 1 (c) 9 (d) 10
- (20)  $\lim_{x \rightarrow \infty} (3x^{-5} + 4x^{-2} + 5) = \dots\dots\dots$
- (a) zero (b) 5 (c) 12 (d)  $\infty$
- (21) If  $\lim_{x \rightarrow \infty} \frac{ax+6}{2x-7} = 4$ , then  $a = \dots\dots\dots$
- (a) 2 (b) 4 (c) 6 (d) 8
- (22) In  $\Delta ABC$  if  $m(\angle A) = 60^\circ$ ,  $m(\angle B) = 50^\circ$  and the length of the radius of its circumcircle = 5 cm, then the area of triangle  $\approx \dots\dots\dots$  to the nearest  $\text{cm}^2$ .
- (a) 9 (b) 12 (c) 31 (d) 62
- (23) If ABCD is a cyclic quadrilateral, then  $\cos A + \cos C = \dots\dots\dots$
- (a) 1 (b) zero (c)  $\frac{1}{2}$  (d) -1
- (24) In  $\Delta XYZ$ , then  $2xz \times \dots\dots\dots = x^2 + z^2 - y^2$
- (a)  $\cos X$  (b)  $\cos Y$  (c)  $\cos Z$  (d)  $\sin Y$
- (25) In  $\Delta ABC$  if  $a = 4$  cm,  $b = 7$  cm,  $m(\angle C) = 120^\circ$ , then the area of  $\Delta ABC = \dots\dots\dots$
- (a) 7 (b)  $7\sqrt{3}$  (c) 14 (d)  $14\sqrt{3}$

(26) In  $\triangle ABC$ ,  $m(\angle A) = 30^\circ$ ,  $a = 7$  cm., then the length of diameter of its circumcircle is .....

- (a) 7 (b)  $7\sqrt{2}$  (c) 14 (d)  $14\sqrt{2}$

(27) In  $\triangle ABC$  if  $\sin A : \sin B : \sin C = 3 : 4 : 2$ , then  $m(\angle C) \approx$  ..... nearest degree.

- (a) 29 (b) 57 (c) 82 (d) 89

## Second Essay questions

Answer the following questions :

1 Graph the function  $f : f(x) = (x-2)^2$  determine its type whether it is even, odd or otherwise and deduce the range.

2 If  $\lim_{x \rightarrow a} \frac{x^8 - a^8}{x^5 - a^5} = 25$  find the value of  $a$

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El-Dakahlia Governorate



Maths Supervision



Interactive test 9

## First Multiple choice questions

Choose the correct answer from the given ones :

(1) In any triangle XYZ,  $z : x =$  .....

- (a)  $\sin X : \sin Y$  (b)  $\sin Y : \sin Z$  (c)  $\sin Z : \sin X$  (d)  $\sin Z : \sin Y$

(2) In  $\triangle ABC$ , if  $\frac{\sin A}{4} = \frac{\sin B}{9} = \frac{\sin C}{7}$ , then the greatest angle in measure is .....

- (a)  $\angle A$  (b)  $\angle B$  (c)  $\angle C$  (d) right.

(3) In  $\triangle ABC$ ,  $b = 2$  cm.,  $c = 2.5$  cm.,  $\cos A = \frac{2}{5}$ , then the type of  $\triangle ABC$  according to its sides is .....

- (a) a right-angled triangle. (b) an isosceles triangle.  
(c) an equilateral triangle. (d) a scalene triangle.

(4) The radius length of the circumcircle of the triangle ABC in which  $m(\angle A) = 30^\circ$ , and  $a = 10$  cm. is ..... cm.

- (a) 5 (b) 10 (c) 20 (d) 40

(5)  $\triangle XYZ$  is an equilateral triangle, the length of its sides is  $10\sqrt{3}$  cm., then the length of the diameter of its circumcircle is ..... cm.

- (a) 5 (b) 10 (c) 15 (d) 20

- (6) In  $\triangle ABC$ ,  $6a = 4b = 3c$ , then the measure of the smallest angle in triangle  $\approx$  .....  
 (a)  $57^\circ 28'$  (b)  $41^\circ 12'$  (c)  $28^\circ 57'$  (d)  $36^\circ 52'$
- (7) In all the following relation,  $y$  is a function in  $x$  except .....  
 (a)  $y = 3x + 1$  (b)  $y = x^2 - 4$  (c)  $y^2 = x - 2$  (d)  $y = \sin x$
- (8) The domain of the function  $f : f(x) = \sqrt{x-3}$  is .....  
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{3\}$  (c)  $[3, \infty[$  (d)  $]-\infty, 3]$
- (9) The type of function  $f : f(x) = \frac{\sin x}{x}$  is .....  
 (a) even. (b) odd.  
 (c) linear. (d) neither even nor odd.
- (10) The function  $f : f(x) = \begin{cases} 2 & , x > 0 \\ -2 & , x < 0 \end{cases}$  is symmetric about the point .....  
 (a)  $(2, 0)$  (b)  $(-2, 0)$  (c)  $(0, 0)$  (d)  $(2, -2)$
- (11) The point of symmetry of the curve of the function  $f : f(x) = \frac{1}{x-3} + 4$  is .....  
 (a)  $(3, 4)$  (b)  $(3, -4)$  (c)  $(-3, 4)$  (d)  $(-3, -4)$
- (12)  $\lim_{x \rightarrow 3} 15 =$  .....  
 (a) 4 (b) 45 (c) 15 (d) 18
- (13)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} =$  .....  
 (a) undefined. (b) 8 (c) -4 (d) 4
- (14)  $\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - 1}{x} =$  .....  
 (a) zero (b)  $\sqrt{2}$  (c)  $\frac{1}{2}$  (d) has no existence.
- (15) If  $\lim_{x \rightarrow 2} \frac{a}{x+1} = 4$ , then  $a =$  .....  
 (a) 3 (b) 4 (c) 12 (d)  $\frac{2}{3}$
- (16)  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^3 - 8} =$  .....  
 (a) 4 (b) zero (c)  $6\frac{2}{3}$  (d)  $\frac{5}{3}$
- (17)  $\lim_{x \rightarrow 0} \frac{(x+1)^9 - 1}{x} =$  .....  
 (a) 9 (b) 1 (c) zero (d) 10
- (18)  $\lim_{x \rightarrow \infty} \left( \frac{3}{x^2} - 2 \right) =$  .....  
 (a) 3 (b) 2 (c) -3 (d) -2
- (19)  $\lim_{x \rightarrow \infty} \frac{2x^2 + 1}{x^2 + 1} =$  .....  
 (a) zero (b) 2 (c)  $\infty$  (d) doesn't exist.



- (20)  $a^m \times a^m = \dots\dots\dots$   
 (a)  $a^{m^2}$  (b)  $a^{2m}$  (c)  $2a^m$  (d)  $ma^2$
- (21) If  $3^{x-5} = 9$ , then  $x = \dots\dots\dots$   
 (a)  $-7$  (b)  $-3$  (c)  $2$  (d)  $7$
- (22) Which of the following is not equal to  $\sqrt[5]{x^4} = \dots\dots\dots$   
 (a)  $(\sqrt[5]{x})^4$  (b)  $\sqrt[4]{x^5}$  (c)  $x^{\frac{4}{5}}$  (d)  $(x^{\frac{1}{5}})^4$
- (23) If the curve of the function  $f : f(x) = a^x$  passing through  $(1, 3)$ , then  $a = \dots\dots\dots$   
 (a) zero (b)  $1$  (c)  $-1$  (d)  $3$
- (24)  $\log_a x = y$  is equivalent to  $\dots\dots\dots$   
 (a)  $\log_a y = x$  (b)  $a^y = x$  (c)  $a^x = y$  (d)  $y = ax$
- (25) The solution set of the equation  $\log_x (x+6) = 2$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\{3\}$  (b)  $\{3, -2\}$  (c)  $\{3, 1\}$  (d)  $\{6, 1\}$
- (26) The curve of the function  $f : f(x) = \log_2 x$  passing through the point  $(8, \dots\dots\dots)$   
 (a)  $2$  (b)  $3$  (c)  $\log_2 3$  (d)  $256$
- (27)  $\frac{1}{\log_2 14} + \frac{1}{\log_7 14} = \dots\dots\dots$   
 (a)  $1$  (b)  $2$  (c)  $7$  (d)  $14$

## Second

## Essay questions

Answer the following questions :

- 1 Draw the curve of the function  $f$  where  $f(x) = x^2$ ,  $x \in \mathbb{R}$ , from graph determine the range and the type of the function (even, odd, or neither even nor odd)
- 2 Find :  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$

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Damietta Governorate



Maths Inspection

First

## Multiple choice questions

Choose the correct answer from the given ones :

- (1) The domain of the function  $f : f(x) = \sqrt{x-5}$  is  $\dots\dots\dots$   
 (a)  $[5, \infty[$  (b)  $] -\infty, 5]$  (c)  $]5, \infty[$  (d)  $[-5, \infty[$
- (2) Which of the functions that are defined by the following rules represents an exponential decay function ?  
 (a)  $f(x) = 2^x$  (b)  $f(x) = \left(\frac{1}{3}\right)^{-x}$  (c)  $f(x) = 3^x$  (d)  $f(x) = \left(\frac{2}{3}\right)^x$

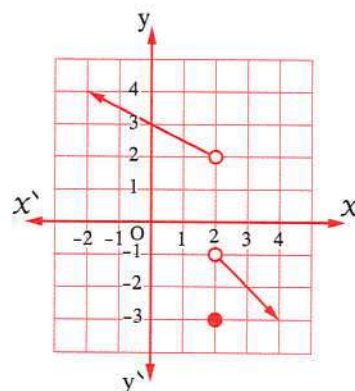


Interactive test 10

(3) In the opposite figure :

$$\lim_{x \rightarrow 2} f(x) = \dots\dots\dots$$

- (a) -3  
(b) 2  
(c) -1  
(d) does not exist.



(4) A circle with diameter of length 20 cm. , passes through the vertices of  $\triangle ABC$  which is an acute-angled triangle in which  $BC = 10$  cm. , then  $m(\angle A) = \dots\dots\dots^\circ$

- (a) 30 (b) 60 (c) 45 (d) 150

(5) The even function from the functions that are defined by the following rules is .....

- (a)  $f(x) = x^3$  (b)  $g(x) = 3x$  (c)  $h(x) = \frac{1}{x}$  (d)  $n(x) = x \sin x$

(6) If  $2^{x-1} = 7$  , then  $x \approx \dots\dots\dots$

- (a) 2.81 (b) 3.81 (c) 2.6 (d) 3.6

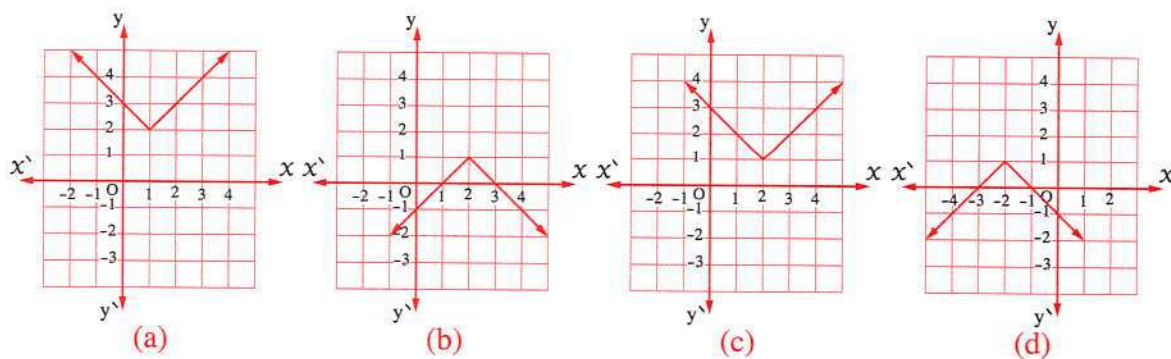
(7) If  $\lim_{x \rightarrow 3} \frac{x^2 - 2x + k}{x^2 - 9} = m$  , where  $m \in \mathbb{R}$  , then  $k \times m = \dots\dots\dots$

- (a)  $\frac{2}{3}$  (b) -3 (c) -2 (d) -1

(8) In  $\triangle ABC$  ,  $\frac{2b}{\sin B} = \dots\dots\dots r$  (where  $r$  is the radius of its circumcircle)

- (a) 1 (b) 2 (c) 4 (d) 8

(9) If  $f : f(x) = 1 - |x - 2|$  , then the figure which represents the function  $f$  is .....



(10) If  $\lim_{x \rightarrow 3} \frac{x^2 - 2x - a}{x - 3} = 4$  , then  $a = \dots\dots\dots$

- (a) -5 (b) -3 (c) -1 (d) 3

(11) In  $\triangle ABC$  ,  $a = 9$  cm. ,  $b = 15$  cm. ,  $m(\angle C) = 106^\circ$  , then its perimeter  $\approx \dots\dots\dots$  cm.

- (a) 44 (b) 42 (c) 34 (d) 28

- (12) The range of the function  $f : f(x) = |x|$  is .....
- (a)  $\mathbb{R}^+$  (b)  $\mathbb{R}^-$  (c)  $\mathbb{R}$  (d)  $[0, \infty[$
- (13)  $\lim_{x \rightarrow 16} \frac{\sqrt[4]{x^5 - 32}}{x - 16} = \dots\dots\dots$
- (a) 5 (b)  $\frac{5}{2}$  (c)  $\frac{5}{4}$  (d)  $\frac{5}{8}$
- (14) The solution set of the equation :  $|x| + 2 = 0$  in  $\mathbb{R}$  is .....
- (a)  $\{-3\}$  (b)  $\{3\}$  (c)  $\{-3, 3\}$  (d)  $\emptyset$
- (15)  $\log_b a \times \log_c b \times \log_d c \times \log_a d = \dots\dots\dots$
- (a) zero (b) 1 (c)  $abcd$  (d)  $ad$
- (16)  $\lim_{x \rightarrow \infty} (5 + 3^{\frac{1}{x}}) = \dots\dots\dots$
- (a) 8 (b)  $\infty$  (c) 5 (d) 6
- (17)  $\lim_{x \rightarrow 0} \frac{1 - \cos \theta}{3 - x} = \dots\dots\dots$
- (a)  $\frac{1}{3}$  (b)  $\frac{1}{2}$  (c) 1 (d) zero
- (18) In  $\triangle ABC$ , if  $2 \sin A = 3 \sin B = 4 \sin C$ , then  $a : b : c = \dots\dots\dots$
- (a)  $4 : 6 : 3$  (b)  $6 : 3 : 4$  (c)  $3 : 6 : 4$  (d)  $6 : 4 : 3$
- (19) The solution set of the equation :  $3^x + 3^{2+x} = 90$  in  $\mathbb{R}$  is .....
- (a)  $\{1\}$  (b)  $\{2\}$  (c)  $\{3\}$  (d)  $\{-3\}$
- (20) If  $\log 3 = x$ ,  $\log 4 = y$ , then  $\log 12 = \dots\dots\dots$
- (a)  $x + y$  (b)  $xy$  (c)  $x - y$  (d)  $\log x + \log y$
- (21) If ABC is a triangle in which  $a = 4$  cm.,  $b = 4\sqrt{3}$  cm.,  $c = 8$  cm., then cosine of the smallest angle equals .....
- (a)  $\frac{1}{2}$  (b)  $\frac{\sqrt{3}}{2}$  (c) 1 (d) zero
- (22) If  $\lim_{x \rightarrow \infty} \frac{4ax^n - 4x + 5}{3 - 9x + 8x^2} = 3$ , then  $a + n = \dots\dots\dots$
- (a) 8 (b) -8 (c) 9 (d) 4
- (23) The straight line  $y = 9$  cuts the curve of the function  $f : f(x) = 3^x$  at the point .....
- (a)  $(0, 9)$  (b)  $(-2, 9)$  (c)  $(2, 9)$  (d)  $(1, 9)$
- (24)  $\lim_{x \rightarrow 3} \frac{(x-2)^7 - 1}{x-3} = \dots\dots\dots$
- (a) 7 (b) 14 (c) 2 (d) -2
- (25) The solution set in  $\mathbb{R}$  of :  $\sqrt{x^2 - 6x + 9} < 5$  is .....
- (a)  $]-5, 5[$  (b)  $]-2, 8[$  (c)  $]-8, 2[$  (d)  $]-2, 5[$



(26) In  $\triangle ABC$ , if  $m(\angle B) = 60^\circ$ ,  $m(\angle C) = 30^\circ$ ,  $c = 4$  cm, then  $b = \dots\dots\dots$  cm.

- (a) 4 (b) 8 (c)  $2\sqrt{3}$  (d)  $4\sqrt{3}$

(27) If  $\log_3(2x + 3) = 2$ , then  $x = \dots\dots\dots$

- (a) 3 (b) 2 (c) 9 (d) 4

## Second Essay questions

Answer the following questions :

1 Draw the curve of the function  $f : f(x) = \frac{1}{x-2} + 1$ , then from the graph :

- (1) Discuss the monotonicity of  $f$   
(2) Determine whether  $f$  is even, odd or otherwise.

2 Find :  $\lim_{x \rightarrow 5} \frac{\sqrt{x-1}-2}{x-5}$

## 11 El-Beheira Governorate



Maths Inspection

## First Multiple choice questions

Choose the correct answer from the given ones :

(1) The range of the function  $f(x) = x - 2$  is  $\dots\dots\dots$

- (a)  $\mathbb{R}^+$  (b)  $\mathbb{R}^-$  (c)  $\mathbb{R} - \{2\}$  (d)  $\mathbb{R}$

(2) The point of symmetry of the curve of the function  $f(x) = x^3 + 1$  is  $\dots\dots\dots$

- (a) (1, 0) (b) (-1, 0) (c) (0, 1) (d) (0, -1)

(3) If  $f(x) = 2^x$ , then  $f(3) = \dots\dots\dots$

- (a) 2 (b) 4 (c) 0 (d) 1

(4) The solution set of the inequality :  $|x| \leq 2$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $]-\infty, 2]$  (b)  $]-2, 2]$  (c)  $[-2, 2]$  (d)  $]-2, 2[$

(5) The domain of the function  $f(x) = x - 4$  is  $\dots\dots\dots$

- (a)  $[4, \infty[$  (b)  $]4, \infty[$  (c)  $[-\infty, 3[$  (d)  $\mathbb{R}$

(6) The solution set of the equation :  $x^{\frac{3}{2}} = 8$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\{4\}$  (b)  $\{4, -4\}$  (c)  $\{8\}$  (d)  $\{-8, 8\}$

(7) If  $3^{x+1} = 5^{x+1}$ , then  $7^{x+1} = \dots\dots\dots$

- (a) 0 (b) 1 (c) 2 (d) 3

- (8) If  $f(x) = 3^x$ , then  $f(-1) = \dots\dots\dots$   
 (a)  $-1$  (b)  $1$  (c)  $\frac{1}{3}$  (d)  $-\frac{1}{3}$
- (9) If  $\log 3 = a$ ,  $\log 5 = b$ , then  $\log 15 = \dots\dots\dots$   
 (a)  $ab$  (b)  $\frac{a}{b}$  (c)  $a + b$  (d)  $a - b$
- (10) If  $\log_2 x = 3$ , then  $x = \dots\dots\dots$   
 (a)  $2$  (b)  $3$  (c)  $8$  (d)  $9$
- (11)  $\log_2 3 \times \log_3 4 \times \log_4 5 \times \log_5 8 = \dots\dots\dots$   
 (a)  $1$  (b)  $2$  (c)  $3$  (d)  $4$
- (12) The solution set of the equation :  $\log_2 x \times \log_3 2 = 4$  is  $\dots\dots\dots$   
 (a)  $\{81\}$  (b)  $\{4\}$  (c)  $\{3\}$  (d)  $\{2\}$
- (13) If  $5^x = 17$ , then  $x \approx \dots\dots\dots$  (to the nearest hundredth)  
 (a)  $1.34$  (b)  $1.32$  (c)  $1.76$  (d)  $1.67$
- (14)  $\lim_{x \rightarrow 0} \frac{x^5 - 1}{x + 1} = \dots\dots\dots$   
 (a)  $1$  (b)  $-1$  (c)  $-2$  (d)  $5$
- (15)  $\lim_{x \rightarrow \infty} (3 + 5x^2 + 3x) \dots\dots\dots$   
 (a) not exist. (b)  $5$  (c)  $\infty$  (d)  $11$
- (16)  $\lim_{x \rightarrow 0} (3) = \dots\dots\dots$   
 (a)  $0$  (b)  $1$  (c)  $2$  (d)  $3$
- (17)  $\lim_{x \rightarrow \infty} \frac{3x^2 + 4}{x^2 + 5} = \dots\dots\dots$   
 (a)  $3$  (b)  $4$  (c)  $5$  (d)  $1$
- (18) If  $\lim_{x \rightarrow 2} \frac{a}{x + 1} = 3$ , then  $a = \dots\dots\dots$   
 (a)  $6$  (b)  $8$  (c)  $9$  (d)  $12$
- (19)  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^2 - 4} = \dots\dots\dots$   
 (a)  $20$  (b)  $40$  (c)  $60$  (d)  $80$
- (20)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} = \dots\dots\dots$   
 (a)  $4$  (b)  $2$  (c)  $0$  (d)  $8$
- (21)  $\lim_{x \rightarrow 0} \frac{\sqrt{x+4} - 2}{x} = \dots\dots\dots$   
 (a)  $0$  (b)  $1$  (c)  $\frac{1}{4}$  (d)  $4$

- (22) In  $\Delta ABC$  if  $m(\angle A) = 30^\circ$  and  $a = 6$  cm. , then  $\frac{b}{\sin B} = \dots\dots\dots$   
 (a) 3 (b) 6 (c) 8 (d) 12
- (23) In  $\Delta ABC$  if  $2 \sin A = 3 \sin B = 4 \sin C$  , then  $a : b : c = \dots\dots\dots$   
 (a) 2 : 3 : 4 (b) 4 : 3 : 2 (c) 3 : 4 : 6 (d) 6 : 4 : 3
- (24) The length of the diameter of the circumcircle of the triangle ABC in which  $b = 12$  cm. and  $m(\angle B) = 90^\circ$  is  $\dots\dots\dots$  cm.  
 (a) 6 (b) 40 (c) 20 (d) 12
- (25) In  $\Delta ABC$  ,  $a : b : c = 3 : 7 : 5$  , then the measure of the greatest angle in the triangle ABC is  $\dots\dots\dots^\circ$   
 (a) 60 (b) 30 (c) 90 (d) 120
- (26) In  $\Delta ABC$  :  $a = 4$  cm. ,  $b = 7$  cm. and  $m(\angle C) = 120^\circ$  , then the area of the triangle =  $\dots\dots\dots$   
 (a) 14 (b)  $7\sqrt{3}$  (c) 28 (d)  $7\sqrt{2}$
- (27) In  $\Delta ABC$  :  $a = 10$  cm. ,  $b = 10$  cm. and  $m(\angle C) = 120^\circ$  , then  $c = \dots\dots\dots$  cm.  
 (a) 12 (b) 14 (c)  $10\sqrt{3}$  (d) 7

**Second**

**Essay questions**

**Answer the following questions :**

**1** Find the solution set in  $\mathbb{R}$  of the equation :  $|2x - 3| = 1$

**2** Find :  $\lim_{x \rightarrow -3} \frac{(x+5)^4 - 16}{x+3}$

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**El-Menia Governorate**



**Mattay Educational Directorate**

**First**

**Multiple choice questions**

**Choose the correct answer from the given ones :**

- (1) The domain of the function  $f : f(x) = 7$  is  $\dots\dots\dots$   
 (a)  $\{7\}$  (b)  $\mathbb{R}$  (c)  $\mathbb{R} - \{7\}$  (d)  $\mathbb{R} - \{0\}$
- (2)  $f(x) = x + x^3 = \dots\dots\dots$   
 (a) even. (b) odd.  
 (c) neither even nor odd. (d) anything else.



- (3) Symmetric point  $f(x) = x^3 - 1$  is .....
- (a) (0, 0) (b) (1, 0) (c) (0, 1) (d) (0, -1)
- (4) Solve the equation :  $|x + 2| + 1 = 0$  is .....
- (a)  $\mathbb{R}$  (b)  $\{3\}$  (c)  $\{-1\}$  (d)  $\emptyset$
- (5) Solve the equality :  $|x| < 2$  is .....
- (a)  $\emptyset$  (b)  $\mathbb{R} - [-2, 2]$  (c)  $] -2, 2[$  (d)  $[-2, 2]$
- (6)  $2^{x+1} = 8$ , then  $x =$  .....
- (a) 8 (b) 2 (c) 3 (d) 4
- (7)  $\lim_{x \rightarrow 1} (7x + 3) =$  .....
- (a) 7 (b) 3 (c) 10 (d) 1
- (8) If the curve of function  $f : f(x) = 5^x$ , then  $f(3) + f(2) =$  .....
- (a) 125 (b) 25 (c) 150 (d) 100
- (9) If  $\triangle ABC$ , in which  $m(\angle A) = 60^\circ$ ,  $m(\angle C) = 40^\circ$ ,  $c = 8.4$  cm., then  $a \approx$  .....
- (a) 5.3 (b) 11.3 (c) 22.6 (d) 12
- (10) If  $\triangle ABC$ , which  $b = 2r \times$  .....
- (a)  $\sin A$  (b)  $\sin B$  (c)  $\cos B$  (d)  $\sin C$
- (11) In  $\triangle ABC$ , if  $2 \sin A = 3 \sin B = 4 \sin C$ , then  $a : b : c =$  .....
- (a) 2 : 3 : 4 (b) 4 : 3 : 2 (c) 3 : 2 : 4 (d) 6 : 4 : 3
- (12) In  $\triangle ABC$  which  $a = b = 5$  cm.,  $c = 6$  cm., then  $\cos A =$  .....
- (a) 0.4 (b) 0.6 (c) 0.8 (d) 0.2
- (13)  $\log x - \log 3 = \log 9$ , then  $x =$  .....
- (a) 3 (b) 4 (c) 9 (d) 27
- (14)  $\log 2 = x$ ,  $\log 3 = y$ , then  $\log 6 =$  .....
- (a)  $x + y$  (b)  $xy$  (c)  $x - y$  (d)  $\log x + \log y$
- (15)  $\lim_{x \rightarrow \infty} (5x^{70} + 8x^{30} + 4) =$  .....
- (a) 0 (b) 4 (c) 19 (d)  $\infty$
- (16)  $\log_3 2 = A$ ,  $\log_5 3 = B$ , then  $A \times B =$  .....
- (a)  $\log_5 2$  (b)  $\log_2 5$  (c)  $\log_3 10$  (d)  $\log 5$
- (17)  $\lim_{x \rightarrow 4} (2x + \sqrt{x})$  .....
- (a) 4 (b) 6 (c) 8 (d) 10

(18)  $\sqrt{5} \times \sqrt{2} = \sqrt[6]{x}$ , then  $x = \dots\dots\dots$

- (a) 500 (b) 108 (c) 72 (d) 1000

(19) If  $\frac{3^x + 2^x + 1}{5^x + 10^x + 15^x} = \frac{1}{25}$ , then  $x = \dots\dots\dots$

- (a) 1 (b) 2 (c) -1 (d) -2

(20) Measure of greatest angle in the triangle whose sides length 7 cm. , 5 cm. , 3 cm. =  $\dots\dots\dots$

- (a)  $120^\circ$  (b)  $150^\circ$  (c)  $60^\circ$  (d)  $30^\circ$

(21) Length of diameter in the circumcircle of the triangle ABC which  $a = 8 \sin A$  is  $\dots\dots\dots$  unit.

- (a) 4 (b) 5 (c) 8 (d)  $8 \sin A$

(22) The solution set of the equation :  $4^x + 2^{x+1} = 8$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\{1\}$  (b)  $\{-1\}$  (c)  $\{-2\}$  (d)  $\emptyset$

(23)  $\lim_{x \rightarrow 5} (3 + x) = \dots\dots\dots$

- (a) 8 (b) 2 (c) 4 (d) -2

(24)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} = \dots\dots\dots$

- (a) 2 (b) -4 (c) 4 (d) undefined.

(25)  $\lim_{x \rightarrow 3} \frac{\sqrt{x+1} - 2}{x - 3} = \dots\dots\dots$

- (a)  $\frac{1}{4}$  (b)  $\frac{1}{8}$  (c) 12 (d) 3

(26)  $\lim_{x \rightarrow \infty} \frac{9x + 5}{3x - 7} = \dots\dots\dots$

- (a) 3 (b) 6 (c) 9 (d)  $\infty$

(27)  $\lim_{x \rightarrow 1} \frac{x^3 - x^2}{x^3 + 1} = \dots\dots\dots$

- (a) 0 (b) -1 (c) not exist. (d)  $\frac{1}{3}$

## Second

## Essay questions

Answer the following questions :

- 1 Represent the function  $f$  graphically , then show the range and determine its type whether it is even , odd or otherwise where :  $f(x) = (x - 2)^3 + 1$

- 2 Find :  $\lim_{x \rightarrow 3} \frac{x^5 - 243}{x - 3}$

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Assiut Governorate



Kousya Directorate

First

Multiple choice questions

Choose the correct answer from the given ones :

(1) The domain of the function  $f : f(x) = \frac{2x+1}{x-2}$  is .....

- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \left\{-\frac{1}{2}\right\}$  (c)  $\mathbb{R} - \left\{-\frac{1}{2}, 2\right\}$  (d)  $\mathbb{R} - \{2\}$

(2) If  $x^{\frac{3}{2}} = 64$ , then  $x =$  .....

- (a) 512 (b) 16 (c) 4 (d) 2

(3) The type of the function  $f : f(x) = \frac{\sin x}{x}$  is .....

- (a) even. (b) odd.  
(c) neither even nor odd. (d) linear.

(4)  $\lim_{x \rightarrow 0} (2x^2 + 3) =$  .....

- (a) 3 (b) 2 (c) 7 (d) 5

(5) The range of the function  $f : f(x) = |x|$  is .....

- (a)  $[0, \infty[$  (b)  $]0, \infty[$  (c)  $] - \infty, 0]$  (d)  $] - \infty, 0[$

(6)  $\lim_{x \rightarrow 0} \frac{x^2 - x}{x} =$  .....

- (a) zero (b) 1 (c) -1 (d) does not exit.

(7) The vertex point of the curve of the function  $f : f(x) = |x + 3| - 2$  is .....

- (a) (3, 2) (b) (-3, -2) (c) (-3, 2) (d) (3, -2)

(8) The side length of an equilateral triangle is 9 cm., then the area of its circumcircle equals .....  $\text{cm}^2$ 

- (a)  $9\pi$  (b)  $27\pi$  (c)  $81\pi$  (d)  $72\pi$

(9) The point of symmetry of the curve of the function  $f : f(x) = \frac{1}{x-3} + 4$  is .....

- (a) (3, -4) (b) (-3, -4) (c) (3, 4) (d) (-3, 4)

(10)  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2} =$  .....

- (a) 1 (b) 12 (c) 0 (d) 3

(11) The solution set of the inequality  $|2x + 3| \leq 1$  is .....

- (a)  $\emptyset$  (b)  $[-2, -1]$  (c)  $] -2, -1[$  (d)  $\mathbb{R}$



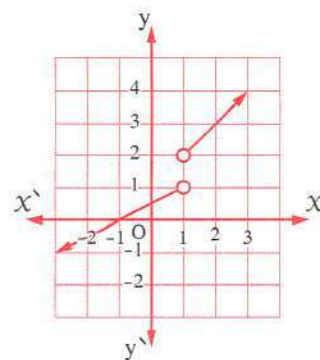
- (12)  $\lim_{x \rightarrow \infty} \frac{\sqrt[3]{64x^3 + 7x - 2}}{3x + 2} = \dots\dots\dots$   
 (a) 4 (b) 3 (c)  $\frac{2}{3}$  (d)  $\frac{4}{3}$
- (13) The solution set of the equation :  $|x - 2| = 3$  is  $\dots\dots\dots$   
 (a)  $\{2, 3\}$  (b)  $\{-1, 5\}$  (c)  $]-1, 5[$  (d)  $\{5, -5\}$
- (14) In  $\triangle ABC$ , if  $a = 5$  cm. ,  $b = 7$  cm. and  $c = 8$  cm. , then  $m(\angle B) = \dots\dots\dots$   
 (a)  $90^\circ$  (b)  $80^\circ$  (c)  $70^\circ$  (d)  $60^\circ$
- (15) If  $f(x - 1) = 2^{x+1}$ , then  $f(x) = \dots\dots\dots$   
 (a)  $2^x$  (b)  $2^{x-1}$  (c)  $2^{x+2}$  (d)  $2^{x-2}$
- (16)  $\lim_{x \rightarrow a} \frac{x^n - a^n}{x^m - a^m} = \dots\dots\dots$   
 (a)  $\frac{m}{n}$  (b)  $\frac{m}{n} (a)^{m-n}$  (c)  $\frac{n}{m} (a)^{m-n}$  (d)  $\frac{n}{m} (a)^{n-m}$
- (17) The exponential function of base  $a$  is increasing if  $\dots\dots\dots$   
 (a)  $a > 0$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = 1$
- (18) In triangle ABC :  $m(\angle A) = 45^\circ$ , the length of the radius of its circumcircle = 6 cm. , then  $a = \dots\dots\dots$   
 (a) 13 (b)  $6\sqrt{2}$  (c) 12 (d)  $\sqrt{2}$
- (19) If  $5^{x-3} = 4^{x-3}$ , then  $x = \dots\dots\dots$   
 (a) 4 (b) 3 (c) 1 (d) zero
- (20) In  $\triangle LMN$ ,  $\frac{\ell}{\sin L} = \dots\dots\dots$   
 (a)  $\frac{m}{\sin N}$  (b)  $\frac{n}{\sin N}$  (c)  $\frac{m}{\sin L}$  (d)  $3r$
- (21) If  $\log_3(2x + 3) = 2$ , then  $x = \dots\dots\dots$   
 (a) 3 (b) 2 (c) 9 (d) 4
- (22)  $\lim_{x \rightarrow 5} \frac{x^2 - 25}{x - 5} = \dots\dots\dots$   
 (a) 10 (b) 2 (c) 5 (d) 4
- (23) If  $\log_2 x + \log_2 x^2 = 6$ , then  $x = \dots\dots\dots$   
 (a) 2 (b) 4 (c) 6 (d) 216
- (24) In  $\triangle ABC$ ,  $m(\angle A) = 30^\circ$ ,  $b = 15\sqrt{3}$ ,  $m(\angle B) = 60^\circ$ , then  $a = \dots\dots\dots$   
 (a) 30 (b) 45 (c) 15 (d) 60
- (25) In  $\triangle ABC$  :  $a^2 + b^2 - c^2 = \dots\dots\dots$   
 (a)  $\cos A$  (b)  $ab \cos C$  (c)  $\cos C$  (d)  $2ab \cos C$

**(26) In the opposite figure :**

The graph of function  $f$

, then  $\lim_{x \rightarrow 1} f(x) = \dots\dots\dots$

- (a) 2
- (b) 3
- (c) 1
- (d) not exist.



**(27)** By solving the triangle ABC in which  $a = 5$  cm. ,  $b = 7$  cm. ,  $m(\angle C) = 65^\circ$   
 , then  $c \approx \dots\dots\dots$  cm.

- (a) 4.4
- (b) 2.1
- (c) 6.7
- (d) 8.2

**Second Essay questions**

**Answer the following questions :**

**1** Draw the graph of the function  $f : f(x) = \begin{cases} x^2 & , x < 0 \\ x & , x \geq 0 \end{cases}$  and deduce from the graph its range and its type of being odd , even or otherwise.

**2** Find the S.S. of the equation :  $\log_x 81 = 4$

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**Qena Governorate**



**Mathematics Inspection**

**First Multiple choice questions**

**Choose the correct answer from the given ones :**

**(1)** Solution set of inequality :  $|x + 2| \leq 3$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\mathbb{R}$
- (b)  $\emptyset$
- (c)  $[-5, 1]$
- (d)  $] -5, 1[$

**(2)** In  $\triangle ABC$  if  $a = 4$  cm. ,  $m(\angle A) = 30^\circ$  , then length radius of circumcircle  $\triangle ABC = \dots\dots\dots$  cm.

- (a) 4
- (b) 2
- (c) 12
- (d) 24

- (3) Domain of function  $f : f(x) = \sqrt[3]{x-2}$  is .....
- (a)  $[-2, \infty[$  (b)  $[-2, 2]$  (c)  $]-\infty, 2]$  (d)  $\mathbb{R}$
- (4)  $\lim_{x \rightarrow \infty} \left( \frac{x}{2-x^2} \right) = \dots\dots\dots$
- (a) 0 (b)  $\frac{1}{2}$  (c) 2 (d) -1
- (5) If  $\log 2 = x$ ,  $\log 3 = y$ , then  $\log 6 = \dots\dots\dots$
- (a)  $xy$  (b)  $x \div y$  (c)  $x + y$  (d)  $x^y$
- (6)  $\lim_{x \rightarrow -3} \left( \frac{x^2 + 4x + 3}{x^2 - 9} \right) = \dots\dots\dots$
- (a) 2 (b) 0 (c)  $-\frac{1}{3}$  (d)  $\frac{1}{3}$
- (7) In  $\Delta ABC$  if  $a = 5$  cm.,  $m(\angle B) = 120^\circ$  and surface area of  $\Delta ABC = 10\sqrt{3}$  cm<sup>2</sup>, then  $c = \dots\dots\dots$  cm.
- (a) 5 (b) 8 (c) 7.2 (d) 10
- (8) If  $5^x = 2$ , then  $5^{x+2} = \dots\dots\dots$
- (a) 5 (b) 2 (c) 25 (d) 50
- (9) In  $\Delta XYZ$  if  $x = 5$  cm.,  $y = 7$  cm.,  $z = 8$  cm., then  $m(\angle Y) = \dots\dots\dots$
- (a)  $30^\circ$  (b)  $60^\circ$  (c)  $45^\circ$  (d)  $120^\circ$
- (10) Solution set of equation :  $x^{\frac{7}{2}} = 128$  in  $\mathbb{R}$  is .....
- (a)  $\{4\}$  (b)  $\{7\}$  (c)  $\{2\}$  (d)  $\{\pm 4\}$
- (11)  $\lim_{x \rightarrow 0} \left( \frac{x^2 + 2x}{x} \right) = \dots\dots\dots$
- (a) -2 (b) 2 (c) 0 (d) 1
- (12) Point vertex curve of function  $f : f(x) = (x+2)^2 + 1$  is .....
- (a)  $(-2, 1)$  (b)  $(2, 1)$  (c)  $(-2, -1)$  (d)  $(2, -1)$
- (13)  $\log_2 6 \times \log_6 2 = \dots\dots\dots$
- (a) 0 (b) 2 (c) 1 (d) 3
- (14) In  $\Delta ABC$  if :  $3 \sin A = 6 \sin B = 4 \sin C$ , then  $a : b : c = \dots\dots\dots$
- (a)  $3 : 4 : 6$  (b)  $2 : 3 : 4$  (c)  $3 : 6 : 4$  (d)  $4 : 2 : 3$
- (15) The curve of function  $f : f(x) = \frac{1}{x+1}$  symmetry around point .....
- (a)  $(-1, 0)$  (b)  $(0, 1)$  (c)  $(0, 0)$  (d)  $(1, 0)$
- (16)  $\lim_{x \rightarrow 1} \frac{x^4 - 1}{x^2 - 1} = \dots\dots\dots$
- (a) 6 (b) 3 (c) 2 (d) 1



(17) If  $\log x \in ]0, 1[$ , then  $x \in$  .....

- (a)  $]1, 2[$  (b)  $]0, 1[$  (c)  $]1, 10[$  (d)  $]1, \infty[$

(18)  $\lim_{x \rightarrow 1} (10) =$  .....

- (a) 1 (b) 0 (c) -10 (d) 10

(19) In  $\Delta DEF$  if,  $m(\angle E) = 35^\circ$ ,  $m(\angle F) = 40^\circ$ ,  $EF = 12$  cm., then  $ED \approx$  ..... to nearest centimeter.

- (a) 2 (b) 3 (c) 8 (d)  $\sqrt{3}$

(20) In  $\Delta ABC$  if  $AB = 3$  cm.,  $BC = 5$  cm.,  $m(\angle B) = 120^\circ$ , then  $AC =$  ..... cm.

- (a) 8 (b) 7 (c) 9 (d) 4

(21) Which of following functions represent an even function .....

- (a)  $f(x) = x^4 + 1$  (b)  $f(x) = x^3 + 1$  (c)  $f(x) = x \cos x$  (d)  $f(x) = x^2 \sin x$

(22)  $\lim_{n \rightarrow \infty} \frac{5x^{-3} + x^{-1} + 5}{2x^{-3} + 2x^{-1} + 7} =$  .....

- (a)  $\frac{5}{7}$  (b)  $\frac{7}{5}$  (c)  $\frac{1}{2}$  (d)  $\frac{5}{2}$

(23) Function  $f$  where  $f(x) = a^x$  is increase on its domain when .....

- (a)  $a = 1$  (b)  $a > 1$  (c)  $a = -1$  (d)  $0 < a < 1$

(24)  $\lim_{x \rightarrow 2} \frac{2x^2 - x - k}{x^2 - x - 2} = \frac{7}{3}$ , then  $k =$  .....

- (a) 2 (b) 7 (c) -6 (d) 6

(25)  $\lim_{x \rightarrow 0} \frac{(x+2)^5 - 32}{x} =$  .....

- (a) 4 (b) 16 (c) 32 (d) 80

(26) If  $\log_4(x+1) = 1$ , then  $x =$  .....

- (a) 3 (b) 4 (c) 2 (d) 1

(27) If  $f(x) = 3^x$ , then solution set of equation :  $f(x+1) - f(x-1) = 24$  is .....

- (a)  $\{2\}$  (b)  $\{3\}$  (c)  $\{8\}$  (d)  $\{0\}$

## Second

## Essay questions

Answer the following questions :

1 Represent graphically function  $f : f(x) = (x-1)^3 + 2$  from drawing determine the range of the function and discuss its monotonicity.

2 Find value of :  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$

# كيفية طباعة صفحات معينة من ملف معين مثلا ازاي نطبع الصفحات من صفحة 4 الى صفحة 9





حمل الآن

مجاناً وحصرياً

# امتحانات رقم (2)

## الترم الاول







## First

## Multiple choice questions

Choose the correct answer from the given ones :

- (1) If  $f$  is an odd function ,  $a \in$  the domain of  $f$  , then  $f(a) + f(-a) = \dots\dots\dots$   
 (a) 2 (a) (b)  $2(-a)$  (c) zero (d) (a)
- (2) If  $f(x) = \sqrt{x+4}$  ,  $g(x) = \sqrt{6-x}$  , then  $(f+g)(5) = \dots\dots\dots$   
 (a) undefined (b) zero (c) 5 (d) 4
- (3) The domain of the function  $f : f(x) = \begin{cases} x+3 & , x > 3 \\ 6 & , x < 3 \end{cases}$  is  $\dots\dots\dots$   
 (a)  $\{3\}$  (b)  $\mathbb{R} - \{3\}$  (c)  $[3, \infty[$  (d)  $\mathbb{R}$
- (4) If  $y = f(x)$  is a real function , then its image by translation 3 units right is  $g(x) = \dots\dots\dots$   
 (a)  $f(x-3)$  (b)  $f(x+3)$  (c)  $f(x)+3$  (d)  $f(x)-3$
- (5) The solution set of the equation :  $\log_5 y = 2$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\{25\}$  (b)  $\{25, 625\}$  (c)  $\{\frac{1}{25}, 625\}$  (d)  $\{125, 625\}$
- (6) If  $\log_2 x = 3$  , then  $\log_x 2 = \dots\dots\dots$   
 (a) 2 (b)  $\frac{1}{3}$  (c) 8 (d) 9
- (7) If  $5^{x+1} = 7^{x+1}$  , then  $3^{x+1} = \dots\dots\dots$   
 (a) zero (b) 3 (c) 2 (d) 1
- (8) Solution set of the equation :  $\log_x (x+6) = 2$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\{3, -2\}$  (b)  $\{3\}$  (c)  $\{3, 1\}$  (d)  $\{6, 1\}$
- (9) The domain of the function :  $f(x) = \frac{1}{x^2-4}$  is  $\dots\dots\dots$   
 (a)  $\{2, -2\}$  (b)  $[2, -2]$  (c)  $\mathbb{R} - [2, -2]$  (d)  $\mathbb{R} - \{2, -2\}$
- (10) The solution set of the inequality :  $|x-3| < 6$  is  $\dots\dots\dots$   
 (a)  $] -1, 7[$  (b)  $\mathbb{R} - [-3, 9]$  (c)  $\mathbb{R} - [-1, 7]$  (d)  $] -3, 9[$
- (11) If  $2^{x+1} = 8$  , then  $x = \dots\dots\dots$   
 (a) 3 (b) 2 (c) -3 (d) -2
- (12) The function  $f$  where  $f(x) = a^x$  is decreasing on its domain if  $\dots\dots\dots$   
 (a)  $a = 1$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = -1$

- (13) If  $3^a = 4$ , then  $9^a = \dots\dots\dots$   
 (a) 7 (b) 12 (c) 16 (d) 25
- (14) The equation of axis of symmetry of the curve of the function  $f : f(x) = |x + 3| - 2$  is  $\dots\dots\dots$   
 (a)  $x = -3$  (b)  $x = -2$  (c)  $y = -3$  (d)  $y = -2$
- (15)  $\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - 1}{x} = \dots\dots\dots$   
 (a)  $\frac{1}{2}$  (b) 2 (c) zero (d) 1
- (16)  $\lim_{x \rightarrow \infty} x^{-5} = \dots\dots\dots$   
 (a)  $\infty$  (b)  $-5$  (c) 5 (d) zero
- (17)  $\lim_{x \rightarrow 1} \frac{x^2 - x}{x^3 - 1} = \dots\dots\dots$   
 (a) zero (b)  $-\frac{1}{3}$  (c)  $\frac{1}{3}$  (d) does not exist.
- (18)  $\lim_{x \rightarrow \infty} \frac{x^{-3} + 3x^{-2} + 1}{x^{-2} + x^{-1} + 3} = \dots\dots\dots$   
 (a) 2 (b) 1 (c) 3 (d)  $\frac{1}{3}$
- (19)  $\lim_{x \rightarrow 3} \frac{(x-6)^2 - 9}{x^2 - 9} = \dots\dots\dots$   
 (a)  $-1$  (b) 3 (c) 1 (d) 2
- (20)  $\lim_{x \rightarrow 1} \frac{x^2 + 5x - 6}{x^2 - 1} = \dots\dots\dots$   
 (a) 1 (b) 5 (c) 6 (d) 3.5
- (21) In  $\triangle ABC$ ,  $b^2 + c^2 - a^2 = 2bc \times \dots\dots\dots$   
 (a)  $\cos A$  (b)  $\sin A$  (c)  $\cos C$  (d)  $\cos B$
- (22) In triangle ABC If:  $\frac{a}{\sin A} = 6$  cm., then the circumference of the circumcircle of triangle =  $\dots\dots\dots$   
 (a)  $12\pi$  (b)  $6\pi$  (c)  $5\pi$  (d)  $9\pi$
- (23) In  $\triangle ABC$ ,  $c = 7$  cm.,  $m(\angle A) = 70^\circ$ ,  $m(\angle B) = 40^\circ$ , then  $b \approx \dots\dots\dots$  cm.  
 (a) 3.7 (b) 4.8 (c) 8.4 (d) 7.3
- (24) If ABC is a triangle in which  $a = 4$  cm.,  $b = 4\sqrt{3}$  cm.,  $c = 8$  cm., then the measure of the smallest angle equals  $\dots\dots\dots$   
 (a)  $60^\circ$  (b)  $30^\circ$  (c)  $90^\circ$  (d)  $120^\circ$
- (25) The diameter length of the circle inscribed in an equilateral triangle whose side length is  $4\sqrt{3}$  cm. equals  $\dots\dots\dots$  cm.  
 (a) 8 (b)  $4\sqrt{3}$  (c) 4 (d)  $2\sqrt{3}$

- (26) In  $\Delta ABC$  , if  $2 \sin A = 3 \sin B = 4 \sin C$  , then  $a : b : c = \dots\dots\dots$   
 (a)  $6 : 4 : 3$  (b)  $4 : 3 : 2$  (c)  $3 : 4 : 6$  (d)  $2 : 3 : 4$
- (27) In  $\Delta ABC$  , if  $m(\angle B) = 60^\circ$  ,  $m(\angle C) = 30^\circ$  ,  $c = 4$  cm. , then  $b = \dots\dots\dots$  cm.  
 (a) 4 (b) 8 (c)  $2\sqrt{3}$  (d)  $4\sqrt{3}$
- (28) ABCD is a parallelogram in which :  $AB = 9$  cm. ,  $BC = 13$  cm. ,  $AC = 20$  cm. , then the length of BD equals  $\dots\dots\dots$  cm.  
 (a) 10 (b) 5 (c) 18.5 (d) 20

## Second Essay questions

Answer the following questions :

- 1 Find :  $\lim_{x \rightarrow 1} \frac{x^3 - 2x + 1}{x^2 + x - 2}$
- 2 Write the steps to find :  $\lim_{x \rightarrow 3} \frac{\sqrt{x+1} - 2}{x-3}$
- 3 If  $f(x) = x^2 - 1$  graph the function showing its domain , range , and monotony
- 4 If  $f(x) = 7^x$  , then find the value of  $x$  satisfying  $f(2x-1) + f(2x+1) = \frac{50}{49}$

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## First Multiple choice questions

Choose the correct answer from the given ones :

- (1) In  $\Delta ABC$  , if  $m(\angle B) = 60^\circ$  ,  $m(\angle C) = 30^\circ$  and  $c = 4$  cm. , then  $a = \dots\dots\dots$  cm.  
 (a) 2 (b) 4 (c) 8 (d)  $4\sqrt{3}$
- (2) The point of symmetry of the function  $f : f(x) = \frac{2x-1}{x}$  is  $\dots\dots\dots$   
 (a)  $(2, 0)$  (b)  $(0, 2)$  (c)  $(-2, 0)$  (d)  $(2, -1)$
- (3) The solution set of  $|2x-3| \leq 3$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $[-3, 3]$  (b)  $]-3, 3[$  (c)  $[0, 6]$  (d)  $[0, 3]$
- (4)  $\lim_{h \rightarrow 0} \frac{(x+h)^7 - x^7}{h} = \dots\dots\dots$   
 (a)  $7x^6$  (b)  $6x^7$  (c)  $7h^6$  (d)  $7h^7$
- (5) In  $\Delta ABC$  , if  $b^2 = c^2 + a^2 - ac$  , then  $m(\angle B) = \dots\dots\dots$   
 (a)  $30^\circ$  (b)  $45^\circ$  (c)  $60^\circ$  (d)  $120^\circ$



(6)  $5^{x-3} = 4^{3-x}$ , then  $x = \dots\dots\dots$

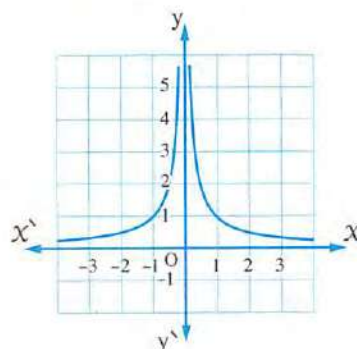
- (a) 3 (b) 4 (c) 5 (d) 0

(7) The range of the function  $f : f(x) = \begin{cases} 1 & , x \leq 0 \\ 0 & , x > 0 \end{cases}$

- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{0, 1\}$  (c)  $\{0, 1\}$  (d)  $\mathbb{R} - [0, 1]$

(8) The opposite figure represents  $f : f(x) = \dots\dots\dots$

- (a)  $\frac{1}{x}$   
(b)  $-\frac{1}{x}$   
(c)  $\frac{1}{|x|}$   
(d)  $\frac{1}{x} + 5$



(9) In  $\triangle XYZ$ ,  $x = 5$  cm. ,  $y = 7$  cm. ,  $m(\angle Z) = 65^\circ$ , then  $z \approx \dots\dots\dots$  cm.

- (a) 5.7 (b) 6.7 (c) 7.5 (d) 44

(10) If  $\log_x 2 = 3$ , then  $\log_2 x = \dots\dots\dots$

- (a)  $x$  (b) 1 (c)  $\frac{1}{3}$  (d) 3

(11) The solution set of  $|x| + 3 = 1$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\{2\}$  (b)  $\{-2\}$  (c)  $\{-2, 2\}$  (d)  $\emptyset$

(12)  $\lim_{y \rightarrow 2} \frac{y^5 - 32}{y^2 - 4} = \dots\dots\dots$

- (a) 20 (b) 40 (c) 60 (d) 80

(13) If the curve of the function  $f : f(x) = \log_4 (1 - ax)$  passes through the point  $(\frac{1}{8}, -\frac{1}{2})$ , then  $a = \dots\dots\dots$

- (a) 1 (b) 2 (c) 3 (d) 4

(14) The domain of the function  $f : f(x) = \sqrt{9-x}$  is  $\dots\dots\dots$

- (a)  $[9, \infty[$  (b)  $]-\infty, 9]$  (c)  $[-9, \infty[$  (d)  $\mathbb{R}$

(15) In  $\triangle XYZ$ ,  $\sin X = 2 \sin Z$  and  $YZ = 6$  cm. , then  $XY = \dots\dots\dots$

- (a) 3 (b) 6 (c)  $3\sqrt{6}$  (d) 12

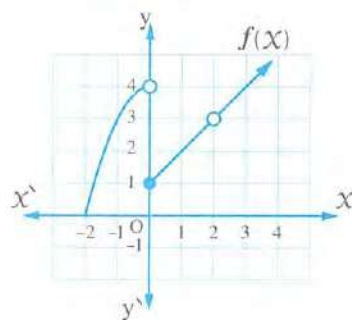
(16)  $\lim_{x \rightarrow \infty} \frac{6x^2 - 3x + 6}{1 + 4x + 2x^2} = \dots\dots\dots$

- (a) 0 (b) 3 (c) 4 (d) 6

(17) If  $f$  is an odd function and  $a \in$  its domain, then  $f(a) + f(-a) = \dots\dots\dots$

- (a) 0 (b) 2 (c)  $2f(a)$  (d)  $f(a)$

- (18)  $f(x) = 2^{1-x}$ , then  $f(-1) = \dots\dots\dots$   
 (a) 0 (b) 1 (c) 2 (d) 4
- (19)  $\lim_{x \rightarrow 3} \frac{\sqrt{x+1}-2}{x-3} = \dots\dots\dots$   
 (a) 0 (b)  $\frac{1}{4}$  (c)  $\frac{2}{3}$  (d) does not exist.
- (20)  $f(x) = 3^{x+1}$ , then  $f(x+1) \times f(-x) = \dots\dots\dots$   
 (a) 1 (b) 3 (c) 9 (d) 27
- (21) The side length of an equilateral triangle is 9 cm., then the area of its circumcircle equals  $\dots\dots\dots \text{cm}^2$   
 (a)  $9\pi$  (b)  $27\pi$  (c)  $81\pi$  (d)  $72\pi$
- (22) The opposite figure represents the curve of the function  $f$ , then  $\lim_{x \rightarrow 0} f(x) = \dots\dots\dots$   
 (a) 1  
 (b) 4  
 (c) 0  
 (d) does not exist.
- (23) If  $\lim_{x \rightarrow 2} \frac{ax}{3} = 6$ , then  $a = \dots\dots\dots$   
 (a) 1 (b) 4 (c) 6 (d) 9
- (24) In  $\triangle ABC$ , if  $b = c$ , then  $\cos C = \dots\dots\dots$   
 (a)  $c$  (b)  $\frac{a}{b}$  (c)  $\frac{a}{2b}$  (d)  $\frac{b}{2a}$
- (25) If  $\log_2 x = 5$ , then the exponential form of it is  $\dots\dots\dots$   
 (a)  $x^2 = 5$  (b)  $2^5 = x$  (c)  $5^2 = x$  (d)  $x^5 = 2$
- (26) In  $\triangle ABC$ , if  $m(\angle A) = 110^\circ$ ,  $m(\angle B) = 34^\circ$ ,  $c = 19 \text{ cm.}$ , then  $b$  to nearest cm. =  $\dots\dots\dots \text{cm.}$   
 (a) 14 (b) 18 (c) 19.8 (d) 30.4
- (27)  $\lim_{x \rightarrow \infty} \frac{6}{3x^2} + \frac{8x}{2+x} = \dots\dots\dots$   
 (a) 2 (b) 4 (c) 6 (d) 8
- (28) If  $\log 3 = x$  and  $\log 4 = y$ , then  $\log 12 = \dots\dots\dots$   
 (a)  $x - y$  (b)  $x + y$  (c)  $xy$  (d)  $\frac{x}{y}$



## Second Essay questions

Answer the following questions :

1 Find :  $\lim_{x \rightarrow 2} \frac{x^2 - 5x + 6}{x^2 - 4}$

- 2** Graph the function  $f : f(x) = \begin{cases} |x| & , x \leq 0 \\ x^3 & , x > 0 \end{cases}$ , then  
**(1)** deduce its range. **(2)** discuss the monotony.

**3** Find :  $\lim_{x \rightarrow 1} \frac{(x+1)^5 - 32}{x-1}$

**4** Find the solution set of :  $3^{x+2} - 3^{x+1} = 18$  in  $\mathbb{R}$

**3**

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Ain Shams Educational directorate

**First**

**Multiple choice questions**

Choose the correct answer from the given ones :

- (1)** The type of the function  $f : f(x) = \frac{\sin x}{x}$  is .....  
 (a) even. (b) odd.  
 (c) neither even nor odd. (d) linear.
- (2)** The domain of the function  $f : f(x) = \frac{2x+1}{x-2}$  is .....  
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \left\{-\frac{1}{2}\right\}$  (c)  $\mathbb{R} - \left\{-\frac{1}{2}, 2\right\}$  (d)  $\mathbb{R} - \{2\}$
- (3)**  $1 + \log 2 = \dots\dots\dots$   
 (a)  $\log 5$  (b)  $\log 2$  (c)  $\log 20$  (d)  $-\log 5$
- (4)** In  $\Delta XYZ$ ,  $y^2 + z^2 - x^2 = 2yz \times \dots\dots\dots$   
 (a)  $\cos X$  (b)  $\sin Z$  (c)  $\cos Z$  (d)  $\sin X$
- (5)**  $\lim_{x \rightarrow \infty} \frac{3x}{4x+5} = \dots\dots\dots$   
 (a)  $\infty$  (b)  $\frac{3}{4}$  (c)  $\frac{1}{5}$  (d) zero
- (6)** The set of the real roots of the equation  $(x-2)^4 = 16$  equals .....  
 (a)  $\{0\}$  (b)  $\{4\}$  (c)  $\{8\}$  (d)  $\{0, 4\}$
- (7)** The range of the function  $f : f(x) = |x-2|$  is .....  
 (a)  $]-\infty, 2[$  (b)  $[-2, \infty[$  (c)  $[0, \infty[$  (d)  $]2, \infty[$
- (8)** If  $\log x - \log 2 = \log 4$ , then  $x = \dots\dots\dots$   
 (a) 4 (b) 6 (c) 8 (d) 16
- (9)**  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^3 - 2^3} = \dots\dots\dots$   
 (a) 4 (b)  $\frac{5}{3}$  (c) zero (d)  $6\frac{2}{3}$



- (10) In  $\Delta ABC$ ,  $\frac{a}{\sin A} = 6$ , then the length of the diameter of its circumcircle is ..... length units  
 (a) 6 (b) 12 (c) 3 (d) 9
- (11) If  $\sqrt[3]{x^2} = 9$ , then  $x \in$  .....  
 (a)  $\{27\}$  (b)  $\{27, -27\}$  (c)  $\{1\}$  (d)  $\emptyset$
- (12) If  $\log_3 x = 2$ , then  $x =$  .....  
 (a) 3 (b) 5 (c) 8 (d) 9
- (13)  $\lim_{x \rightarrow -1} 3x^2 =$  .....  
 (a) 2 (b) 3 (c) 4 (d) 5
- (14) In  $\Delta ABC$ ,  $\cos(A + B) =$  .....  
 (a)  $\frac{a^2 + b^2 - c^2}{2ab}$  (b)  $\frac{a^2 + c^2 - b^2}{2ab}$  (c)  $\frac{b^2 + c^2 - a^2}{2bc}$  (d)  $\frac{c^2 - a^2 - b^2}{2ab}$
- (15) If  $2^{x+1} = 8$ , then  $x =$  .....  
 (a) 1 (b) 2 (c) 3 (d) 4
- (16) The solution set of the inequality:  $|2x + 3| \leq 1$  in  $\mathbb{R}$  is .....  
 (a)  $\mathbb{R}$  (b)  $]-2, -1[$  (c)  $[-2, -1]$  (d)  $\emptyset$
- (17) The vertex of the curve of the function  $f$  where  $f(x) = (1 + x)^2 - 3$  is .....  
 (a)  $(1, 3)$  (b)  $(1, -3)$  (c)  $(-1, 3)$  (d)  $(-1, -3)$
- (18)  $\lim_{x \rightarrow 4} \frac{(x-3)^2 - 1}{x-4} =$  .....  
 (a) zero (b) 2 (c) 3 (d) 4
- (19)  $\lim_{x \rightarrow \infty} \frac{2x}{\sqrt{9x^2 + 1}} =$  .....  
 (a)  $\frac{2}{9}$  (b) zero (c)  $\frac{2}{3}$  (d)  $\infty$
- (20) If the perimeter of triangle ABC equals 15 cm.,  $m(\angle A) = 82^\circ$ ,  $m(\angle B) = 47^\circ$ , then the length of AB  $\simeq$  ..... cm.  
 (a) 6 (b) 7 (c) 5 (d) 8
- (21) In  $\Delta ABC$ ,  $m(\angle A) = 45^\circ$ , the length of the radius of its circumcircle = 6 cm., then  $a =$  ..... cm.  
 (a) 13 (b)  $6\sqrt{2}$  (c) 12 (d)  $\sqrt{2}$
- (22) If  $y = f(x)$  is a real function, then its image by translation 3 units vertically upwards is  $g(x) =$  .....  
 (a)  $f(x - 3)$  (b)  $f(x + 3)$  (c)  $f(x) + 3$  (d)  $f(x) - 3$

- (23)  $\lim_{x \rightarrow -2} \frac{3x^2 - 12}{x + 2} = \dots\dots\dots$   
 (a) 18 (b) -3 (c) 12 (d) -12
- (24) DEF is a triangle in which  $m(\angle D) = 80^\circ$  and  $m(\angle E) = 60^\circ$ , if  $f = 12$  cm., then  $d = \dots\dots\dots$  cm.  
 (a)  $\frac{12 \sin 80^\circ}{\sin 40^\circ}$  (b)  $\frac{12 \sin 80^\circ}{\sin 60^\circ}$  (c)  $\frac{12 \sin 40^\circ}{\sin 80^\circ}$  (d)  $\frac{12 \cos 80^\circ}{\cos 40^\circ}$
- (25) In  $\triangle ABC$  : If  $\frac{\sin A}{4} = \frac{\sin B}{9} = \frac{\sin C}{7}$ , then the greatest angle in measure is  $\dots\dots\dots$   
 (a)  $\angle A$  (b)  $\angle B$  (c)  $\angle C$  (d) right.
- (26) In  $\triangle XYZ$ ,  $x = 5$  cm. ,  $y = 3$  cm. ,  $m(\angle Z) = 120^\circ$ , then  $z = \dots\dots\dots$  cm.  
 (a) 7 (b) 6 (c)  $3\sqrt{3}$  (d) 4
- (27) The solution set of the equation :  $|x - 2| = 3$  is  $\dots\dots\dots$   
 (a)  $\{2, 3\}$  (b)  $\{-1, 5\}$  (c)  $[-1, 5]$  (d)  $\{5, -5\}$
- (28) If  $3^x = 5$ , then  $x = \dots\dots\dots$   
 (a) 3 (b)  $\log_3 5$  (c)  $\log_5 3$  (d)  $\frac{5}{3}$

## Second

## Essay questions

Answer the following questions :

1 Find the solution set in  $\mathbb{R}$  :  $|x - 3| = |x + 1|$

2 If  $f(x) = 5^x$ , find the value of :  $\frac{f(x+4) - f(x+3)}{f(x+5) - f(x+4)}$

3 Find :  $\lim_{x \rightarrow \infty} \left( \frac{x}{2x+1} + \frac{3x^2}{(x-2)^2} \right)$

4 Find :  $\lim_{x \rightarrow -1} \frac{x+1}{\sqrt{x+5}-2}$

4

Giza Governorate



Awseem Educational Directorate  
Mathematics Inspection

## First

## Multiple choice questions

Choose the correct answer from the given ones :

- (1) The type of the functions  $f : f(x) = x^2$  where  $f : \mathbb{Z}^+ \longrightarrow \mathbb{Z}$  is  $\dots\dots\dots$   
 (a) even. (b) odd.  
 (c) neither even nor odd. (d) constant.

- (2) If  $f : f(x) = 2$ , then the range of the function  $f$  is .....
- (a)  $\mathbb{R}$  (b)  $\mathbb{R}^+$  (c)  $\{2\}$  (d)  $\mathbb{R} - \{2\}$
- (3) The range of the function  $f : f(x) = \frac{1}{x} + 1$  is .....
- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{2\}$  (c)  $\mathbb{R}^+$  (d)  $\mathbb{R} - \{1\}$
- (4) The S.S. of the equation :  $|x - 2| + 1 = 0$  is .....
- (a)  $\mathbb{R}$  (b)  $\emptyset$  (c)  $\{3\}$  (d)  $\{-1\}$
- (5) The axis of symmetry of the function  $f : f(x) = 2 - (x - 1)^2$  is  $x =$  .....
- (a) 1 (b) -1 (c) 2 (d) 3
- (6) If  $5^{x+2} = 125$ , then  $x =$  .....
- (a) 2 (b) 1 (c) 3 (d) 4
- (7) If  $9 \times 3^{2-x} = 81^{-1}$ , then  $x =$  .....
- (a) 6 (b) 7 (c) 8 (d) 9
- (8)  $\left((2)^7 \div (2)^5\right)^{\frac{1}{2}} =$  .....
- (a) 2 (b) -2 (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
- (9) The two curves of the two functions  $f : f(x) = 2^x$ ,  $g : g(x) = 3^x$  will intersect at  $x =$  .....
- (a) 2 (b) 3 (c) zero (d) 5
- (10) If  $\log_x(5x) = 2$ , then  $x \in \{\dots\dots\dots\}$
- (a)  $\{0, 5\}$  (b)  $\{5\}$  (c)  $\{0\}$  (d)  $\{2\}$
- (11)  $\log_8 \log_2 \log_3(x - 4) = \frac{1}{3}$ , then  $x =$  .....
- (a) 8 (b) 48 (c) 90 (d) 85
- (12)  $\log 125 - \log 6 + \log 48 =$  .....
- (a) 3 (b) 6 (c) 7 (d) 8
- (13) If  $\log_2 x + \log_4 x = 3$ , then  $x =$  .....
- (a) 2 (b) 3 (c) 4 (d) 5
- (14) If  $2^x = 7$ , then  $x \simeq$  .....
- (a) 2.25 (b) 2.81 (c) 2.85 (d) 3
- (15)  $\lim_{x \rightarrow 3} \frac{x^3 - 27}{x^2 - 2x - 3} =$  .....
- (a) 6.5 (b) 6.75 (c) 7 (d) 7.5
- (16)  $\lim_{x \rightarrow 2} (10) =$  .....
- (a) 2 (b) 5 (c) 10 (d) 8



- (17)  $\lim_{x \rightarrow 2} \frac{x^4 - k^4}{x - k} = 32$ , then  $k = \dots\dots\dots$   
 (a) zero (b) 1 (c) 2 (d) 3
- (18)  $\lim_{x \rightarrow \infty} (3x^{-5} + 4x^{-2} + 5) = \dots\dots\dots$   
 (a) 5 (b)  $\infty$  (c) 12 (d) zero
- (19)  $\lim_{x \rightarrow \infty} x^{-4} = \dots\dots\dots$   
 (a) zero (b) -4 (c) 4 (d)  $\infty$
- (20) In  $\triangle XYZ$ , the expression  $\frac{x^2 + y^2 - z^2}{2xy} = \dots\dots\dots$   
 (a)  $\cos X$  (b)  $\cos Y$  (c)  $\cos Z$  (d)  $\sin Y$
- (21)  $\lim_{h \rightarrow 0} \frac{(2 + 3h)^5 - 32}{2h} = \dots\dots\dots$   
 (a) 32 (b) 64 (c) 80 (d) 120
- (22) In triangle ABC if  $a^2 = b^2 + c^2 + bc$ , then  $m(\angle A) = \dots\dots\dots^\circ$   
 (a) 120 (b) 60 (c) 45 (d) 30
- (23) In triangle ABC if  $m(\angle C) = 30^\circ$ ,  $AB = 14$  cm., then the circumference of the circle =  $\dots\dots\dots$  cm.  
 (a)  $28\pi$  (b)  $30\pi$  (c) 28 (d)  $335\pi$
- (24) The radius length of the circumcircle of triangle ABC in which  $m(\angle A) = 30^\circ$ ,  $a = 10$  cm. is  $\dots\dots\dots$   
 (a) 5 (b) 10 (c) 20 (d) 40
- (25) If  $r$  is the radius of the circumcircle of triangle XYZ, then  $\frac{2y}{\sin X} = \dots\dots\dots$   
 (a)  $r$  (b)  $2r$  (c)  $4r$  (d)  $3r$
- (26) ABC is a triangle in which  $\cos B = \frac{c}{2a}$ , then the triangle will be  $\dots\dots\dots$   
 (a) scalene. (b) right-angled. (c) isosceles. (d) equilateral.
- (27) In triangle XYZ :  $y^2 + z^2 - x^2 = 2yz \dots\dots\dots$   
 (a)  $\cos X$  (b)  $\sin Z$  (c)  $\cos Z$  (d)  $\sin X$
- (28) In triangle XYZ if :  $2 \sin X = 3 \sin Y = 4 \sin Z$ , then  $X : y : z = \dots\dots\dots$   
 (a)  $2 : 3 : 4$  (b)  $6 : 4 : 3$  (c)  $3 : 4 : 6$  (d)  $4 : 3 : 2$

## Second Essay questions

**Answer the following questions :**

- 1** Draw the graph of the function  $f : f(x) = x^3 + 1$  and deduce from the graph its range and its monotony.

**2** Find in  $\mathbb{R}$  the S.S. of the equation :  $5^{x+1} + 5^{x-1} = 26$

**3** Find : (1)  $\lim_{x \rightarrow 1} \frac{x^3 - 2x + 1}{x^2 - 1}$

(2)  $\lim_{x \rightarrow 0} \frac{(x+1)^{11} - 1}{x}$

**4** Find the value of : (1)  $\lim_{x \rightarrow 3} \frac{x^2 - 8x + 15}{x - 3}$  (2)  $\lim_{x \rightarrow \infty} (x^5 + x^2 - 1)$

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Giza Governorate



Mathematics inspection

First

Multiple choice questions

Choose the correct answer from the given ones :

(1) The opposite figure

represents a function it's range

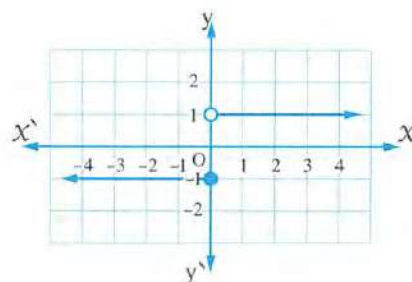
is .....

(a)  $\{1\}$

(b)  $\{1, -1\}$

(c)  $\{-1\}$

(d)  $\mathbb{R}$



(2)  $\lim_{x \rightarrow \infty} \frac{2x+3}{5x^2+4} = \dots\dots\dots$

(a) 2

(b) zero

(c)  $\frac{3}{4}$

(d)  $\frac{4}{10}$

(3) ABC is an equilateral triangle , its side length is  $5\sqrt{3}$  cm. , then the length of the diameter of circumcircle = ..... cm.

(a) 5

(b) 10

(c) 15

(d) 20

(4) The exponential function  $f : f(x) = a^x$  is increasing when .....

(a)  $a > 0$

(b)  $a > 1$

(c)  $a = 1$

(d)  $1 > a > 0$

(5)  $\lim_{x \rightarrow 1} \frac{x^7 - 1}{x - 1} = \dots\dots\dots$

(a) 35

(b) 7

(c) 42

(d) 1

(6) In  $\Delta ABC$  ,  $m(\angle A) : m(\angle B) : m(\angle C) = 3 : 5 : 4$  , then  $c^2 : a^2 = \dots\dots\dots$

(a)  $\sqrt{6} : 2$

(b)  $2 : 3$

(c)  $4 : 3$

(d)  $3 : 2$

(7)  $f$  is a function , where  $f(x) = (x-2)^2$  , then the equation of its symmetric axis is  $x = \dots\dots\dots$

(a) 2

(b) -2

(c) 1

(d) -1

- (8)  $\lim_{x \rightarrow 1} \frac{2x+k}{x+1} = 5$ , then  $k = \dots\dots\dots$   
 (a) 2 (b) 5 (c) 8 (d) 10
- (9) In  $\Delta ABC$ ,  $\frac{a}{\sin A} = 6$ , then the radius length of circumcircle =  $\dots\dots\dots$  cm.  
 (a) 2 (b) 3 (c) 5 (d) 6
- (10)  $\log_3 5 \times \log_2 3 \times \log_5 16 = \dots\dots\dots$   
 (a) 30 (b) 15 (c)  $\log 10000$  (d)  $\log_{30} 240$
- (11) The curve of the function  $g : g(x) = x^2 + 4$  is the same curve of the function  $f : f(x) = x^2$  by translation of magnitude 4 units in direction of  $\dots\dots\dots$   
 (a)  $\overrightarrow{OX}$  (b)  $\overrightarrow{OX}$  (c)  $\overrightarrow{Oy}$  (d)  $\overrightarrow{Oy}$
- (12)  $\lim_{x \rightarrow 1} \frac{x^2 - x^{-2}}{x - x^{-1}} = \dots\dots\dots$   
 (a) zero (b) 1 (c) 2 (d) -2
- (13) In  $\Delta ABC$ ,  $m(\angle A) = 30^\circ$ ,  $b = 15\sqrt{3}$  cm.,  $m(\angle B) = 60^\circ$ , then  $a = \dots\dots\dots$  cm.  
 (a) 30 (b) 45 (c) 15 (d) 60
- (14) S.S. of the equation  $\log_x (x+6) = 2$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $(3, -2)$  (b)  $\{3\}$  (c)  $\{3, 1\}$  (d)  $\{6, 1\}$
- (15)  $\lim_{x \rightarrow 1} (2x - 5) = \dots\dots\dots$   
 (a) 2 (b) -3 (c) 7 (d) zero
- (16) In  $\Delta ABC$ ,  $a^2 + b^2 - c^2 = \dots\dots\dots$   
 (a)  $\cos A$  (b)  $a b \cos C$  (c)  $\cos C$  (d)  $2 a b \cos C$
- (17) The solution set of inequality :  $|x - 2| < 5$  is  $\dots\dots\dots$   
 (a)  $[-3, 7]$  (b)  $] -3, 7[$  (c)  $\mathbb{R} - [-3, 7]$  (d)  $\mathbb{R} - ] -3, 7[$
- (18)  $\lim_{x \rightarrow 1} \frac{2x-4}{x-2} = \dots\dots\dots$   
 (a) 1 (b) 2 (c) -2 (d) zero
- (19) In  $\Delta ABC$ , if  $\sin A = 2 \sin C$ ,  $BC = 6$  cm., then  $AB = \dots\dots\dots$  cm.  
 (a) 2 (b) 3 (c) 4 (d) 6
- (20) In  $\Delta ABC$ ,  $\frac{a}{a+b} = \frac{\sin A}{\dots\dots\dots}$   
 (a)  $\sin B$  (b)  $\sin A + \sin B$  (c)  $\sin A + \sin C$  (d)  $\sin C$
- (21) In  $\Delta ABC$ ,  $a = 3$  cm.,  $b = 5$  cm.,  $c = 7$  cm., the measure of the greatest angle of  $\Delta ABC$  is  $\dots\dots\dots^\circ$   
 (a) 60 (b) 150 (c) 120 (d) 90



- (22) If  $X^{\frac{3}{2}} = 64$ , then  $X = \dots\dots\dots$
- (a) 512 (b) 16 (c) 4 (d) 2
- (23)  $f(X) = \dots\dots\dots$  is an even function.
- (a)  $\sin X$  (b)  $\tan 45^\circ$  (c)  $X \cos X$  (d)  $X^2 + \tan X$
- (24) The function  $f : f(X) = \frac{5}{X} + 2$ , its range is  $\dots\dots\dots$
- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{2\}$  (c)  $\{2\}$  (d)  $\mathbb{R} - \{0\}$
- (25) The symmetric point of the function  $f$  where  $f(X) = \frac{2X-1}{X}$  is  $\dots\dots\dots$
- (a) (1, 2) (b) (2, 1) (c) (-1, 2) (d) (0, 2)
- (26) The point of the vertex of the curve of the function  $f : f(X) = (X-2)^2 + 3$  is  $\dots\dots\dots$
- (a) (2, 3) (b) (2, -3) (c) (-2, 3) (d) (-2, -3)
- (27) If  $\log_4 X = 2$ , then the equivalent exponential form is  $\dots\dots\dots$
- (a)  $X^2 = 4$  (b)  $X^4 = 2$  (c)  $X = 8$  (d)  $X = 4^2$
- (28) If  $3^{X-2} = 2^{X-2}$ , then  $X = \dots\dots\dots$
- (a) 3 (b) -2 (c) 0 (d) 2

## Second Essay questions

Answer the following questions :

- 1 Without using calculator find the value of :

$$\log_2 \frac{3}{25} + 5 \log_2 5 + \log_2 27 - \log_2 \frac{125}{12} - \log_2 243$$

2 Find : (1)  $\lim_{x \rightarrow 3} \frac{X^3 - 27}{X^2 - 9}$

(2)  $\lim_{x \rightarrow \infty} \frac{4X^2 + 1}{X^2 - 2}$

3 Find : (1)  $\lim_{x \rightarrow 1} \frac{X^2 + 5X - 6}{X^2 - 1}$

(2)  $\lim_{x \rightarrow 1} \frac{(X+1)^5 - 32}{X - 1}$

- 4 Graph the curve of the function  $f$  where  $f(X) = |X - 3|$ , deduce the range and monotony of the function and tell whether it is even, odd or otherwise.


**First Multiple choice questions**

Choose the correct answer from the given ones :

- (1) The solution of the inequality  $|2X + 3| \leq 7$  is .....
- (a)  $[-5, 2]$  (b)  $]-5, 2[$  (c)  $\mathbb{R} - [-5, 2]$  (d)  $\mathbb{R} - ]-5, 2[$
- (2) In any  $\Delta ABC$  :  $\frac{\sin(A+B)}{\sin A} = \dots\dots\dots$
- (a)  $\frac{a}{a+b}$  (b)  $\frac{a+b}{a}$  (c)  $\frac{c}{a}$  (d)  $-\frac{c}{a}$
- (3) Which of the following functions is even function ?
- (a)  $y = X \cos X$  (b)  $y = X^2 \sin X$  (c)  $y = X \sin X$  (d)  $y = X^3$
- (4) The solution set of the equation  $3 \log_5 (X-2) = 6$  is .....
- (a)  $\{27\}$  (b)  $\{-27\}$  (c)  $\{25\}$  (d)  $\{7\}$
- (5) ABC is equilateral triangle inscribed in a circle of radius length 10 cm.  
 , then AB = ..... cm.
- (a) 5 (b)  $10\sqrt{3}$  (c) 10 (d)  $5\sqrt{3}$
- (6)  $\lim_{x \rightarrow \infty} \frac{(2X+1)(3-X)}{(X^2+2)} = \dots\dots\dots$
- (a) 6 (b) 2 (c) -2 (d)  $\infty$
- (7) The range of the function  $f : f(X) = |X-2| + 3$  is .....
- (a)  $[2, \infty[$  (b)  $[3, \infty[$  (c)  $]3, \infty[$  (d)  $]-\infty, 2]$
- (8) The solution set of the equation :  $\sqrt{X^2 - 10X + 25} = 10$  is .....
- (a)  $\{-15, 5\}$  (b)  $\{-15, -5\}$  (c)  $\{15, -5\}$  (d)  $\{15, 5\}$
- (9)  $\lim_{x \rightarrow 5} \frac{X^2 - 25}{X - 5} = \dots\dots\dots$
- (a) 5 (b) -5 (c) -10 (d) 10
- (10) In  $\Delta ABC$  , if  $a^2 + b^2 - c^2 = ab$  , then  $m(\angle C) = \dots\dots\dots$
- (a)  $\frac{\pi}{3}$  (b)  $\frac{\pi}{6}$  (c)  $\frac{\pi}{4}$  (d)  $\frac{\pi}{2}$
- (11)  $\lim_{x \rightarrow 1} \frac{aX+3}{X^2+1} = 5$  , then a = .....
- (a) 3 (b) 5 (c) -7 (d) 7
- (12) The solution set of the equation :  $5^X + 5^{X+1} = 150$  is .....
- (a)  $\{-2\}$  (b)  $\{2\}$  (c)  $\{-3\}$  (d)  $\{2, 3\}$

- (13)  $\lim_{x \rightarrow 2} \frac{x^n - 2^5}{x^2 - 2^m} = k$ , then  $m + n + k = \dots\dots\dots$   
 (a) 47 (b) 20 (c) 7 (d) 27
- (14) If  $\log 3 = x$ , then  $\log 90 = \dots\dots\dots$   
 (a)  $9x$  (b)  $2x + 1$  (c)  $x + 1$  (d)  $2x + 10$
- (15) The domain of the function  $f : f(x) = \sqrt{x - 3}$  is  $\dots\dots\dots$   
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{3\}$  (c)  $[3, \infty[$  (d)  $] - \infty, 3[$
- (16) In  $\triangle ABC$ ,  $\frac{a}{\sin A} + \frac{c}{\sin C} = 20$  cm., then the diameter length of the circumcircle of triangle ABC =  $\dots\dots\dots$  cm.  
 (a) 5 (b) 10 (c) 20 (d) 40
- (17) The axis of symmetry of the function  $f : f(x) = 5 - (3 - x)^2$  is  $\dots\dots\dots$   
 (a)  $x = 3$  (b)  $y = 5$  (c)  $x + 3 = 0$  (d)  $x = 5$
- (18) If the domain of the function  $f : f(x) = \frac{1}{x - 2} + 3$  is  $\mathbb{R} - \{a\}$ , then  $a^2 = \dots\dots\dots$   
 (a) 9 (b) -9 (c) -4 (d) 4
- (19) In  $\triangle LMN$ ,  $3 \sin L = 4 \sin M = 5 \sin N$ , then  $\ell : m : n = \dots\dots\dots$   
 (a) 4 : 5 : 3 (b) 15 : 12 : 20 (c) 20 : 15 : 12 (d) 3 : 4 : 5
- (20) If  $5^x = 7$ , then  $5^{x+1} = \dots\dots\dots$   
 (a)  $5^7$  (b)  $7^5$  (c) 12 (d) 35
- (21) The number of solutions of the  $\triangle ABC$  in which  $m(\angle A) = 112^\circ$ ,  $a = 7$  cm.,  $b = 4$  cm., equals  $\dots\dots\dots$   
 (a) 0 (b) 1 (c) 2 (d) 3
- (22)  $\lim_{x \rightarrow 0} \frac{\sqrt{x+9} - 3}{5x} = \dots\dots\dots$   
 (a) -30 (b) 30 (c)  $\frac{1}{30}$  (d)  $-\frac{1}{30}$
- (23) The domain of the function  $f : f(x) = \log x^2$  is  $\dots\dots\dots$   
 (a)  $\mathbb{R}^*$  (b)  $\mathbb{R}$  (c)  $\mathbb{R}^-$  (d)  $\mathbb{R}^+$
- (24) Measure of the greatest angle in triangle whose side lengths are 5, 7, 4 cm. is  $\dots\dots\dots$   
 (a)  $135^\circ 23'$  (b)  $44^\circ 25'$  (c)  $120^\circ$  (d)  $101^\circ 32'$
- (25)  $\lim_{x \rightarrow 0} \frac{x}{\cos x} = \dots\dots\dots$   
 (a) zero (b) 1 (c) not exist (d)  $\infty$
- (26)  $\triangle ABC$  in which  $m(\angle A) = 80^\circ$ ,  $m(\angle C) = 60^\circ$ ,  $b = 14$  cm., then  $a = \dots\dots\dots$   
 (a) 17.8 cm. (b) 18.9 cm. (c) 15.6 cm. (d) 21.4 cm.



(27) Which of the following is not a function from  $X$  to  $y$  ?

- (a)  $|y| = 2x^2$       (b)  $y^3 = 2x$       (c)  $y = |x + 1|$       (d)  $y = x^2 + 1$

(28)  $\frac{1}{\log_a abc} + \frac{1}{\log_c abc} + \frac{1}{\log_b abc} = \dots\dots\dots$

- (a)  $(abc)^2$       (b)  $abc$       (c)  $2abc$       (d)  $1$

## Second Essay questions

Answer the following questions :

- 1 Draw the curve of the function  $f : f(x) = (x - 2)^3$  from the graph deduce its range , and discuss its monotony.
- 2 If the volume of a sphere gives by the relation  $v = \frac{4}{3} \pi r^3$  ,  
if the volume equals  $345.45 \text{ cm}^3$ . Find its radius length.
- 3 Find with steps :  $\lim_{x \rightarrow 4} \frac{x^3 - 3x^2 - 4x}{x - 4}$
- 4 Find with steps :  $\lim_{x \rightarrow 0} \frac{x^2 + x}{\sqrt{2x + 9} - 3}$

7 Alexandria Governorate



West Education Zone  
Nabaa Elfekr secondary school

## First Multiple choice questions

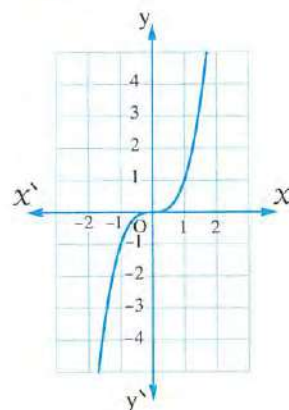
Choose the correct answer from the given ones :

(1) The domain of the function  $f : f(x) = \sqrt[3]{x - 5}$  is .....

- (a)  $[5, \infty[$       (b)  $]5, \infty[$       (c)  $] - \infty, 5[$       (d)  $\mathbb{R}$

(2) The opposite figure represents ..... function.

- (a) even  
(b) neither even nor odd  
(c) odd  
(d) symmetric about y-axis



(3) The range of  $f : f(x) = \frac{1}{x-2} - 1$  is .....

- (a)  $\mathbb{R} - \{2\}$  (b)  $\mathbb{R} - \{1\}$  (c)  $\mathbb{R} - \{-1\}$  (d)  $\mathbb{R}$

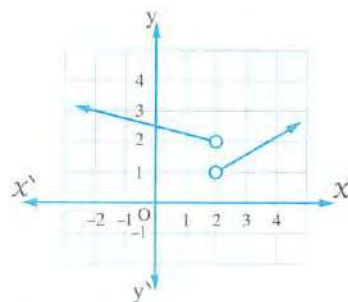
(4) The curve of the function  $g : g(x) = (x-2)^2$  is the same of the curve of the function  $f : f(x) = x^2$  by translate 2 units in direction of .....

- (a)  $\vec{OX}$  (b)  $\vec{OX}$  (c)  $\vec{OY}$  (d)  $\vec{OY}$

(5) In the opposite figure :

$$\lim_{x \rightarrow 2} f(x) = \dots\dots\dots$$

- (a) 1  
(b) zero  
(c) 2  
(d) not exist.



(6) In  $\triangle ABC$  :  $m(\angle A) = 112^\circ$  ,  $m(\angle B) = 33^\circ$  ,  $c = 19$  cm. , then  $b \simeq$  ..... cm.

- (a) 16 (b) 17 (c) 18 (d) 20

(7) The radius of circumcircle of  $\triangle XYZ$  when  $m(\angle X) = 30^\circ$  ,  $x = 7$  cm. equals .....

- (a) 10 (b) 14 (c) 7 (d) 21

(8) The S.S. of the inequality  $|x| - 1 > 0$  in  $\mathbb{R}$  is .....

- (a)  $\mathbb{R} - [-1, 1]$  (b)  $]-1, 1[$  (c)  $\mathbb{R} - ]-1, 1[$  (d)  $[-1, 1]$

(9) The S.S. of the equation :  $5^{x+1} = 7^{x+1}$  in  $\mathbb{R}$  is .....

- (a)  $\{1\}$  (b)  $\{-1\}$  (c)  $\{\text{zero}\}$  (d)  $\{5\}$

(10) The equation of symmetry axis of the function  $f$  where  $f(x) = (x-2)^2 + 3$  is .....

- (a)  $x = 2$  (b)  $x = 3$  (c)  $y = 2$  (d)  $y = 3$

(11) The S.S. of the equation :  $\log_x(x+2) = 2$  is .....

- (a)  $\{-1\}$  (b)  $\{2\}$  (c)  $\{-1, 2\}$  (d)  $\{4\}$

(12)  $\lim_{x \rightarrow 0} (2x^2 + 3) = \dots\dots\dots$

- (a) 2 (b) 3 (c) 5 (d) 7

(13) In  $\triangle ABC$  :  $\frac{\sin A}{2} = \frac{\sin B}{3} = \frac{\sin C}{5}$  , then  $a : b : c = \dots\dots\dots$

- (a)  $4 : 3 : 10$  (b)  $2 : 3 : 5$  (c)  $4 : 6 : 5$  (d)  $4 : 3 : 5$

(14) In  $\triangle ABC$  :  $a^2 + b^2 - c^2 = \dots\dots\dots$

- (a)  $\cos A$  (b)  $ab \cos C$  (c)  $\cos C$  (d)  $2 ab \cos C$

- (15) If  $f$  odd function,  $a \in \text{domain of } f$ , then  $f(a) + f(-a) = \dots\dots\dots$   
 (a)  $2f(a)$  (b)  $2f(-a)$  (c) zero (d)  $f(a)$
- (16) The point of symmetry of the curve of the function  $f : f(x) = (x-2)^3 + 1$  is  $\dots\dots\dots$   
 (a)  $(2, 1)$  (b)  $(-2, -1)$  (c)  $(-2, 1)$  (d)  $(2, -1)$
- (17) If  $2^x = 3$ , then  $x = \dots\dots\dots$   
 (a) 2 (b)  $\frac{3}{2}$  (c)  $\log_3 2$  (d)  $\log_2 3$
- (18)  $\lim_{x \rightarrow 2} \frac{x^2 - 5x + 4}{x^2 - 1} = \dots\dots\dots$   
 (a)  $-\frac{2}{3}$  (b)  $\frac{2}{3}$  (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
- (19)  $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 + 1}}{x - 2} = \dots\dots\dots$   
 (a) 4 (b) 5 (c)  $-\frac{5}{2}$  (d) 2
- (20) The measure of smallest angle in  $\triangle ABC$  where  $a = 8$  cm.,  $b = 7$  cm. and its perimeter 21 cm.  $\approx \dots\dots\dots$   
 (a)  $22^\circ 34'$  (b)  $42^\circ 34'$  (c)  $36^\circ 34'$  (d)  $46^\circ 34'$
- (21) In  $\triangle ABC : \cos A = \frac{2}{5}$ ,  $b = 2.5$  cm.,  $c = 2$  cm., then  $a = \dots\dots\dots$   
 (a) 2 (b) 2.5 (c) 3 (d) 3.5
- (22) The S.S. of the equation  $|x - 7| = 5$  is  $\dots\dots\dots$   
 (a)  $\{7, 12\}$  (b)  $\{-2, 2\}$  (c)  $\{7, 5\}$  (d)  $\{12, 2\}$
- (23) The exponential function which its base (a) is increasing if  $\dots\dots\dots$   
 (a)  $a > 0$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = 1$
- (24) If  $f(x) = 5^x$ , then the S.S. of the equation :  $f(x+1) + f(x) = 150$  is  $\dots\dots\dots$   
 (a)  $\{5\}$  (b)  $\{2, 5\}$  (c)  $\{3\}$  (d)  $\{2\}$
- (25) In  $\triangle XYZ : X = 5$  cm.,  $Y = 7$  cm.,  $m(\angle Z) = 65^\circ$ , then  $Z = \dots\dots\dots$   
 (a) 7.6 (b) 6.7 (c) 7.8 (d) 8.7
- (26) In  $\triangle ABC$ , if  $m(\angle A) = 30^\circ$ ,  $a = 6$  cm., then  $\frac{b}{\sin B} = \dots\dots\dots$   
 (a) 3 (b) 6 (c)  $\frac{1}{2}$  (d) 12
- (27)  $\lim_{x \rightarrow 0} \frac{5x - 10}{4x - 8} = \dots\dots\dots$   
 (a)  $\frac{5}{4}$  (b) zero (c) 2 (d)  $\frac{4}{5}$
- (28) If  $\lim_{x \rightarrow 1} \frac{b}{x+1} = 5$ , then  $b = \dots\dots\dots$   
 (a) 4 (b) -1 (c) 1 (d) 10



## Second Essay questions

Answer the following questions :

- 1 Draw the curve of the function  $f : f(x) = (x-2)^2 + 1$ , then find its range and monotony and its type.
- 2 Find in  $\mathbb{R}$  the solution set of the inequality :  $|3x - 2| \leq 7$
- 3 Find :  $\lim_{x \rightarrow 5} \frac{x-5}{\sqrt{x+4}-3}$
- 4 Find :  $\lim_{x \rightarrow \infty} \frac{4x^2+1}{x^2-2}$

8 El-Kalyoubia Governorate

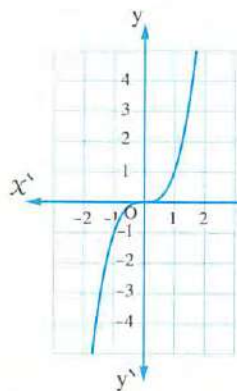


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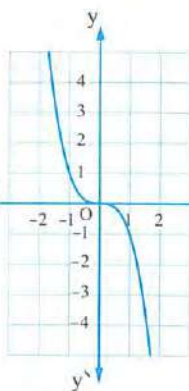
## First Multiple choice questions

Choose the correct answer from the given ones :

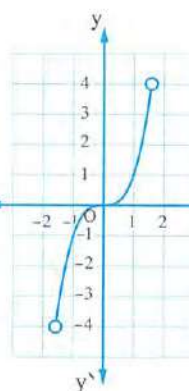
- (1) If  $f : \mathbb{R} \rightarrow \mathbb{R}$  where  $f(x) = x^3$ , then the figure which represents the function  $f$  is .....



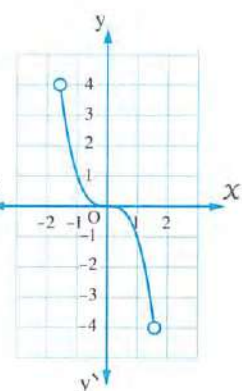
(a)



(b)



(c)



(d)

- (2) If  $5^{x-3} = 4^{3-x}$ , then  $x = \dots\dots\dots$

(a)  $\frac{5}{4}$

(b) 3

(c)  $\frac{4}{5}$

(d) 0

- (3) The range of the function  $f$  where  $f(x) = |x|$  is .....

(a)  $[0, \infty[$

(b)  $]0, \infty[$

(c)  $]-\infty, 0]$

(d)  $]-\infty, 0[$

- (4) If  $f(x) = 5^x$ , then  $f(-2) = \dots\dots\dots$

(a) -2

(b) 5

(c)  $\frac{1}{25}$

(d)  $\frac{1}{5}$

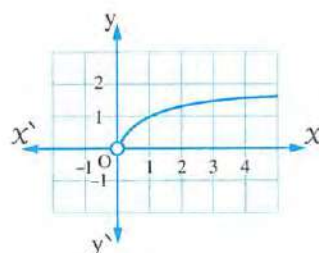
- (5) The solution set of the inequality :  $|x| - 1 > \text{zero}$  in  $\mathbb{R}$  is .....
- (a)  $\mathbb{R} - [-1, 1]$  (b)  $] -1, 1[$  (c)  $\mathbb{R} - ] -1, 1[$  (d)  $[-1, 1]$

- (6) If  $4 = \log_2 x$ , then the equivalent exponential form is .....

- (a)  $x^2 = 4$  (b)  $x^4 = 2$  (c)  $x = 2^4$  (d)  $x = 8$

- (7) The domain of the function in the figure opposite is .....

- (a)  $[0, \infty[$   
 (b)  $]0, \infty[$   
 (c)  $[0, 1]$   
 (d)  $]0, 2[$



- (8) Which of the following functions represents an increasing exponential function on its domain  $\mathbb{R}$  ?

- (a)  $y = 3(1.05)^x$  (b)  $y = 3\left(\frac{1}{1.05}\right)^x$  (c)  $y = 3 + (0.5)^x$  (d)  $y = (0.05)^x$

- (9) In  $\Delta ABC$ , if  $a = b = 8$  cm. and the perimeter of  $\Delta ABC = 26$  cm., then  $m(\angle C) \approx$  .....

- (a)  $35.3^\circ$  (b)  $52.3^\circ$  (c)  $77.4^\circ$  (d)  $108^\circ$

- (10) In  $\Delta ABC$ , if  $m(\angle A) = 30^\circ$  and  $a = 6$  cm., then  $\frac{b}{\sin B} =$  ..... cm.

- (a) 3 (b) 6 (c)  $\frac{1}{5}$  (d) 12

- (11)  $\lim_{x \rightarrow 1} \frac{x^5 - 1}{x - 1} =$  .....

- (a) 5 (b) 1 (c) 4 (d) 20

- (12) In any triangle LMN,  $\frac{l}{\sin L} =$  .....

- (a)  $\frac{m}{\sin N}$  (b)  $\frac{n}{\sin M}$  (c)  $\frac{m+n}{\sin N + \sin M}$  (d)  $3r$

- (13)  $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 + 1}}{x - 2} =$  .....

- (a) 4 (b) 5 (c)  $\frac{5}{-2}$  (d) 2

- (14)  $\lim_{x \rightarrow 0} (2x^2 + 3) =$  .....

- (a) 2 (b) 3 (c) 5 (d) 7

- (15) In  $\Delta ABC$ , if  $2 \sin A = 3 \sin B = 4 \sin C$ , then  $a : b : c =$  .....

- (a)  $2 : 3 : 4$  (b)  $4 : 3 : 2$  (c)  $3 : 4 : 6$  (d)  $6 : 4 : 3$

- (16) In  $\Delta ABC$ , if  $4 \sin A = 3 \sin B = 6 \sin C$ , then  $m(\angle C) \approx$  .....

- (a)  $89^\circ$  (b)  $29^\circ$  (c)  $57^\circ$  (d)  $82^\circ$

- (17) The solution set in  $\mathbb{R}$  of the equation :  $2^{2X} - 12 \times 2^X + 2^5 = 0$  equals .....
- (a)  $\{4, 8\}$  (b)  $\{2, 3\}$  (c)  $\{16, 2\}$  (d)  $\{1, 4\}$
- (18) The function  $f : f(X) = a^X$  is increasing if .....
- (a)  $a > 0$  (b)  $a > 1$  (c)  $a = 1$  (d)  $0 < a < 1$
- (19) ABC is an equilateral triangle its side length  $= 5\sqrt{3}$  cm. , then the diameter length of its circumcircle equals ..... cm.
- (a)  $5\sqrt{3}$  (b)  $10\sqrt{3}$  (c) 10 (d) 5
- (20)  $\log_5 49 \times \log_8 5 \times \log_9 8 \times \log_7 9 = \dots\dots\dots$
- (a)  $\log 100$  (b)  $\log 7$  (c)  $\log 5$  (d)  $\log 2$
- (21) If  $f : \mathbb{R} \longrightarrow \mathbb{R}$  , where  $f(X) = (a + 1)X + b - 2$  and  $f(X)$  maps each real number to itself , then  $(a, b) = \dots\dots\dots$
- (a)  $(0, 3)$  (b)  $(0, -3)$  (c)  $(0, 2)$  (d)  $(-1, 2)$
- (22) The type of the function  $f : f(X) = \frac{\sin X}{X}$  is .....
- (a) even. (b) odd.  
(c) neither odd nor even. (d) both odd and even.
- (23)  $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\tan X}{X} = \dots\dots\dots$
- (a)  $\frac{\pi}{4}$  (b) 1 (c)  $\frac{4}{\pi}$  (d) does not exist.
- (24)  $\lim_{x \rightarrow 1} \frac{2X + a}{X + 1} = 5$  , then  $a = \dots\dots\dots$
- (a) 2 (b) 5 (c) 8 (d) 10
- (25) In any triangle XYZ ,  $X^2 + y^2 - 2Xy \cos Z = \dots\dots\dots$
- (a)  $X^2$  (b)  $y^2$  (c)  $z^2$  (d)  $z$
- (26) If  $f(X) = \frac{\sqrt{X^2 - 2X + 1}}{X - 1}$  , then the range of the function  $f$  is .....
- (a)  $\{1\}$  (b)  $\mathbb{R}$  (c)  $[-1, 1[$  (d)  $\{-1, 1\}$
- (27)  $\lim_{x \rightarrow 1} \frac{X^2 - 1}{X - 1} = \dots\dots\dots$
- (a) 0 (b) 1 (c) 2 (d) 3
- (28) In  $\Delta ABC$  ,  $m(\angle A) : m(\angle B) : m(\angle C) = 3 : 5 : 4$  , then  $c^2 : a^2 = \dots\dots\dots$
- (a)  $\sqrt{6} : 2$  (b)  $2 : 3$  (c)  $4 : 3$  (d)  $3 : 2$



## Second Essay questions

Answer the following questions :

- 1 Graph the curve of the function  $f$  where  $f(x) = |x - 3|$ , deduce the range and monotony of the function and tell whether it is even, odd or otherwise.
- 2 Find the solution set of the following equation in  $\mathbb{R}$ :  $\log_2 x + \log_2 (x + 1) = 1$
- 3 Find the value of the following :  $\lim_{x \rightarrow \infty} \frac{4 - 3x^2}{\sqrt{x^4 + 5}}$
- 4 Find the value of the following :  $\lim_{x \rightarrow -1} \frac{2x^3 - x^2 - 2x + 1}{x^3 + 1}$

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El-Menia Governorate



Minia Educational Directorate  
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## First Multiple choice questions

Choose the correct answer from the given ones :

- (1) The range of the function  $f : f(x) = |x|$  is .....
  - (a)  $[0, \infty[$
  - (b)  $]0, \infty[$
  - (c)  $]-\infty, 0]$
  - (d)  $]-\infty, 0[$
- (2) The curve of the even function is symmetric about the straight line .....
  - (a)  $y = x$
  - (b)  $\overleftrightarrow{yy}$
  - (c)  $\overleftrightarrow{xx}$
  - (d)  $y = -x$
- (3) The S.S. of the inequality  $|3 - 2x| \leq 1$  in  $\mathbb{R}$  is .....
  - (a)  $[1, 2]$
  - (b)  $]1, 2[$
  - (c)  $\mathbb{R} - ]1, 2[$
  - (d)  $\mathbb{R} - [1, 2]$
- (4) The range of the function  $f : f(x) = \frac{15}{x} + 2$  is .....
  - (a)  $\pi$
  - (b)  $\mathbb{R} - \{2\}$
  - (c)  $\{2\}$
  - (d)  $\mathbb{R} - \{0\}$
- (5) The S.S. of the equation  $|2x - 1| = 5$  in  $\mathbb{R}$  is .....
  - (a)  $\{3\}$
  - (b)  $\{-2\}$
  - (c)  $\emptyset$
  - (d)  $\{3, -2\}$
- (6) The point of symmetry of the curve of the function  $f : f(x) = x^3$  is .....
  - (a)  $(1, 1)$
  - (b)  $(0, 0)$
  - (c)  $(1, 0)$
  - (d)  $(0, 1)$
- (7) The domain of the function  $f : f(x) = \frac{2x}{x^2 - 4}$  is .....
  - (a)  $\mathbb{R} - \{-2, 2\}$
  - (b)  $\mathbb{R} - \{-2, 0, 2\}$
  - (c)  $\mathbb{R}$
  - (d)  $\mathbb{R} - \{4\}$
- (8) The function  $f : f(x) = a^x$  is decreasing if .....
  - (a)  $a = 1$
  - (b)  $a > 1$
  - (c)  $0 < a < 1$
  - (d)  $a = -1$

- (9) If  $3^{X+1} - 3^X = 54$ , then  $X = \dots\dots\dots$   
 (a) 1 (b) 2 (c) 3 (d) 4
- (10) If  $f(X) = 3^{X+2}$ , then  $f(X+1) \times f(-X) = \dots\dots\dots$   
 (a) 27 (b) 81 (c) 243 (d) 729
- (11) If  $\log 3 = X$ ,  $\log 5 = y$ , then  $\log 15 = \dots\dots\dots$   
 (a)  $X + y$  (b)  $X - y$  (c)  $Xy$  (d)  $\frac{X}{y}$
- (12) If  $3^{X-2} = 2^{X-2}$ , then  $X = \dots\dots\dots$   
 (a) 3 (b) -2 (c) 0 (d) 2
- (13) The solution set of the equation :  $X^{\frac{4}{3}} = 81$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\{-27, 27\}$  (b)  $\{9, -9\}$  (c)  $\{9\}$  (d)  $\{27\}$
- (14) If  $2^{X-3} = 1$ , then  $X = \dots\dots\dots$   
 (a) -3 (b) 3 (c) 1 (d) zero
- (15)  $\lim_{x \rightarrow 1} \frac{2X-4}{X-2} = \dots\dots\dots$   
 (a) 1 (b) 2 (c) -2 (d) zero
- (16)  $\lim_{x \rightarrow 4} \frac{X^2 + 7X + b}{X^2 - 6X + 8} = \frac{15}{2}$ , then  $b = \dots\dots\dots$   
 (a) -44 (b) 7 (c) -8 (d) 8
- (17)  $\lim_{y \rightarrow 2} \frac{y^5 - 32}{y - 2} = \dots\dots\dots$   
 (a)  $31y^4$  (b)  $32 \times 2^4$  (c) 64 (d)  $5 \times 2^4$
- (18)  $\lim_{y \rightarrow 0} \frac{X^2 + X}{X} = \dots\dots\dots$   
 (a) zero (b) 1 (c) 2 (d) 3
- (19)  $\lim_{x \rightarrow \infty} \left( \frac{3X^2 + 2X + 1}{X^2 - 3X + 2} \right)^4 = \dots\dots\dots$   
 (a) 3 (b) 9 (c) 27 (d) 81
- (20)  $\lim_{x \rightarrow \infty} \frac{kX}{3X+1} = 4$ , then  $k = \dots\dots\dots$   
 (a) 16 (b) 12 (c) 7 (d)  $\frac{4}{3}$
- (21) In  $\Delta XYZ$ ,  $\frac{X}{\sin X} = 6$ , then the length of diameter of its circumcircle =  $\dots\dots\dots$  length unit.  
 (a) 4 (b) 12 (c) 6 (d) 9
- (22) In  $\Delta ABC$  : if  $2 \sin A = 3 \sin B = 4 \sin C$ , then  $a : b : c = \dots\dots\dots$   
 (a) 2 : 3 : 4 (b) 4 : 3 : 2 (c) 3 : 4 : 6 (d) 6 : 4 : 3
- (23) The measure of the greatest angle of the triangle whose side lengths are 3 cm., 5 cm. and 7 cm. is  $\dots\dots\dots$   
 (a)  $150^\circ$  (b)  $120^\circ$  (c)  $60^\circ$  (d)  $30^\circ$

- (24) Triangle XYZ in which :  $Y = 6$  cm. ,  $Z = 10$  cm. ,  $m(\angle X) = 120^\circ$  , then the perimeter of the triangle = ..... cm.  
 (a) 24.72 (b) 26.3 (c) 28.88 (d) 30
- (25) In  $\Delta ABC$  , if  $4 \sin A = 3 \sin B = 6 \sin C$  , then  $m(\angle C) = \dots\dots\dots$  (to nearest degree)  
 (a)  $89^\circ$  (b)  $29^\circ$  (c)  $57^\circ$  (d)  $82^\circ$
- (26) If ABC is a triangle in which  $a = 4$  cm. ,  $b = 4\sqrt{3}$  cm. ,  $c = 8$  cm. , then sine of its smallest angle = .....  
 (a)  $\frac{1}{2}$  (b)  $\frac{\sqrt{3}}{2}$  (c) 1 (d) zero
- (27)  $\Delta ABC$  in which  $a = 8$  cm. ,  $b = 7$  cm. ,  $\cos C = \frac{1}{2}$  , then the area of  $\Delta ABC = \dots\dots\dots$   $\text{cm}^2$ .  
 (a) 14 (b)  $14\sqrt{3}$  (c) 8 (d)  $28\sqrt{3}$
- (28) In any  $\Delta XYZ : x^2 + y^2 - 2xy \cos z = \dots\dots\dots$   
 (a)  $x^2$  (b)  $y^2$  (c)  $z^2$  (d)  $z$

## Second Essay questions

Answer the following questions :

- 1 Find in  $\mathbb{R}$  the solution set of :  $|x - 3| \leq 4$
- 2 Find the domain of  $f : f(x) = \log_4(4 - x)$
- 3 Find :  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 5x + 6}$
- 4 Find :  $\lim_{x \rightarrow \infty} \frac{2x - 9}{|3x| + 7}$

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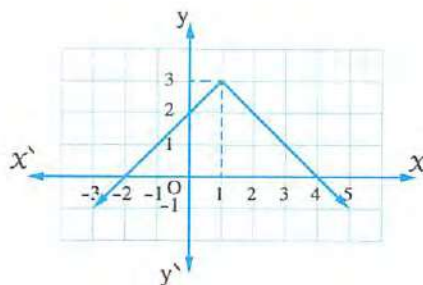
## First Multiple choice questions

Choose the correct answer from the given ones :

- (1) Vertex of function  $f : f(x) = (x - 4)^2 + 2$  is .....  
 (a)  $(-4, 2)$  (b)  $(2, 4)$  (c)  $(4, -2)$  (d)  $(4, 2)$
- (2)  $\lim_{x \rightarrow -2} (3x^2 + x - 4)$  is .....  
 (a) 3 (b) 12 (c) 9 (d) 6
- (3) If  $3^{x-3} = 4^{x-3}$  , then  $x = \dots\dots\dots$   
 (a)  $\{9\}$  (b)  $\{-3\}$  (c)  $\{\text{zero}\}$  (d)  $\{3\}$



- (4) Domain of  $f : f(x) = \frac{x+2}{x^2-4}$  is .....
- (a)  $\mathbb{R} - \{2\}$  (b)  $\mathbb{R} - \{-2\}$  (c)  $\mathbb{R} - \{2, -2\}$  (d)  $\emptyset$
- (5) In  $\triangle ABC$  which is drawn in a circle, then  $\frac{1}{2r} = \dots\dots\dots$
- (a)  $\frac{a}{\sin A}$  (b)  $\frac{b}{\sin B}$  (c)  $\frac{c}{\sin C}$  (d)  $\frac{\sin A}{a}$
- (6)  $\lim_{x \rightarrow 0} \frac{x^2 - x}{x}$  is .....
- (a) zero (b)  $\infty$  (c)  $-\infty$  (d)  $-1$
- (7) In  $\triangle ABC$ , if  $a = 5$ ,  $b = 7$ ,  $c = 8$ , then  $m(\angle B) \simeq \dots\dots\dots$
- (a)  $90^\circ$  (b)  $80^\circ$  (c)  $70^\circ$  (d)  $60^\circ$
- (8) Diameter length of circumcircle of triangle ABC in which  $m(\angle A) = 60^\circ$ ,  $a = \sqrt{3}$  cm. is ..... cm.
- (a)  $\sqrt{\frac{3}{2}}$  (b)  $2\sqrt{3}$  (c) 2 (d)  $\sqrt{3}$
- (9)  $\lim_{x \rightarrow 2} \sqrt{3x+3} = \dots\dots\dots$
- (a) 1 (b)  $-3$  (c) 3 (d)  $\pm 3$
- (10) Solution set of :  $|x| + 3 = 0$ , is .....
- (a)  $\pm 3$  (b) 3 (c)  $-3$  (d)  $\emptyset$
- (11) Type of function  $f : f(x) = 2 - x^2$  is .....
- (a) even. (b) odd.  
(c) neither even nor odd. (d) increasing.
- (12) Monotony of function  $f : f(x) = \left(\frac{1}{5}\right)^x$ , is .....
- (a) increasing. (b) decreasing.  
(c) increasing and decreasing. (d) constant.
- (13)  $\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a}$  is .....
- (a)  $an^{a-1}$  (b)  $na^{1-n}$  (c)  $na^{1-a}$  (d)  $na^{n-1}$
- (14) In the opposite figure :
- Rule of the function is .....
- (a)  $f(x) = |x - 1| + 3$   
(b)  $f(x) = 3 - |x + 1|$   
(c)  $f(x) = 3 - |x - 1|$   
(d)  $f(x) = |1 - x| + 3$



- (15) In  $\Delta ABC$  if  $m(\angle A) = 30^\circ$  and  $a = 6$  cm. , then  $\frac{b}{\sin B} = \dots\dots\dots$   
 (a) 11 (b) 21 (c) 13 (d) 12
- (16)  $\lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x - 1} = \dots\dots\dots$   
 (a) 1 (b) 2 (c) 3 (d) 4
- (17) In  $\Delta ABC : b^2 + c^2 - a^2 = \dots\dots\dots$   
 (a)  $2bc \cos A$  (b)  $2ac \cos B$  (c)  $2bc \cos C$  (d)  $2ab \cos C$
- (18) The range of the function  $f : f(x) = -(x)^2$  is  $\dots\dots\dots$   
 (a)  $]-\infty, 0[$  (b)  $]0, \infty[$  (c)  $[0, \infty[$  (d)  $]-\infty, 0]$
- (19) If :  $\log_2(x) + \log_2(x+1) = 1$  , where  $x \in \mathbb{R}$  , then  $x = \dots\dots\dots$   
 (a)  $\{-1, 2\}$  (b)  $\{1\}$  (c)  $\{2\}$  (d)  $\{-2, 1\}$
- (20)  $\lim_{x \rightarrow 0} \frac{(x+1)^{17} - 1}{x} = \dots\dots\dots$   
 (a) 15 (b) 16 (c) 18 (d) 17
- (21) Symetric point of the curve  $f : f(x) = 3 - \frac{1}{2-x}$   
 (a)  $(3, -2)$  (b)  $(-2, 3)$  (c)  $(-2, -3)$  (d)  $(2, 3)$
- (22)  $\log_5 \sqrt[5]{5} = \dots\dots\dots$   
 (a) 2 (b) 5 (c)  $\frac{1}{2}$  (d) -1
- (23) In  $\Delta ABC$  if  $a : b : c = 3 : 2 : 2$  , then  $\cos A = \dots\dots\dots$   
 (a)  $\frac{1}{2}$  (b)  $-\frac{1}{2}$  (c)  $\frac{3}{4}$  (d)  $-\frac{1}{8}$
- (24)  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x - 2} = \dots\dots\dots$   
 (a) 64 (b) 46 (c) 80 (d) 82
- (25) If  $f : f(x) = \frac{1}{3}$  , then  $f\left(\frac{1}{3}\right) = \dots\dots\dots$   
 (a) 1 (b)  $\frac{1}{9}$  (c) 3 (d)  $\frac{1}{3}$
- (26)  $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 - 1}}{x - 2} = \dots\dots\dots$   
 (a) 4 (b) 5 (c) 1 (d) 2
- (27) Range of the function  $f : f(x) = x$  is  $\dots\dots\dots$   
 (a)  $\mathbb{R} - \{1\}$  (b)  $\mathbb{R} - \{0\}$  (c)  $\mathbb{R}$  (d)  $\mathbb{R} - \{0, 1\}$
- (28) The two curves of the two functions  $f : f(x) = 2^x$  and  $g : g(x) = \left(\frac{1}{2}\right)^x$  intersect at  $x = \dots\dots\dots$  ,  $y = \dots\dots\dots$   
 (a)  $(-2, 0)$  (b)  $(0, -2)$  (c)  $(0, 1)$  (d)  $(1, 0)$

**Second****Essay questions**

**Answer the following questions :**

- 1** Find :  $\lim_{x \rightarrow \infty} \left( 5 - \frac{5}{x^3} \right)$

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- 2** Use the curve of  $f : f(x) = x^3$  to graph  $g : g(x) = x^3 - 3$  From the graph deduce domain and its range.

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- 3** Use the curve of the function  $f$  where  $f(x) = \frac{1}{x-1}$  to represent  $g$  where  $g(x) = f(x) + 2$   
**Find :**
  - (a) Monotony of the function  $g$
  - (b) Range of  $g$

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- 4** Find the perimeter of  $\triangle ABC$  in which  $a = 8$  cm. ,  $b = 6$  cm. and  $m(\angle C) = 48^\circ$



## Model

1

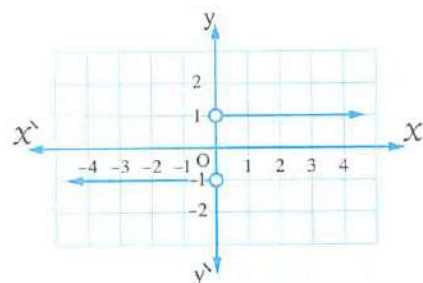
Interactive test 1



### First

### Multiple choice questions

Choose the correct answer from the given ones :



1 The range of the given function in the opposite figure is .....

- (a)  $\{1\}$  (b)  $\{1, -1\}$   
(c)  $\{-1\}$  (d)  $\mathbb{R}$

2 If  $5^{X-3} = 4^{3-X}$ , then  $X = \dots\dots\dots$

- (a)  $\frac{5}{4}$  (b) 3 (c)  $\frac{4}{5}$  (d) zero

3  $\lim_{x \rightarrow \infty} \frac{2x+3}{5x^2+4} = \dots\dots\dots$

- (a) 2 (b) zero (c)  $\frac{3}{4}$  (d)  $\frac{2}{5}$

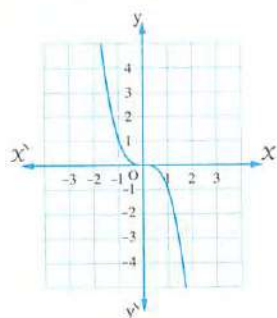
4 In  $\triangle ABC$ , if  $4 \sin A = 3 \sin B = 6 \sin C$ , then  $m(\angle C) \simeq \dots\dots\dots$

- (a)  $89^\circ$  (b)  $29^\circ$  (c)  $57^\circ$  (d)  $82^\circ$

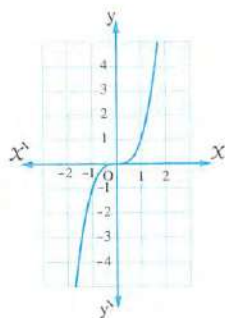
5 In  $\triangle ABC$ ,  $m(\angle C) = 96^\circ 23'$ ,  $a = 7$  cm.,  $b = 9$  cm., then  $c \simeq \dots\dots\dots$  cm.

- (a) 7 (b) 9 (c) 13 (d) 12

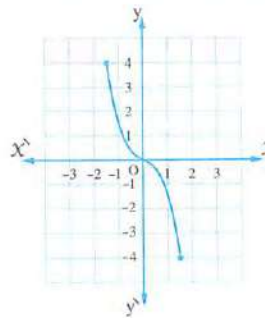
6 If  $f: \mathbb{R} \longrightarrow \mathbb{R}$  where  $f(x) = x^3$ , then the figure which represents the function  $f$  is .....



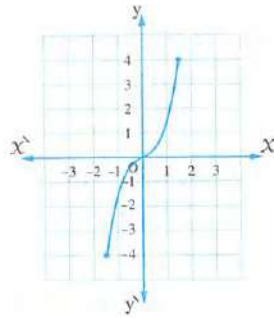
(a)



(b)



(c)



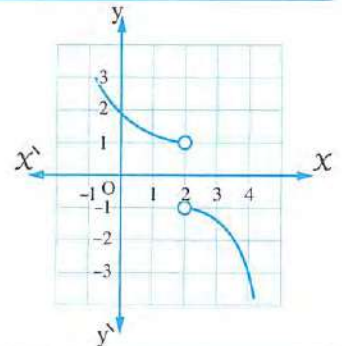
(d)

7 The solution set in  $\mathbb{R}$  of the equation:  $2^{2x} - 12 \times 2^x + 2^5 = 0$  equals .....

- (a)  $\{4, 8\}$  (b)  $\{2, 3\}$  (c)  $\{16, 2\}$  (d)  $\{1, 4\}$

8  $\lim_{x \rightarrow 0} \frac{(x+2)^5 - 32}{x} = \dots\dots\dots$   
 (a) 25 (b) 64 (c) 80 (d) 100

- 9 The opposite figure represents the curve of the function  $f$ , then  $\lim_{x \rightarrow 2} f(x) = \dots\dots\dots$   
 (a) 1 (b) -1  
 (c) 2 (d) does not exist.



- 10 The function  $f : f(x) = a^x$  is increasing if  $\dots\dots\dots$   
 (a)  $a > 0$  (b)  $a > 1$  (c)  $a = 1$  (d)  $0 < a < 1$

- 11 If  $x = 5 + 2\sqrt{6}$ , then  $\log\left(x + \frac{1}{x}\right) = \dots\dots\dots$   
 (a) 1 (b)  $5 - 2\sqrt{6}$  (c) 10 (d)  $5 + 2\sqrt{6}$

- 12 ABC is an equilateral triangle, its side length =  $5\sqrt{3}$  cm., then the diameter length of its circumcircle equals  $\dots\dots\dots$  cm.  
 (a)  $5\sqrt{3}$  (b)  $10\sqrt{3}$  (c) 10 (d) 5

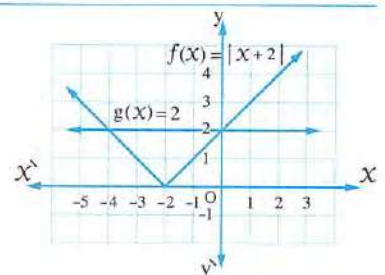
- 13  $\log_5 49 \times \log_8 5 \times \log_9 8 \times \log_7 9 = \dots\dots\dots$   
 (a)  $\log 100$  (b)  $\log 7$  (c)  $\log 5$  (d)  $\log 2$

14  $\lim_{x \rightarrow 1} \frac{x^7 - 1}{x - 1} = \dots\dots\dots$   
 (a) 35 (b) 7 (c) 42 (d) 1

- 15 The solution set of the equation :  $\log_3 x \times \log_2 3 = 5$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\{32\}$  (b)  $\{5\}$  (c)  $\{3\}$  (d)  $\{2\}$

- 16 In  $\triangle ABC$ ,  $m(\angle A) : m(\angle B) : m(\angle C) = 3 : 5 : 4$ , then  $c^2 : a^2 = \dots\dots\dots$   
 (a)  $\sqrt{6} : 2$  (b)  $2 : 3$  (c)  $4 : 3$  (d)  $3 : 2$

- 17 In the opposite figure :  
 The solution set of the inequality :  $f(x) < g(x)$   
 in  $\mathbb{R}$  is  $\dots\dots\dots$



- (a)  $\{-4, 0\}$  (b)  $[-4, 0]$   
 (c)  $\mathbb{R} - [-4, 0]$  (d)  $]-4, 0[$

**18** The type of the function  $f : f(x) = \frac{\sin x}{x}$  is .....

- (a) even. (b) odd.  
(c) neither odd nor even. (d) both odd and even.

**19**  $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\tan x}{x} = \dots\dots\dots$

- (a)  $\frac{\pi}{4}$  (b) 1 (c)  $\frac{4}{\pi}$  (d) does not exist.

**20** If  $x^{\frac{3}{2}} = 8$ , then  $x = \dots\dots\dots$

- (a) 2 (b) 4 (c) 8 (d) 9

**21**  $\lim_{x \rightarrow 2} \frac{x^3 - 7x + 6}{3x^2 - 8x + 4} = \dots\dots\dots$

- (a)  $\frac{4}{5}$  (b)  $\frac{2}{3}$  (c)  $\frac{5}{4}$  (d)  $\frac{3}{2}$

**22** If  $\lim_{x \rightarrow 1} \frac{2x + a}{x + 1} = 5$ , then  $a = \dots\dots\dots$

- (a) 2 (b) 5 (c) 8 (d) 10

**23** In any triangle XYZ,  $x^2 + y^2 - 2xy \cos Z = \dots\dots\dots$

- (a)  $x^2$  (b)  $y^2$  (c)  $z^2$  (d)  $z$

**24** The number of possible solutions for the triangle ABC where :  $m(\angle A) = 60^\circ$ ,  $b = 3$  cm,  $a = 5$  cm. is .....

- (a) 1 (b) 2  
(c) zero (d) infinite number.

**25** If  $\left(\frac{1}{2}\right)^{a^2 - a - 2} = 1$  where  $a > 0$ , then  $a = \dots\dots\dots$

- (a) 1 (b) -3 (c) 2 (d) 3

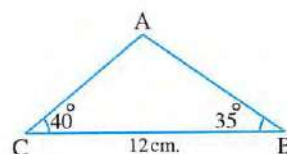
**26** If  $f(x) = \frac{\sqrt{x^2 - 2x + 1}}{x - 1}$ , then the range of the function  $f$  is .....

- (a)  $\{1\}$  (b)  $\mathbb{R}$  (c)  $[-1, 1[$  (d)  $\{-1, 1\}$

**27** In the opposite figure :

The length of  $\overline{AB} \approx \dots\dots\dots$  cm.

- (a) 6 (b) 7  
(c) 8 (d) 9





**28** In  $\Delta XYZ$ , the expression  $\frac{x^2 + y^2 - z^2}{2xy}$  equals .....

(a)  $\cos X$ (b)  $\cos Y$ (c)  $\cos Z$ (d)  $\sin Z$ 

## Second Essay questions

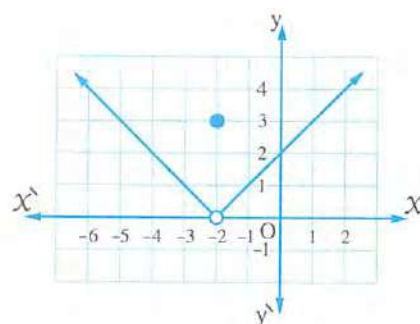
Answer the following questions :

**1** Use the curve of the function  $f$  where  $f(x) = \frac{1}{x}$  to represent the function  $g : g(x) = f(x-2) + 2$  and from the graph determine the range and discuss its monotony.

**2** Find :  $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 + 1}}{5x + 2}$

**3** Find the solution set in  $\mathbb{R}$  of the inequality :  $\sqrt{4x^2 - 12x + 9} \leq 9$

**4** From the opposite figure, find :

(1)  $\lim_{x \rightarrow -2} f(x)$ (2)  $f(-2)$ (3)  $\lim_{x \rightarrow 0} f(x)$ (4)  $f(0)$ 

**Model**

**2**

Interactive test **2**



## First Multiple choice questions

Choose the correct from the given ones :

**1** The range of the function  $f : f(x) = |x|$  is .....

(a)  $[0, \infty[$ (b)  $]0, \infty[$ (c)  $]-\infty, 0]$ (d)  $]-\infty, 0[$ 

**2**  $\lim_{x \rightarrow \infty} \left(\frac{3}{5}\right)^{\frac{1}{x}} = \dots\dots\dots$

(a) 1

(b) -1

(c)  $\frac{3}{5}$ (d)  $\infty$ 

**3**  $\lim_{x \rightarrow 1} \frac{x^5 - 1}{x - 1} = \dots\dots\dots$

(a) 5

(b) 1

(c) 4

(d) 20

- 4** In  $\triangle ABC$ ,  $\frac{a}{\sin A} = 6$  cm., then the radius length of its circumcircle = ..... cm.  
 (a) 2 (b) 3 (c) 5 (d) 6
- 
- 5** If  $f$  is an odd function and  $X f(X) + X^3 f(-X) = 2$ , then  $f(2) =$  .....  
 (a) 3 (b)  $\frac{1}{3}$  (c)  $-\frac{1}{3}$  (d) -3
- 
- 6** In  $\triangle XYZ$ ,  $\frac{X^2 + Y^2 - Z^2}{2XY} =$  .....  
 (a)  $\cos X$  (b)  $\cos Y$  (c)  $\cos Z$  (d)  $\sin Z$
- 
- 7** If  $f(X) = 3^X$ , then the solution set in  $\mathbb{R}$  of the equation  $f(2X) - 28f(X) + f(3) = \text{zero}$  equals .....  
 (a)  $\{1, 27\}$  (b)  $\{1, 3\}$  (c)  $\{0, 3\}$  (d)  $\{3\}$
- 
- 8** The logarithmic form that equivalent to the exponential form :  $2^7 = 128$  is .....  
 (a)  $\log_2 128 = 7$  (b)  $\log_2 7 = 128$   
 (c)  $\log_7 128 = 2$  (d)  $\log_7 2 = 128$
- 
- 9** The curve of the even function is symmetric about the straight line .....  
 (a)  $y = X$  (b)  $\overleftrightarrow{y\bar{y}}$  (c)  $\overleftrightarrow{X\bar{X}}$  (d)  $y = -X$
- 
- 10** In  $\triangle LMN$ ,  $\frac{\sin L}{3} = \frac{2 \sin M}{3} = \frac{\sin N}{4}$ , then  $l : m : n =$  .....  
 (a)  $6 : 8 : 3$  (b)  $3 : 6 : 8$  (c)  $8 : 3 : 6$  (d)  $6 : 3 : 8$
- 
- 11** In  $\triangle ABC$ ,  $c = 7$  cm.,  $m(\angle A) = 70^\circ$ ,  $m(\angle B) = 40^\circ$ , then  $b \simeq$  ..... cm.  
 (a) 3.7 (b) 4.8 (c) 8.4 (d) 7.3
- 
- 12** If  $\lim_{x \rightarrow a} \frac{aX}{3} = 12$ , then  $a =$  .....  
 (a)  $\pm 12$  (b)  $\pm 6$  (c) 3 (d) -3
- 
- 13** The range of the function  $f : f(X) = \frac{X-2}{2-X}$  equals .....  
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{2\}$  (c)  $\mathbb{R} - \{-2\}$  (d)  $\{-1\}$
- 
- 14** If  $\log 3 = X$ ,  $\log 7 = y$ , then  $\log 21 =$  .....  
 (a)  $Xy$  (b)  $X + y$  (c)  $X - y$  (d)  $\frac{X}{y}$

15  $\log_3 5 \times \log_2 3 \times \log_5 16 = \dots\dots\dots$

- (a) 30 (b) 15 (c)  $\log 10000$  (d)  $\log_{30} 240$

16 The curve of the function  $g : g(x) = x^2 + 4$  is the same as the curve of  $f : f(x) = x^2$  by translation 4 units in the direction of .....

- (a)  $\overrightarrow{OX}$  (b)  $\overrightarrow{OX}$  (c)  $\overrightarrow{Oy}$  (d)  $\overrightarrow{Oy}$

17  $\lim_{x \rightarrow 5} \frac{\sqrt{x-1} - 2}{x-5} = \dots\dots\dots$

- (a)  $\frac{4}{3}$  (b)  $\frac{3}{4}$  (c) 4 (d)  $\frac{1}{4}$

18 The function  $f$  where  $f(x) = a^x$  is decreasing on its domain if .....

- (a)  $a = 1$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = -1$

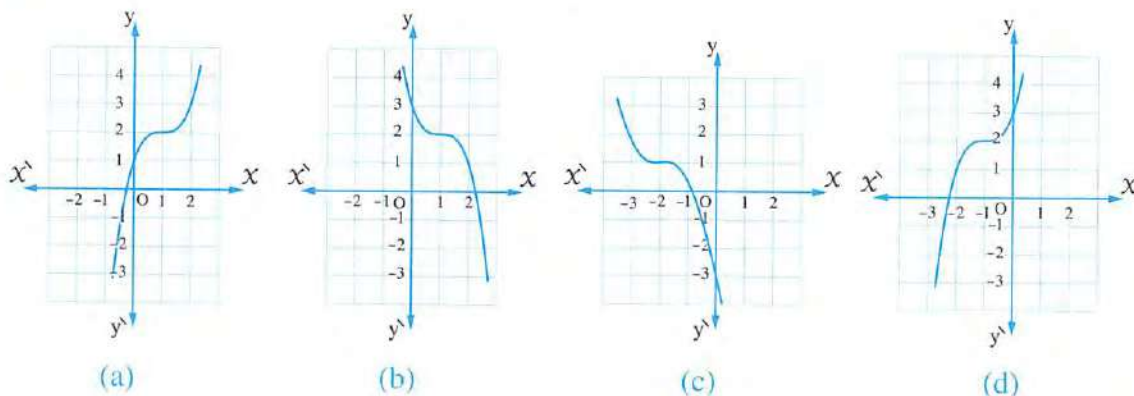
19  $\lim_{x \rightarrow 0} \frac{(4x+1)^9 - 1}{3x} = \dots\dots\dots$

- (a)  $\frac{3}{4}$  (b)  $\frac{4}{3}$  (c) 9 (d) 12

20 The solution set in  $\mathbb{R}$  of the equation :  $|x - 7| = 2$  is .....

- (a)  $\{9, 5\}$  (b)  $\{7, 3\}$  (c)  $\emptyset$  (d)  $\{3, -3\}$

21 If  $f(x) = 2 - (x-1)^3$ , then the figure that represents the function  $f$  is .....



22 If the perimeter of  $\triangle ABC = 33$  cm. ,  $\sin A + \sin C = \frac{2}{3}$  ,  $\sin B = \frac{1}{4}$  , then  $AC = \dots\dots\dots$  cm.

- (a) 6 (b) 9 (c) 12 (d) 15



**23** If  $3^{(2X+7)} = 11^X$ , then the value of  $X$  to the nearest 1 decimal place equals .....

- (a) 28.3                      (b) 38.3                      (c) 3.8                      (d) 28.4

**24**  $\lim_{x \rightarrow \infty} (5 + 3x^2 + x) = \dots\dots\dots$

- (a) not exist.                      (b) 5                      (c)  $\infty$                       (d) 9

**25** ABCD is a parallelogram,  $m(\angle A) = 50^\circ$ ,  $m(\angle DBC) = 70^\circ$ ,  $BD = 8$  cm, then the perimeter of the parallelogram ABCD to the nearest cm. = ..... cm.

- (a) 38                      (b) 30                      (c) 19                      (d) 48

**26** The solution set of the inequality  $|X - 1| \leq 3$  is .....

- (a)  $[-2, 4]$                       (b)  $]-2, 4[$                       (c)  $]-2, 4]$                       (d)  $\mathbb{R} - [-2, 4]$

**27** In  $\triangle ABC$ ,  $\cos(A + B) = \dots\dots\dots$

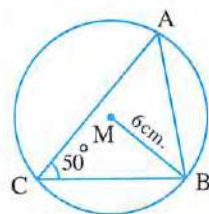
- (a)  $\cos C$                       (b)  $-\cos C$                       (c)  $\sin C$                       (d)  $-\sin C$

**28** In the opposite figure :

M is the centre of the circle

,  $BM = 6$  cm. , then  $AB = \dots\dots\dots$  cm.

- (a)  $6 \sin 50^\circ$                       (b)  $12 \sin 50^\circ$   
(c)  $6 \cos 50^\circ$                       (d)  $12 \cos 50^\circ$



## Second Essay questions

**Answer the following questions :**

**1** If  $X = 5 + 2\sqrt{6}$ , find in the simplest form the value of  $\log\left(\frac{1}{X} + X\right)$  without using calculator.

**2** Use the curve of the function  $f : f(X) = \frac{1}{X}$  to graph the curve of the function  $g : g(X) = \frac{1}{X-2} + 3$ , from the graph state the domain and range of  $g$  and the monotony and its type whether it is even, odd or otherwise.

**3** Find :  $\lim_{x \rightarrow 1} \frac{(x+2)^4 - 81}{x-1}$

**4**  $\lim_{x \rightarrow \infty} \frac{6x - 4x^3}{2 - 7x^3}$

## Model

3

Interactive test 3



## First Multiple choice questions

Choose the correct answer from the given ones :

- 1 If  $f(x) = 7^{x+1}$ , then the solution set of the equation :  $f(2x-1) + f(x-2) = 50$  in  $\mathbb{R}$  equals .....

(a)  $\{1\}$  (b)  $\{1, -1\}$  (c)  $\{1, -50\}$  (d)  $\{7, -50\}$

- 2 If  $\log 3 = x$ ,  $\log 5 = y$ , then  $\log 15 =$  .....

(a)  $xy$  (b)  $\frac{x}{y}$  (c)  $x+y$  (d)  $x-y$

- 3  $\lim_{x \rightarrow \infty} \frac{5+x^{-2}}{1+3x^{-2}} =$  .....

(a)  $\frac{1}{3}$  (b)  $\frac{5}{4}$  (c)  $\frac{5}{3}$  (d) 5

- 4 If  $f(x) = 5^x$ , then  $f(-2) =$  .....

(a) -2 (b) 5 (c)  $\frac{1}{25}$  (d)  $\frac{1}{5}$

- 5 The domain of the function  $f : f(x) = \log_3(x-2)$  is  $x >$  .....

(a) 3 (b) 5 (c) 1 (d) 2

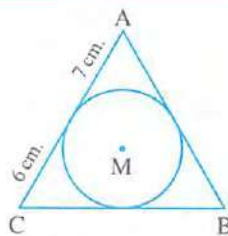
- 6  $\log 25 + \frac{\log 8 \times \log 16}{\log 64} =$  .....

(a)  $\log_2 16$  (b)  $\log_5 25$  (c)  $\log 4$  (d)  $\log 10$

- 7 In the opposite figure :

If the perimeter of  $\triangle ABC = 42$  cm. ,  
the circle touches the sides of the triangle  
internally , then :  $m(\angle B) =$  .....

(a)  $53^\circ 8'$  (b)  $67^\circ 23'$  (c)  $36^\circ 53'$  (d)  $32^\circ 37'$



- 8  $\lim_{x \rightarrow 2} \frac{x-2}{x+1} =$  .....

(a) zero (b) 1 (c) 2 (d)  $\infty$

- 9  $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2}}{x} = \dots\dots\dots$   
 (a) zero (b) 2 (c)  $\infty$  (d) 1
- 
- 10  $\lim_{x \rightarrow 5} \frac{x^2 - 8x + 15}{x^2 - 10x + 25} = \dots\dots\dots$   
 (a) does not exist. (b) zero (c) 2 (d) 3
- 
- 11 The included area between the curves of the two functions  $f : f(x) = |x + 3| - 2$ ,  $g : g(x) = \text{zero}$  is  $\dots\dots\dots$  square units.  
 (a) 2 (b) 3 (c) 4 (d) 5
- 
- 12 If  $\log_3 y = x$ , then the exponential form is  $\dots\dots\dots$   
 (a)  $y = x^3$  (b)  $x = y^3$  (c)  $x = 3^y$  (d)  $y = 3^x$
- 
- 13 If  $f$  is an odd function on  $[-x, x]$ , then  $f(-x) + f(x) = \dots\dots\dots$   
 (a)  $2x$  (b) undefined. (c)  $-2x$  (d) zero
- 
- 14 In  $\triangle ABC$ , if  $2 \sin A = 3 \sin B = 4 \sin C$ , then  $a : b : c = \dots\dots\dots$   
 (a)  $2 : 3 : 4$  (b)  $4 : 3 : 2$  (c)  $3 : 4 : 6$  (d)  $6 : 4 : 3$
- 
- 15  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^2 + 3x - 10} = \dots\dots\dots$   
 (a)  $\frac{16}{7}$  (b)  $\frac{80}{7}$  (c)  $\frac{7}{80}$  (d)  $\frac{7}{16}$
- 
- 16 The radius length of the circumcircle of the triangle ABC in which  $m(\angle A) = 30^\circ$ ,  $a = 10$  cm. equals  $\dots\dots\dots$   
 (a) 10 cm. (b) 20 cm. (c) 5 cm. (d) 40 cm.
- 
- 17 The function  $f : f(x) = \begin{cases} x^2 & , \quad x > 2 \\ -x^2 & , \quad x \leq 2 \end{cases}$  is decreasing on the interval  $\dots\dots\dots$   
 (a)  $]0, 2[$  (b)  $] - \infty, 0[$  (c)  $\mathbb{R} - [0, 2[$  (d)  $]0, \infty[$
- 
- 18 The solution set of the equation :  $\log_x 81 = 4$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\{-3\}$  (b)  $\{3\}$  (c)  $\{3, -3\}$  (d)  $\{9\}$
- 
- 19 The solution set of the equation :  $|x + 2| = -2$  in  $\mathbb{R}$  is  $\dots\dots\dots$   
 (a)  $\emptyset$  (b)  $\mathbb{R}$  (c)  $] - \infty, -2[$  (d)  $] - \infty, -2]$



- 20** The measure of the greatest angle in the triangle whose side lengths are 3 cm. , 5 cm. , 7 cm. equals .....

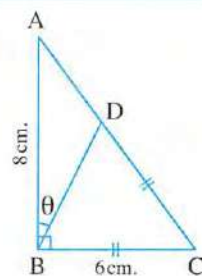
(a)  $150^\circ$  (b)  $120^\circ$  (c)  $60^\circ$  (d)  $30^\circ$

- 21** In the opposite figure :

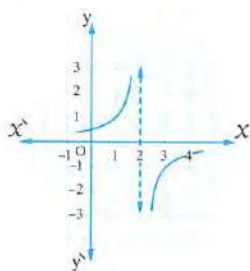
If  $CD = CB = 6$  cm.

, then  $\tan \theta = \dots\dots\dots$

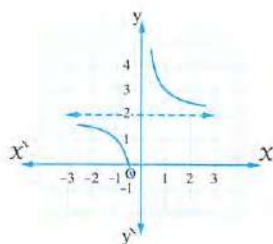
(a)  $\frac{3}{4}$  (b)  $\frac{4}{3}$   
(c)  $\frac{1}{2}$  (d) 2



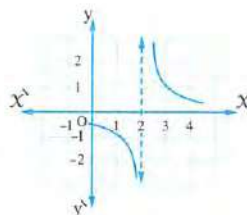
- 22** If  $f(x) = \frac{1}{x-2}$ , then the graph that represents the function  $f$  is .....



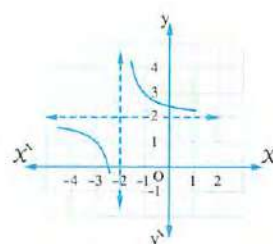
(a)



(b)



(c)

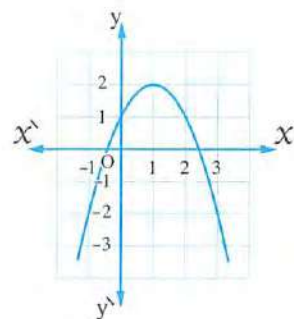


(d)

- 23** The rule of the function shown

in the opposite figure is  $f(x) = \dots\dots\dots$

(a)  $(x-2)^2 + 1$  (b)  $-(x-2)^2 + 1$   
(c)  $-(x-1)^2 + 2$  (d)  $(-x+1)^2 + 1$



- 24** In  $\triangle ABC$ ,  $a^2 + b^2 - c^2 = \dots\dots\dots$

(a)  $\cos A$  (b)  $a b \cos C$  (c)  $\cos C$  (d)  $2 a b \cos C$

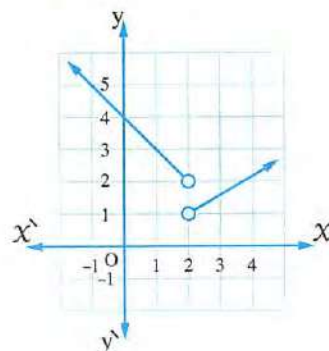
- 25** The solution set of the equation :  $x^{\frac{2}{3}} = 25$  in  $\mathbb{R}$  is .....

(a)  $\{5\}$  (b)  $\{5, -5\}$   
(c)  $\{125\}$  (d)  $\{125, -125\}$

**26** In the opposite figure :

$$\lim_{x \rightarrow 2} f(x) = \dots\dots\dots$$

- (a) zero  
(b) not exist.  
(c) 2  
(d) 1



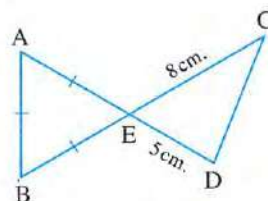
**27** The number of possible solutions of  $\Delta ABC$  in which  $a = 8$  cm. ,  $b = 10$  cm. ,  $m(\angle A) = 42^\circ$  is .....

- (a) 1                                      (b) 2                                      (c) infinite number.    (d) zero.

**28** In the opposite figure :

$CD = \dots\dots\dots$  cm.

- (a) 6                                      (b) 7  
(c) 8                                      (d) 9



## Second Essay questions

**Answer the following questions :**

**1** Prove that :  $\frac{2^x \times 9^{x+1}}{3 \times (18)^x} = 3$

**2** Graph the function  $f : f(x) = \begin{cases} |x| & , \quad x \leq 0 \\ x^3 & , \quad x > 0 \end{cases}$  , from the graph state the range of the function and discuss its monotony.

**3** Find :  $\lim_{x \rightarrow \infty} \frac{(x+1)(5x-3)}{x^2+3}$

**4**  $\lim_{x \rightarrow 2} \frac{5x-10}{4x-8}$

## Model

4

Interactive test 4



## First Multiple choice questions

Choose the correct answer from the given ones :

1  $\lim_{x \rightarrow 0} \frac{x^7 - 1}{x + 1} = \dots\dots\dots$

- (a)  $-2$  (b)  $5$  (c)  $1$  (d)  $-1$

2 In  $\Delta ABC$ ,  $\frac{b^2 + c^2 - a^2}{2bc} = \dots\dots\dots$

- (a)  $\cos A$  (b)  $\cos B$  (c)  $\cos C$  (d)  $\sin A$

3 The solution set in  $\mathbb{R}$  of the inequality :  $|x - 1| \geq 3$  equals  $\dots\dots\dots$

- (a)  $\mathbb{R} - ]-2, 4[$  (b)  $[-2, 4]$  (c)  $\mathbb{R} - [-2, 4]$  (d)  $]-2, 4[$

4  $\lim_{x \rightarrow -1} \frac{x^2 + x}{x^3 + 1} = \dots\dots\dots$

- (a) zero (b)  $-\frac{1}{3}$  (c)  $-1$  (d) does not exist.

5 The radius length of the circumcircle of  $\Delta XYZ$  in which  $X = 20 \sin X$  cm. equals  $\dots\dots\dots$  cm.

- (a)  $5$  (b)  $10$  (c)  $20$  (d)  $40$

6 Which of the following functions represents an increasing exponential function on its domain  $\mathbb{R}$  ?

- (a)  $y = 3(1.05)^x$  (b)  $y = 3\left(\frac{1}{1.05}\right)^x$  (c)  $y = 3 + (0.5)^x$  (d)  $y = (0.05)^x$

7 The solution set of the equation :  $\log_5 x = -1$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\left\{\frac{1}{10}\right\}$  (b)  $\left\{\frac{1}{50}\right\}$  (c)  $\{1\}$  (d)  $\{50\}$

8 The measure of the smallest angle in  $\Delta ABC$  in which ,  $a = 8$  cm. ,  $b = 7$  cm. , and its perimeter is 21 cm. approximately equals  $\dots\dots\dots$

- (a)  $32^\circ 34'$  (b)  $42^\circ 34'$  (c)  $36^\circ 34'$  (d)  $46^\circ 34'$



9 If  $5^X = 17$ , then the value of  $X$  to the nearest two decimals equals .....

- (a) 1.34 (b) 1.32 (c) 1.76 (d) 1.67

10  $\lim_{h \rightarrow 0} \frac{(2-3h)^7 - 128}{4h} = \dots\dots\dots$

- (a) 336 (b) -336 (c) 623 (d) -633

11 If the curve of the function  $f : f(X) = \log_4(1 - aX)$  passes through the point  $(\frac{1}{8}, -\frac{1}{2})$ , then  $a = \dots\dots\dots$

- (a) 3 (b) 2 (c) 4 (d) 8

12 The solution set of the equation :  $X^{\frac{4}{3}} = 81$  in  $\mathbb{R}$  is .....

- (a)  $\{27, -27\}$  (b)  $\{9, -9\}$  (c)  $\{9\}$  (d)  $\{27\}$

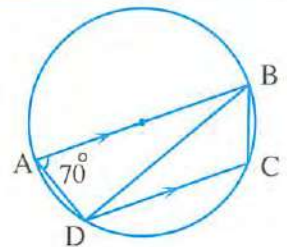
13  $\lim_{x \rightarrow \infty} \frac{(12)^{\frac{1}{x}}}{x+7} = \dots\dots\dots$

- (a)  $\frac{12}{7}$  (b)  $\infty$  (c) 1 (d) zero

14 In the opposite figure :

If  $BC = 10$  cm. , then the perimeter of  $\triangle BDC \simeq \dots\dots\dots$  cm.

- (a) 60 (b) 62  
(c) 64 (d) 67



15 If  $3^{X-2} = 2^{X-2}$ , then  $X = \dots\dots\dots$

- (a) 3 (b) -2 (c) zero (d) 2

16 The domain of the function  $f : f(X) = \frac{1}{|X|-3}$  is .....

- (a)  $\{3, -3\}$  (b)  $[-3, 3]$  (c)  $\mathbb{R} - [-3, 3]$  (d)  $\mathbb{R} - \{-3, 3\}$

17 The vertex of the curve of the function  $f : f(X) = (2-X)^2 + 3$  is .....

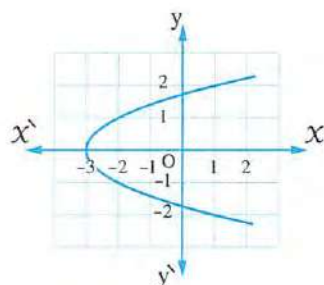
- (a) (2, 3) (b) (2, -3) (c) (-2, 3) (d) (-2, -3)

18  $\lim_{x \rightarrow 0} \frac{(2X+1)^2 - 1}{X} = \dots\dots\dots$

- (a) 4 (b) -3 (c) -4 (d) -2

- 19** The curve represented in the opposite figure is symmetric about the straight line whose equation is .....

(a)  $X = 0$  (b)  $y = 0$   
(c)  $y = -2$  (d)  $X = 2$



- 20** If  $\angle A$  supplements  $\angle C$ , then  $\cos A + \cos C = \dots\dots\dots$

(a) 1 (b) zero (c)  $\frac{1}{2}$  (d) -1

- 21**  $\lim_{x \rightarrow 0} \frac{5 + 2X}{\cos 3X} = \dots\dots\dots$

(a) 5 (b) 3 (c) 2 (d)  $\frac{5}{3}$

- 22** If  $\log_2 X = 4$ , then the exponential form that equivalent to it is .....

(a)  $2^X = 4$  (b)  $X = 2^4$  (c)  $X^2 = 4$  (d)  $4^X = 2$

- 23** If  $\frac{a+b}{13} = \frac{b+c}{11} = \frac{c+a}{12}$ , then  $\cos A = \dots\dots\dots$

(a)  $\frac{1}{5}$  (b)  $\frac{5}{7}$  (c)  $\frac{19}{35}$  (d)  $\frac{4}{11}$

- 24** The solution set of the equation :  $(\log_2 X)^2 - 2 \log_2 X = 3$  in  $\mathbb{R}$  is .....

(a)  $\{16\}$  (b)  $\{8\}$  (c)  $\{8, 0.5\}$  (d)  $\{16, 0.5\}$

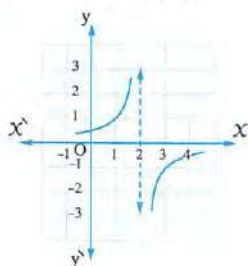
- 25** If  $g$  is a real function whose domain is  $[-2, 3]$ , then the domain of  $n : n(X) = g(X-2)$  is .....

(a)  $[-2, 3]$  (b)  $[-4, 1]$  (c)  $[0, 5]$  (d)  $\mathbb{R}$

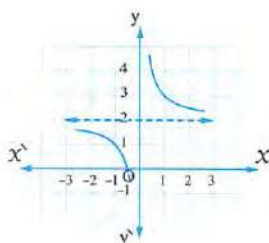
- 26** If the radius length of circumcircle of  $\triangle ABC$  equals 3 cm. and  $\sin A + \sin B + \sin C = 2$ , then the perimeter of triangle  $ABC = \dots\dots\dots$  cm.

(a) 6 (b) 9 (c) 12 (d) 24

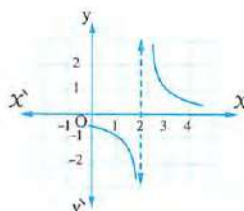
- 27** If  $f(X) = \frac{1}{X-2}$ , then the graph that represents the function  $f$  is .....



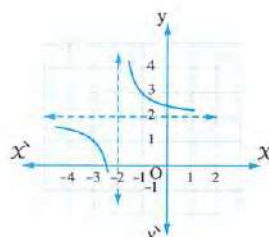
(a)



(b)



(c)



(d)

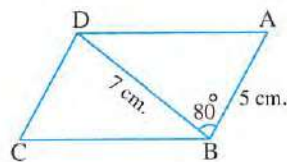
**28 In the opposite figure :**

ABCD is a parallelogram

,  $m(\angle ABD) = 80^\circ$ ,  $BD = 7$  cm.

$AB = 5$  cm. , then the perimeter of parallelogram = ..... to the nearest cm.

- (a) 25 (b) 26 (c) 29 (d) 30


**Second** **Essay questions**

**Answer the following questions :**

**1** Find :  $\lim_{x \rightarrow -2} \frac{3x^2 - 12}{x + 2}$

**2** Graph the function  $f : f(x) = \begin{cases} -x^3, & x < 0 \\ x, & x \geq 0 \end{cases}$ , from the graph find the range and its type whether it is odd, even or otherwise, and discuss its monotony.

**3** If  $f(x) = 2^x$ , find the value of  $x$  which satisfies :  $f(x+1) - f(x-1) = 24$

**4**  $\lim_{x \rightarrow \infty} \frac{4x^5 + 5}{8x^5 + x^4 - 2}$

**Model**
**5**

 Interactive test **5**

**First** **Multiple choice questions**

**Choose the correct answer from the given ones :**

**1**  $\lim_{x \rightarrow 1} \frac{x^{\frac{6}{2}} - x^{\frac{1}{2}}}{x^{\frac{3}{2}} - x^{\frac{1}{2}}} = \dots\dots\dots$

- (a)  $\frac{13}{7}$  (b) 1 (c) 2 (d)  $x$

**2** If  $5^{x+1} = 7^{x+1}$ , then  $3^{x+1} = \dots\dots\dots$

- (a) zero (b) 3 (c) 2 (d) 1

**3** If  $x < 1$ , then  $|3 - x| - |x - 4| = \dots\dots\dots$

- (a) -1 (b) 1 (c)  $2x - 7$  (d)  $7 - 2x$

**4** The solution set in  $\mathbb{R}$  of the equation :  $|2x - 4| = |x + 1|$  equals .....

- (a)  $\{1\}$  (b)  $\{5\}$  (c)  $\{1, 5\}$  (d)  $\emptyset$



**5** The domain of the function  $f : f(x) = \sqrt{x-2}$  is .....

- (a)  $\mathbb{R}$  (b)  $\{2\}$  (c)  $[2, \infty[$  (d)  $]2, \infty[$

**6**  $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2+1}}{x-2} = \dots\dots\dots$

- (a) 4 (b) 5 (c)  $-\frac{5}{2}$  (d) 2

**7** In  $\triangle ABC$ , if  $m(\angle A) = 30^\circ$ ,  $b = 15\sqrt{3}$  cm.,  $m(\angle B) = 60^\circ$ , then  $a = \dots\dots\dots$  cm.

- (a) 30 (b) 45 (c) 15 (d) 60

**8**  $\lim_{x \rightarrow \infty} (3 + 5x^2 + 3x) = \dots\dots\dots$

- (a) does not exist. (b) 5 (c)  $\infty$  (d) 11

**9** The domain of the function  $f : f(x) = 5$  is .....

- (a)  $\left\{\frac{1}{5}\right\}$  (b)  $\{5\}$  (c)  $\mathbb{R}$  (d)  $\mathbb{R} - \{5\}$

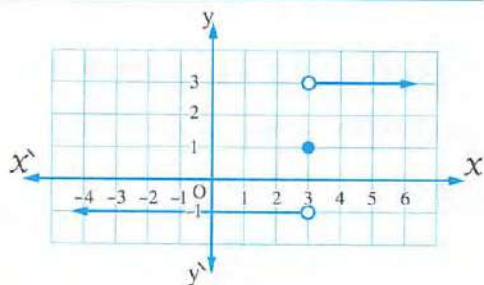
**10** If  $f(a) = 2^a$ , then  $\log_2 f(a) = \dots\dots\dots$

- (a) 2 (b)  $f(a)$  (c)  $a$  (d)  $\frac{1}{2a}$

**11** From the opposite figure :

$\lim_{x \rightarrow 3} f(x) = \dots\dots\dots$

- (a) 1 (b) 3  
(c) -1 (d) does not exist.



**12**  $\lim_{x \rightarrow 0} (2x^2 + 3) = \dots\dots\dots$

- (a) 2 (b) 3 (c) 5 (d) 7

**13** From the following functions, the even function is  $f : f(x) = \dots\dots\dots$

- (a)  $\sin x$  (b)  $\sin 30^\circ$  (c)  $x \cos x$  (d)  $x^2 + \tan x$

**14** In  $\triangle XYZ$ ,  $2x \times \dots\dots\dots = x^2 + z^2 - y^2$

- (a)  $\cos X$  (b)  $\cos Z$  (c)  $\cos Y$  (d)  $\sin Y$

15 If  $\lim_{x \rightarrow -1} \frac{x^2 + kx + m}{x^2 - 1} = 3$ , then  $k + m = \dots\dots\dots$

(a) -4

(b) -5

(c) -8

(d) -9

16 The range of the function  $f : f(x) = \frac{x^2 - 1}{x - 1}$  is  $\dots\dots\dots$

(a)  $\mathbb{R}$ (b)  $\mathbb{R} - \{0\}$ (c)  $\mathbb{R} - \{1\}$ (d)  $\mathbb{R} - \{2\}$ 

17 If  $\frac{a+b}{13} = \frac{b+c}{11} = \frac{c+a}{12}$ , then  $\cos A = \dots\dots\dots$

(a)  $\frac{1}{5}$ (b)  $\frac{5}{7}$ (c)  $\frac{19}{35}$ (d)  $\frac{4}{11}$ 

18 The number of possible solutions of the triangle ABC :  $m(\angle A) = 47^\circ$ ,  $a = 4$  cm.,  $b = 6$  cm. equals  $\dots\dots\dots$

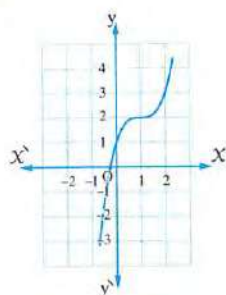
(a) 1

(b) 2

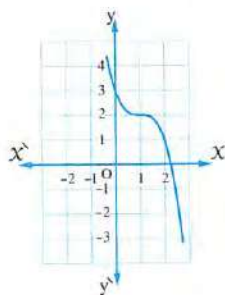
(c) 3

(d) zero

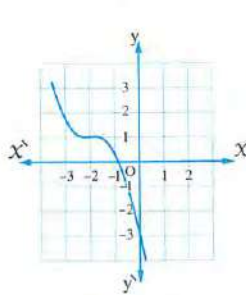
19 If  $f(x) = 2 - (x - 1)^3$ , then the graph that represents the function  $f$  is  $\dots\dots\dots$



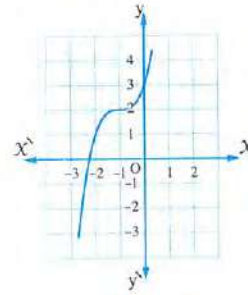
(a)



(b)



(c)



(d)

20 The S.S. of the equation :  $\log_x (x + 6) = 2$  in  $\mathbb{R}$  is  $\dots\dots\dots$

(a)  $\{3, -2\}$ (b)  $\{3\}$ (c)  $\{3, 1\}$ (d)  $\{6, 1\}$ 

21 A man deposite L.E. 12000 in a bank that gives yearly interest 13 % , then the sum of money after 10 years approximately equals L.E.  $\dots\dots\dots$

(a) 40735

(b) 38735

(c) 36049

(d) 46030

22 In  $\triangle LMN$ ,  $m(\angle L) = 30^\circ$ ,  $MN = 7$  cm., then the diameter length of the circle passing through its vertices equals  $\dots\dots\dots$

(a) 7 cm.

(b) 3.5 cm.

(c) 14 cm.

(d)  $\frac{14}{\sqrt{2}}$  cm.

23 The solution set of the equation :  $2^{x^2} = 16$  in  $\mathbb{R}$  is  $\dots\dots\dots$

(a)  $\{2\}$ (b)  $\{-2\}$ (c)  $\{2, -2\}$ (d)  $\{4, -4\}$

- 24** The curve :  $y = 3(X - 5)^2 + 7$  under action of translation 3 units in the positive direction of the  $X$ -axis and one unit in the negative direction of the  $y$ -axis is the curve .....

(a)  $y = 3(X + 8)^2 + 6$

(b)  $y = 3(X - 8)^2 + 8$

(c)  $y = 3(X - 8)^2 + 6$

(d)  $y = 3(X + 8)^2 - 6$

- 25** In the opposite figure :

$BC = 7$  cm. ,  $m(\angle A) = 120^\circ$  ,  $AB < AC$

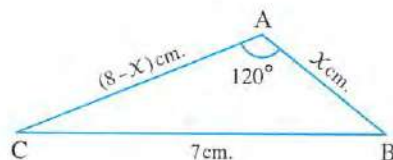
, then  $AC = \dots\dots\dots$  cm.

(a) 5

(b) 3

(c) 8

(d) 4



- 26** The simplest form of the expression :  $\frac{1}{\log_x X y z} + \frac{1}{\log_y X y z} + \frac{1}{\log_z X y z} = \dots\dots\dots$

(a)  $z$

(b)  $y$

(c) 1

(d)  $X$

- 27** In any triangle  $XYZ$  ,  $XY : YZ = \dots\dots\dots$

(a)  $\sin X : \sin Y$

(b)  $\sin Y : \sin Z$

(c)  $\sin Z : \sin X$

(d)  $\sin Z : \sin Y$

- 28** If the curve  $y = f(X)$  represents a real function , then its image by translation 5 units vertically downward is  $g(X) = \dots\dots\dots$

(a)  $f(X - 5)$

(b)  $f(X + 5)$

(c)  $f(X) + 5$

(d)  $f(X) - 5$

## Second

## Essay questions

**Answer the following questions :**

- 1** Showing steps , find the solution set of the equation :

$3^{2X-1} - 4 \times 3^X + 9 = 0$  , where  $X$  is a real number.

- 2** If the function  $f : f(X) = \frac{1}{X}$  , then find the domain of the function  $f$  and the coordinates of the symmetric point of the curve of this function , then find in  $\mathbb{R}$  the solution set of the equation :  $f\left(\frac{1}{X}\right) = 4$

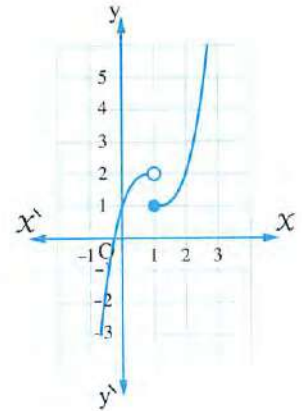
- 3** Find :  $\lim_{x \rightarrow 0} \frac{\sqrt{x+4} - 2}{x}$



**4** Study the opposite figure , then find :

(1)  $f(1)$

(2)  $\lim_{x \rightarrow 1} f(x)$



**Model**

**6**

Interactive test **6**



**First**

**Multiple choice questions**

Choose the correct answer from the given ones :

**1** If  $\lim_{x \rightarrow 4} \frac{x^2 + 7x + b}{x^2 - 6x + 8} = \frac{15}{2}$ , then  $b = \dots\dots\dots$

- (a) -44                      (b) 7                      (c) -8                      (d) 8

**2** The vertex point of the curve of the function  $f : f(x) = x^2 + 3$  is  $\dots\dots\dots$

- (a) (3, 0)                      (b) (0, 3)                      (c) (-3, 0)                      (d) (0, -3)

**3** If  $\log_a(x+2) - \log_a(x-1) = \log_a 4$ , then  $x = \dots\dots\dots$

- (a) -2                      (b) 2                      (c) 1                      (d) -1

**4** All the functions defined by the following rules are odd except  $\dots\dots\dots$

- (a)  $f(x) = \tan x$                       (b)  $f(x) = \csc x$                       (c)  $f(x) = 7x^3$                       (d)  $f(x) = \cos x$

**5**  $\lim_{x \rightarrow 0} \frac{x^2 - 1}{x} = \dots\dots\dots$

- (a) zero                      (b) 1                      (c) does not exist.                      (d) -1

**6** If  $x^{\frac{3}{2}} = 64$ , then  $x = \dots\dots\dots$

- (a) 512                      (b) 16                      (c) 4                      (d) 2

**7** The area of the circle passing through the vertices of the equilateral triangle ABC whose side length is 9 cm. equals  $\dots\dots\dots \text{cm}^2$

- (a)  $9\pi$                       (b)  $9\sqrt{3}\pi$                       (c)  $27\pi$                       (d)  $81\pi$

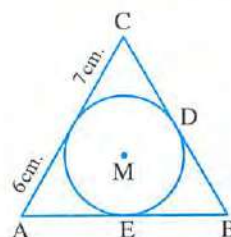
- 8** If  $f(x) = 3^x$ , then the solution set in  $\mathbb{R}$  of the equation :  $f(x-2) + f(x-1) = 36$  equals .....
- (a)  $\{9\}$  (b)  $\{4\}$  (c)  $\{2\}$  (d)  $\{3\}$
- 
- 9**  $\lim_{h \rightarrow 0} \frac{(x+h)^7 - x^7}{h} = \dots\dots\dots$
- (a)  $x^7$  (b)  $7x^6$  (c) zero (d) 1
- 
- 10** In  $\triangle ABC$ ,  $a^2 + b^2 - c^2 = \dots\dots\dots$
- (a)  $\cos A$  (b)  $ab \cos C$  (c)  $\cos C$  (d)  $2ab \cos C$
- 
- 11** The curve  $g(x) = |x+3|$  is the same as the curve  $f(x) = |x|$  by translation 3 units in the direction of .....
- (a)  $\overrightarrow{OX}$  (b)  $\overrightarrow{OX}$  (c)  $\overrightarrow{Oy}$  (d)  $\overrightarrow{Oy}$
- 
- 12** The solution set of the inequality :  $|3 - 2x| \leq 1$  in  $\mathbb{R}$  is .....
- (a)  $[1, 2]$  (b)  $]1, 2[$  (c)  $\mathbb{R} - ]1, 2[$  (d)  $\mathbb{R} - [1, 2]$
- 
- 13** If  $(2, 3)$  lies on the curve of an odd function, then the point ..... lies on the curve of the same function.
- (a)  $(-2, -3)$  (b)  $(2, -3)$  (c)  $(-2, 3)$  (d)  $(3, 2)$
- 
- 14** The point of symmetry of the function  $f : f(x) = \frac{2x-1}{x}$  is .....
- (a)  $(1, 1)$  (b)  $(2, 1)$  (c)  $(1, 2)$  (d)  $(0, 2)$
- 
- 15**  $\lim_{x \rightarrow 1} \frac{2x-4}{x-2} = \dots\dots\dots$
- (a) 1 (b) 2 (c) -2 (d) zero
- 
- 16** The range of the function  $f : f(x) = \frac{5}{x} + 2$  is .....
- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{2\}$  (c)  $\{2\}$  (d)  $\mathbb{R} - \{0\}$
- 
- 17** The range of the function  $f : f(x) = \begin{cases} 0 & , \quad x \leq 0 \\ 1 & , \quad x > 0 \end{cases}$  is .....
- (a)  $\{1\}$  (b)  $\{0\}$  (c)  $\mathbb{R}$  (d)  $\{0, 1\}$

- 18** The radius length of the circumcircle of the triangle XYZ in which :  
 $x = 3$  cm. ,  $y = 5$  cm. ,  $z = 7$  cm. approximately equals ..... cm.  
 (a) 6 (b) 8 (c) 4 (d) 2

- 19** In the opposite figure :

If the perimeter of  $\triangle ABC = 42$  cm. and the circle M is the inscribed circle in it , then  $m(\angle A) = \dots\dots\dots$

- (a)  $53^\circ 7'$  (b)  $67^\circ 23'$   
 (c)  $36^\circ 53'$  (d)  $22^\circ 37'$



- 20** If  $5^{x-3} = 4^{3-x}$  , then  $x = \dots\dots\dots$

- (a)  $\frac{5}{4}$  (b) 3 (c)  $\frac{4}{5}$  (d) zero

- 21** The numerical value of the expression  $\frac{\log 64}{\log 8}$  equals .....

- (a) 2 (b) 8 (c) 80 (d) 72

- 22** In  $\triangle DEF$  ,  $m(\angle D) = 80^\circ$  ,  $m(\angle E) = 60^\circ$  , if  $f = 12$  cm. , then  $d = \dots\dots\dots$  cm.

- (a)  $\frac{12 \sin 80^\circ}{\sin 40^\circ}$  (b)  $\frac{12 \sin 80^\circ}{\sin 60^\circ}$  (c)  $\frac{12 \sin 40^\circ}{\sin 80^\circ}$  (d)  $\frac{12 \cos 80^\circ}{\cos 40^\circ}$

- 23**  $\lim_{x \rightarrow \infty} \frac{(2x+1)(4x-1)^2}{(2x+3)^3} = \dots\dots\dots$

- (a) 4 (b) 32 (c) 1 (d) 8

- 24** If  $\lim_{x \rightarrow 1} \frac{b}{x+1} = 5$  , then  $b = \dots\dots\dots$

- (a) 5 (b) -1 (c) 1 (d) 10

- 25** In  $\triangle ABC$  , if  $b^2 = (c-a)^2 + ca$  , then  $m(\angle B) = \dots\dots\dots$

- (a)  $30^\circ$  (b)  $60^\circ$  (c)  $90^\circ$  (d)  $120^\circ$

- 26** The absolute inequality that represents mark of a student from 50 to 70 marks is .....

- (a)  $|x - 20| < 10$  (b)  $|x - 60| < 10$   
 (c)  $|x - 60| \leq 10$  (d)  $|x - 20| \leq 10$

- 27** In  $\triangle ABC$  ,  $\cos(A+B) = \dots\dots\dots$

- (a)  $\frac{a^2 + b^2 - c^2}{2ab}$  (b)  $\frac{a^2 + c^2 - b^2}{2ab}$  (c)  $\frac{b^2 + c^2 - a^2}{2bc}$  (d)  $\frac{c^2 - a^2 - b^2}{2ab}$



**28 In the opposite figure :**

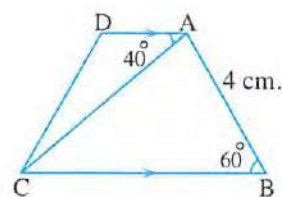
$\overline{AD} \parallel \overline{BC}$ ,  $AB = 4$  cm. ,  $m(\angle DAC) = 40^\circ$  ,  $m(\angle B) = 60^\circ$   
 , then the length of  $\overline{AC} \approx \dots\dots\dots$  cm.

(a) 5

(b) 3

(c) 2

(d) 4

**Second Essay questions**

**Answer the following questions :**

- 1** Graph the curve of the function  $f : f(x) = |x + 2| + 1$  and deduce its range and discuss its monotonicity and its type whether it is even , odd or otherwise.

- 2** Find :  $\lim_{x \rightarrow \infty} (\sqrt{x^2 + 5x} - x)$

- 3** Without using calculator find the value of :

$$\log_2 \frac{3}{25} + 5 \log_2 5 + \log_2 27 - \log_2 \frac{125}{12} - \log_2 243$$

- 4** Find :  $\lim_{x \rightarrow 0} \frac{x^2}{3x^3 - 2x^2}$

**Model****7**Interactive test **7****First Multiple choice questions**

Choose the correct answer from the given ones :

- 1** The range of the function  $f : f(x) = |x|$  is .....

(a)  $[0, \infty[$ (b)  $]0, \infty[$ (c)  $]-\infty, 0]$ (d)  $]-\infty, 0[$ 

- 2** In  $\Delta ABC$  ,  $\frac{a}{a+b} = \frac{\sin A}{\dots\dots\dots}$

(a)  $\sin B$ (b)  $\sin C$ (c)  $\sin A + \sin B$ (d)  $\sin A + \sin C$ 

- 3** In  $\Delta ABC$  , if  $\sin A = 2 \sin C$  ,  $BC = 6$  cm. , then  $AB = \dots\dots\dots$  cm.

(a) 2

(b) 3

(c) 4

(d) 6

- 4** The solution set in  $\mathbb{R}$  of the equation :  $x^{\frac{4}{3}} - 10x^{\frac{2}{3}} + 9 = 0$
- (a)  $\{1, 27\}$  (b)  $\{-1, 1\}$   
 (c)  $\{-1, 1, 27\}$  (d)  $\{-1, 1, -27, 27\}$
- 
- 5**  $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\tan x}{x} = \dots\dots\dots$
- (a)  $\frac{\pi}{2}$  (b)  $\frac{4}{\pi}$  (c) 1 (d) does not exist.
- 
- 6** If  $\sqrt[3]{x^2} = 4$ , then  $x = \dots\dots\dots$
- (a) 8 (b) -8 (c)  $\pm 8$  (d)  $\pm 4$
- 
- 7** In  $\Delta ABC$ ,  $b^2 + c^2 - a^2 = 2bc \times \dots\dots\dots$
- (a)  $\sin(90^\circ - B)$  (b)  $\sin(90^\circ - A)$  (c)  $\cos B$  (d)  $\cos(90^\circ - B)$
- 
- 8**  $\lim_{x \rightarrow 1} \frac{4 - \sqrt{x+15}}{1 - x^2} = \dots\dots\dots$
- (a) 16 (b) -16 (c)  $\frac{1}{16}$  (d)  $-\frac{1}{16}$
- 
- 9** If the radius length of the circle passing through the vertices of  $\Delta ABC$  equals 6 cm, then  $\frac{2a}{\sin A} = \dots\dots\dots$  cm.
- (a) 12 (b) 6 (c) 18 (d) 24
- 
- 10** The solution set of the equation :  $(\log_5 y)^2 - 7\log_5 y + 12 = 0$  in  $\mathbb{R}$  is  $\dots\dots\dots$
- (a)  $\{25, 125\}$  (b)  $\{25, 625\}$  (c)  $\{\frac{1}{25}, 625\}$  (d)  $\{125, 625\}$
- 
- 11** The solution set of the equation :  $|x| + 3 = 0$  in  $\mathbb{R}$  is  $\dots\dots\dots$
- (a)  $\{3\}$  (b)  $\{-3\}$  (c)  $\{0\}$  (d)  $\emptyset$
- 
- 12** If  $\lim_{x \rightarrow 1} \frac{x^2 - k^2}{x + 2} = -1$ , then  $k = \dots\dots\dots$
- (a) 2 (b) -2 (c) 4 (d)  $\pm 2$
- 
- 13** If  $f$  is an odd function, then  $\frac{5f(x) + 2f(-x)}{4f(x)} = \dots\dots\dots$
- (a)  $\frac{7}{4}$  (b)  $\frac{3}{4}$  (c)  $\frac{1}{2}$  (d)  $\frac{5}{4}$
- 
- 14** In  $\Delta XYZ$ ,  $x = 5$  cm.,  $y = 7$  cm.,  $m(\angle Z) = 65^\circ$ , then  $z$  approximately equals  $\dots\dots\dots$  cm.
- (a) 7.6 (b) 6.7 (c) 7.8 (d) 8.7

**15** If  $\log_2 X = 3$ , then  $\log_X 2 = \dots\dots\dots$

(a) 2

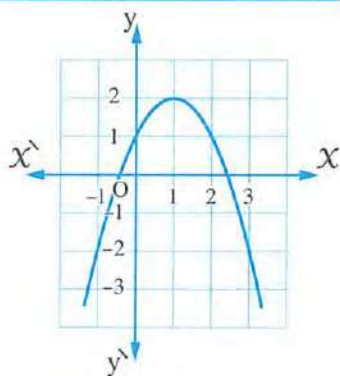
(b)  $\frac{1}{3}$ 

(c) 8

(d) 9

**16** The rule of the function represented in the opposite

figure is  $f(X) = \dots\dots\dots$

(a)  $(X-2)^2 + 1$ (b)  $-(X-2)^2 + 1$ (c)  $-(X-1)^2 + 2$ (d)  $(-X+1)^2 + 2$ 

**17** The solution set of the equation :  $|2X - 1| = 5$  in  $\mathbb{R}$  is  $\dots\dots\dots$

(a)  $\{3\}$ (b)  $\{-2\}$ (c)  $\emptyset$ (d)  $\{3, -2\}$ 

**18** If  $f(X) = \begin{cases} X-4 & , & X \geq 4 \\ g(X) & , & X < 4 \end{cases}$  is symmetric about the straight line  $X = 4$

, then the function  $g$  is  $\dots\dots\dots$

(a) an increasing function.

(b) a decreasing function.

(c) an even function.

(d) a constant function.

**19**  $\lim_{x \rightarrow 0} \frac{3X + 2X^{-1}}{X + 4X^{-1}} = \dots\dots\dots$

(a)  $\frac{1}{4}$ (b)  $\frac{1}{2}$ 

(c) 2

(d) 4

**20** The domain of the function  $f : f(X) = \frac{X+2}{X^2-9}$  is  $\dots\dots\dots$

(a)  $\{3, -3\}$ (b)  $\mathbb{R} - \{3, -3\}$ (c)  $\mathbb{R} - \{3\}$ (d)  $\mathbb{R}$ 

**21**  $\lim_{x \rightarrow \infty} \left( \frac{1}{X-2} + 1 \right) = \dots\dots\dots$

(a) 2

(b) 1

(c) zero

(d)  $\infty$ 

**22** The solution set in  $\mathbb{R}$  of the equation :  $\sqrt{X^2 - 6X + 9} = 9$  is  $\dots\dots\dots$

(a)  $\{-6, 12\}$ (b)  $\{12\}$ (c)  $\{-6\}$ (d)  $\{6, -12\}$ 

**23** If the curve of the function  $f : f(X) = \log_4(1 - aX)$  passes through  $\left(\frac{1}{8}, -\frac{1}{2}\right)$ , then  $a = \dots\dots\dots$

(a) 3

(b) 2

(c) 4

(d) 8



**24** In  $\Delta ABC$ , if  $b = c$ , then  $\cos C = \dots\dots\dots$

- (a)  $\frac{a}{2b}$  (b)  $\frac{b}{2c}$  (c)  $\frac{2b}{c}$  (d)  $\frac{2b}{a}$

**25** The solution set of the inequality  $|2x + 3| \leq 7$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $]-5, 2[$  (b)  $]-2, 5[$  (c)  $[-2, 5]$  (d)  $[-5, 2]$

**26**  $\lim_{x \rightarrow \frac{\pi}{2}} (1 - \cos x + \sin x) = \dots\dots\dots$

- (a)  $-1$  (b)  $2$  (c)  $1$  (d) zero

**27**  $\Delta ABC$  in which  $a = 4$  cm.,  $b = 4\sqrt{3}$  cm.,  $c = 8$  cm., then sine of the smallest angle measure in it =  $\dots\dots\dots$

- (a)  $\frac{1}{2}$  (b)  $\frac{\sqrt{3}}{2}$  (c)  $1$  (d) zero

**28** In  $\Delta ABC$ , if  $m(\angle C) = 60^\circ$ ,  $a^2 + b^2 - c^2 = k ab$ , then  $k = \dots\dots\dots$

- (a)  $\frac{1}{2}$  (b)  $2$  (c)  $1$  (d)  $-1$

## Second Essay questions

**Answer the following questions :**

**1** Without using the calculator, find the value of :

$$\log_2 \frac{3}{25} + 5 \log_2 5 + \log_2 27 - \log_2 \frac{125}{12} - \log_2 243$$

**2** Find :  $\lim_{x \rightarrow \infty} \frac{2x - 3}{\sqrt[3]{125x^3 + 5}}$

**3** Graph the function  $f : f(x) = \begin{cases} x^2, & x < 0 \\ x, & x \geq 0 \end{cases}$  and determine the range and monotonicity.

**4**  $\lim_{x \rightarrow 0} \frac{(x+2)^2 - 4}{x^2 + x}$

## Model

8

Interactive test 8



## First Multiple choice questions

Choose the correct answer from the given ones :

1 If  $\log_2 X = 3$ , then  $X = \dots\dots\dots$ 

- (a) 6 (b) 2 (c) 9 (d) 8

2  $\lim_{x \rightarrow 0} \sqrt{64 + x^2} = \dots\dots\dots$ 

- (a) 64 (b) 16 (c) 8 (d) otherwise.

3 The diameter length of the circle inscribed in an equilateral triangle whose side length is  $4\sqrt{3}$  cm. equals  $\dots\dots\dots$  cm.

- (a)  $2\sqrt{3}$  (b)  $4\sqrt{3}$  (c) 4 (d) 8

4 If  $y = f(X)$  is a real function, then its image by translation 2 units right is  $g(X) = \dots\dots\dots$ 

- (a)  $f(X-2)$  (b)  $f(X+2)$  (c)  $f(X)+2$  (d)  $f(X)-2$

5 The number of possible solutions of  $\triangle ABC$  where  $m(\angle A) = 60^\circ$ ,  $b = 3$  cm,  $a = 5$  cm. is  $\dots\dots\dots$ 

- (a) 1 (b) 2  
(c) no solution. (d) an infinite number of triangles.

6  $\lim_{x \rightarrow \text{zero}} \frac{x^2 + x}{x} = \dots\dots\dots$ 

- (a) zero (b) 1 (c) 2 (d) 3

7 If  $f(X) = 5^X$ , then the solution set in  $\mathbb{R}$  of the equation :  $f(X) + f(X-1) = 150$  equals  $\dots\dots\dots$ 

- (a)  $\{3\}$  (b)  $\{5\}$  (c)  $\{2\}$  (d)  $\{3, 5\}$

8 In  $\triangle ABC$ ,  $\cos(A+B) = \dots\dots\dots$ 

- (a)  $\frac{a^2 + b^2 - c^2}{2ab}$  (b)  $\frac{a^2 + c^2 - b^2}{2ac}$  (c)  $\frac{b^2 + c^2 - a^2}{2bc}$  (d)  $\frac{c^2 - a^2 - b^2}{2ab}$

9 The vertex point of the curve of  $f : f(X) = X^2 + 1$  is  $\dots\dots\dots$ 

- (a) (1, 0) (b) (-1, 0) (c) (0, 1) (d) (0, -1)

10  $\lim_{x \rightarrow 3} \frac{x^2 - 7x + 12}{x - 3} = \dots\dots\dots$

- (a) 1 (b) -1 (c) -2 (d) 7

11 The domain of the function  $f : f(x) = \frac{3}{\sqrt{x+4}}$  equals  $\dots\dots\dots$

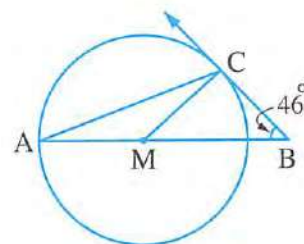
- (a)  $[-4, \infty[$  (b)  $]-\infty, 4]$  (c)  $]-4, \infty[$  (d)  $]-\infty, -4[$

12 In the opposite figure :

If  $AC = 20$  cm.

, then the perimeter of  $\triangle ACM \simeq \dots\dots\dots$  cm.

- (a) 41.6 (b) 43.5  
(c) 45 (d) 47.5



13  $\log 2 + \log 5 = \dots\dots\dots$

- (a) 1 (b)  $\log 7$  (c) 10 (d)  $\log 5$

14 The domain of the function  $f : f(x) = \sqrt{9-x}$  is  $\dots\dots\dots$

- (a)  $\mathbb{R}$  (b)  $\mathbb{R} - \{9\}$  (c)  $]-\infty, 9]$  (d)  $[9, \infty[$

15 In  $\triangle ABC$ ,  $c = 19$  cm. ,  $m(\angle A) = 112^\circ$  ,  $m(\angle B) = 33^\circ$  , then the area of  $\triangle ABC$  to the nearest  $\text{cm}^2$  equals  $\dots\dots\dots \text{cm}^2$

- (a) 64 (b) 128 (c) 185 (d) 159

16 The solution set of the inequality :  $|x| - 1 > 0$  in  $\mathbb{R}$  is  $\dots\dots\dots$

- (a)  $\mathbb{R} - [-1, 1]$  (b)  $]-1, 1[$  (c)  $\mathbb{R} - ]-1, 1[$  (d)  $[-1, 1]$

17  $\lim_{x \rightarrow -2} \left| \frac{1}{x} \right| = \dots\dots\dots$

- (a) 1 (b) -1 (c)  $-\frac{1}{2}$  (d)  $\frac{1}{2}$

18  $\lim_{x \rightarrow \infty} \left( \frac{3x^2 + 2x + 1}{x^2 - 3x + 2} \right)^4 = \dots\dots\dots$

- (a) 3 (b) 9 (c) 27 (d) 81

19 Which of the following does not equal  $(\sqrt[5]{x^4})$  ?

- (a)  $(\sqrt[5]{x})^4$  (b)  $\sqrt[4]{x^5}$  (c)  $x^{\frac{4}{5}}$  (d)  $(x^{\frac{1}{5}})^4$



**20** If the function  $f$  is even in  $[c, d]$ , then  $c + d = \dots\dots\dots$

- (a)  $2c$  (b)  $2d$  (c)  $c - d$  (d) zero

**21** If  $\sqrt[3]{x^2} = 9$ , then  $x \in \dots\dots\dots$

- (a)  $\{27\}$  (b)  $\{27, -27\}$  (c)  $\{1\}$  (d)  $\emptyset$

**22** If  $\left(\frac{1}{2}\right)^{a^2 - a - 2} = 1$ , where  $a > \text{zero}$ , then  $a = \dots\dots\dots$

- (a) 1 (b)  $-3$  (c) 2 (d) 3

**23** Which of the functions defined by the following rules represents an exponential function increasing on its domain  $\mathbb{R}$ ?

- (a)  $y = 3(1.05)^x$  (b)  $y = \frac{1}{3}\left(\frac{1}{1.5}\right)^x$  (c)  $y = 3 + (0.5)^x$  (d)  $y = (0.5)^x$

**24** In  $\Delta ABC$ , if  $2 \sin A = 3 \sin B = 4 \sin C$ , then  $a : b : c = \dots\dots\dots$

- (a)  $2 : 3 : 4$  (b)  $4 : 3 : 2$  (c)  $3 : 4 : 6$  (d)  $6 : 4 : 3$

**25** If  $\lim_{x \rightarrow a} \frac{ax}{3} = 12$ , then  $a = \dots\dots\dots$

- (a)  $\pm 12$  (b)  $\pm 6$  (c) 4 (d)  $\frac{1}{6}$

**26** If  $|x| + |x - 3| = 3$ , then  $x(x - 3) \dots\dots\dots \text{zero}$

- (a)  $<$  (b)  $>$  (c)  $\leq$  (d)  $\geq$

**27** In  $\Delta XYZ$ , if  $X = y$ , then  $\cos X = \dots\dots\dots$

- (a)  $\frac{2y^2}{z}$  (b)  $\frac{z}{2y}$  (c)  $\frac{z}{4x}$  (d)  $\frac{y}{2x}$

**28** The perimeter of  $\Delta ABC$ , in which  $b = 11 \text{ cm.}$ ,  $m(\angle A) = 67^\circ$ ,  $m(\angle C) = 46^\circ$  equals  $\dots\dots\dots$  (to the nearest cm.)

- (a) 22 (b) 38 (c) 31 (d) 27

## Second Essay questions

**Answer the following questions :**

**1** Without using the calculator find the value of :

$$\log_3 54 - \log_3 \frac{8}{15} + \log_3 \frac{4}{5}$$

**2 Find :**  $\lim_{x \rightarrow 5} \frac{x^2 - 5x}{\sqrt{x+4} - 3}$

**3** Graph the curve of the function  $f : f(x) = (x+2)^3 + 1$  and from the graph deduce the range and its monotony and its type whether it is even, odd or otherwise.

**4**  $\lim_{x \rightarrow \infty} \frac{5x^{-3} + 4x^{-2} - 3}{7x^{-3} - 2x^{-2} + 8}$

**Model**

**9**

Interactive test **9**



### First Multiple choice questions

Choose the correct answer from the given ones :

**1** The solution set of the equation :  $\log_{(x+3)} 125 = 3$  in  $\mathbb{R}$  is .....

- (a)  $\{5\}$  (b)  $\{3\}$  (c)  $\emptyset$  (d)  $\{2\}$

**2**  $\Delta LMN$  in which  $m(\angle L) = 30^\circ$ ,  $m = 9$  cm. has two solutions when  $l = \dots$  cm.

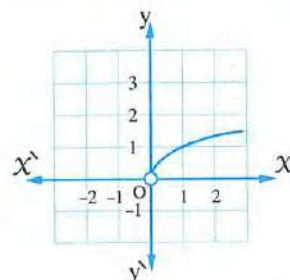
- (a) 6 (b) 10 (c) 11 (d) 2

**3** If  $4 = \log_2 x$ , then the equivalent exponential form is .....

- (a)  $x^2 = 4$  (b)  $x^4 = 2$  (c)  $x = 2^4$  (d)  $2^x = 4$

**4** The domain of the function represented by the opposite figure is .....

- (a)  $[0, \infty[$  (b)  $]0, \infty[$   
(c)  $] -\infty, 0[$  (d)  $]0, 3[$



**5** If  $f : \mathbb{R} \rightarrow \mathbb{R}$  where  $f(x+1) - f(x) = x - 1$ , then  $f(10) - f(9) = \dots$

- (a) 1 (b) 9 (c) 8 (d) 18

**6**  $\lim_{x \rightarrow 0} \frac{x^2 + x}{x^3 + x} = \dots$

- (a)  $\frac{2}{3}$  (b) 1 (c) zero (d) does not exist.

**7** The image of the curve  $f(x) = |x| - 5$  by translation 3 units in the direction of  $\overrightarrow{OX}$  and 5 units in the direction of  $\overrightarrow{Oy}$  is .....

(a)  $g(x) = |x - 3| + 5$

(b)  $g(x) = |x - 3|$

(c)  $g(x) = |x - 3| - 10$

(d)  $g(x) = |x + 3|$

**8**  $\lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 + 7} + 3x}{2x + 9} = \dots\dots\dots$

(a)  $\frac{3}{2}$

(b)  $\frac{5}{2}$

(c)  $\frac{5}{4}$

(d)  $\frac{5}{9}$

**9** The solution set of the inequality :  $|x - 1| < -2$  in  $\mathbb{R}$  is .....

(a)  $] -1, 3[$

(b)  $\mathbb{R} - [-1, 3]$

(c)  $] -2, 2[$

(d)  $\emptyset$

**10** In  $\triangle ABC$ ,  $c(a \cos B + b \cos A) = \dots\dots\dots$

(a)  $a^2$

(b)  $b^2$

(c)  $c^2$

(d)  $2c^2$

**11** ABCD is a parallelogram in which :  $AB = 9$  cm. ,  $BC = 13$  cm. ,  $AC = 20$  cm. , then the length of  $\overline{BD}$  equals ..... cm.

(a) 10

(b) 5

(c) 18.5

(d) 20

**12** If the domain of the function  $f : f(x) = \frac{2}{x^2 - 6x + k}$  is  $\mathbb{R} - \{3\}$ , then  $k = \dots\dots\dots$

(a) 3

(b) -3

(c) 9

(d)  $\pm 9$

**13**  $\lim_{x \rightarrow 4} \frac{x^3 - 64}{x - 4} = \dots\dots\dots$

(a) 96

(b) 48

(c) 32

(d) 16

**14** If  $f(x) = \frac{\sqrt{x^2 - 2x + 1}}{x - 1}$ , then the range of the function  $f$  is .....

(a)  $\{1\}$

(b)  $\mathbb{R}$

(c)  $[-1, 1[$

(d)  $\{-1, 1\}$

**15** The solution set of the following equation in  $\mathbb{R}$  :  $\log_2 x - \frac{3}{\log_2 x} = 2$  equals .....

(a)  $\{\frac{1}{2}\}$

(b)  $\{8, 2\}$

(c)  $\{8, \frac{1}{2}\}$

(d)  $\{2\}$

**16**  $\lim_{h \rightarrow 0} \frac{(x+h)^9 - x^9}{h} = \dots\dots\dots$

(a)  $x^9$

(b)  $9x^8$

(c) zero

(d) does not exist.

**17**  $\log_3 15 - \log_3 5 = \dots\dots\dots$

(a) 3

(b) 1

(c) zero

(d) -3



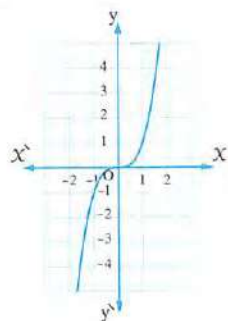
- 18** If ABC is a triangle in which  $a = 4$  cm. ,  $b = 4\sqrt{3}$  cm. ,  $c = 8$  cm. , then sine of its smallest angle equals .....

(a)  $\frac{1}{2}$  (b)  $\frac{\sqrt{3}}{2}$  (c) 1 (d) zero

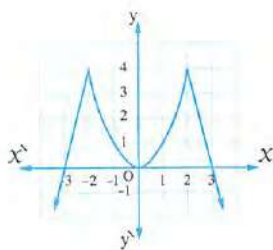
- 19** If  $x = 5 + 2\sqrt{6}$  , then  $\log\left(\frac{1}{x} + x\right) = \dots\dots\dots$

(a) 1 (b)  $5 - 2\sqrt{6}$  (c) 10 (d)  $5 + 2\sqrt{6}$

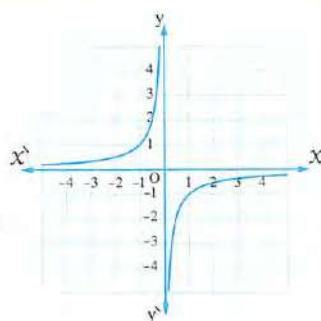
- 20** Which of the functions represented graphically as follows is neither even nor odd ?



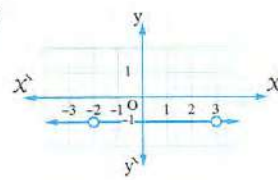
(a)



(b)



(c)

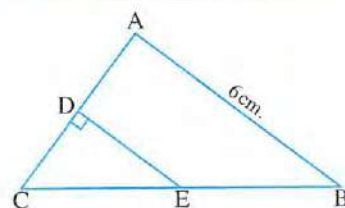


(d)

- 21** In the opposite figure :

If  $\tan(\angle DEC) = \frac{3}{4}$  , then the radius length of the circumcircle of  $\triangle ABC = \dots\dots\dots$  cm.

(a) 9 (b) 5.7  
(c)  $4\frac{3}{4}$  (d) 3.75



- 22** The solution set of the equation :  $\frac{1}{\log_2 x} + \frac{1}{\log_3 x} = 2$  is .....

(a)  $\{\sqrt{6}\}$  (b)  $\{-\sqrt{6}\}$  (c)  $\{\sqrt{6}, -\sqrt{6}\}$  (d)  $\{6\}$

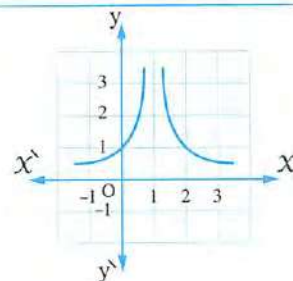
- 23** If  $\sqrt[3]{x^2} = 9$  , then  $x \in \dots\dots\dots$

(a)  $\{-81, 81\}$  (b)  $\{-27, 27\}$  (c)  $\{-9, 9\}$  (d)  $]3, 7[$

- 24** In the opposite figure :

$f(x) = \dots\dots\dots$

(a)  $\frac{1}{x-1}$  (b)  $\frac{1}{|x-1|}$   
(c)  $|x^2 - 1|$  (d)  $|x - 1|^2$



**25**  $\lim_{x \rightarrow \infty} (x - \sqrt{x^2 + 5x}) = \dots\dots\dots$

(a) 2

(b) 3

(c)  $\frac{-5}{2}$

(d)  $\frac{1}{4}$

**26** In  $\triangle XYZ$ , if  $\sin X = 2 \sin Z$ ,  $YZ = 6$  cm., then the length of  $\overline{XY} = \dots\dots\dots$  cm.

(a) 12

(b) 2

(c) 6

(d) 3

**27** In  $\triangle ABC$ , if  $a = 4$  cm.,  $b = 7$  cm.,  $m(\angle C) = 120^\circ$ , then the area of the triangle =  $\dots\dots\dots \text{cm}^2$

(a)  $7\sqrt{3}$

(b)  $14\sqrt{3}$

(c) 7

(d) 14

**28** In any triangle  $ABC$ ,  $\cos A = \dots\dots\dots$

(a)  $-(\cos B + \cos C)$

(b)  $\cos B - \cos C$

(c)  $\cos(B + C)$

(d)  $-\cos(B + C)$

## Second

## Essay questions

**Answer the following questions :**

**1** Graph the function  $f : f(x) = \sqrt{x^2 - 4x + 4}$  and determine its range and discuss its monotony.

**2** Graph the curve of the function  $f : f(x) = x^3 - 5$  and from the graph discuss the monotonicity of the function and show its type whether it is even, odd or otherwise.

**3** Find :  $\lim_{x \rightarrow 0} \frac{\sqrt{9x + 16} - 4}{x}$

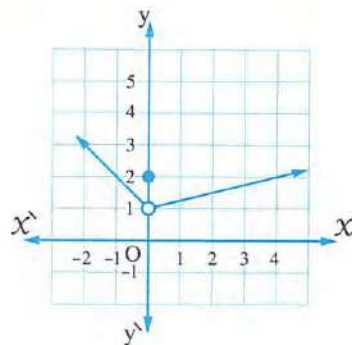
**4** Study the opposite figure, then find :

(1)  $f(0)$

(2)  $\lim_{x \rightarrow 0} f(x)$

(3)  $f(2)$

(4)  $\lim_{x \rightarrow 2} f(x)$



# Model 10

Interactive test 10



## First Multiple choice questions

Choose the correct answer from the given ones :

1 The solution set of the equation  $\log_3 (X-4) + \log_3 (X+4) = 2$  in  $\mathbb{R}$  is .....

- (a)  $\{5\}$  (b)  $\{5, -5\}$  (c)  $\{3, -3\}$  (d)  $\{3, 5\}$

2  $\lim_{x \rightarrow 0} \frac{(X+2)^2 - 4}{X^2 + X} = \dots\dots\dots$

- (a) zero (b) 2 (c) 4 (d) 8

3 If the ratio among the measures of the angles of a triangle is  $8 : 3 : 1$ , then the ratio between the longest two sides in the triangle is .....

- (a)  $\sqrt{3} : 2$  (b)  $\sqrt{6} : 2$  (c)  $8 : 3$  (d)  $8 : 5$

4  $\lim_{x \rightarrow -3} \frac{\sqrt{X+7} - 2}{X+3} = \dots\dots\dots$

- (a)  $\frac{1}{4}$  (b)  $\frac{1}{2}$  (c) 2 (d) 4

5 If  $3^a = 4^b$ , then :  $9^{\frac{a}{b}} + 16^{\frac{b}{a}} = \dots\dots\dots$

- (a) 7 (b) 12 (c) 20 (d) 25

6 If  $\lim_{x \rightarrow \infty} \frac{3k|X|}{4X+3} = 6$ , then  $k = \dots\dots\dots$

- (a) 6 (b)  $\frac{3}{4}$  (c) 8 (d) 3

7 If  $f(X) = X^3$ , then the image of the curve of  $f$  by reflection in  $X$ -axis and translation 3 units in the direction of  $\overrightarrow{OX}$  and two units in the direction of  $\overrightarrow{Oy}$  is .....

- (a)  $-(X-3)^3 - 2$  (b)  $-(X+3)^3 + 2$   
(c)  $-(X+3)^3 - 2$  (d)  $-[(X+3)^3 + 2]$

8 If  $2^{X-3} = 1$ , then  $X = \dots\dots\dots$

- (a) -3 (b) 3 (c) 1 (d) zero

9 If  $a \in \mathbb{R}^+ - \{1\}$ ,  $X, y \in \mathbb{R}^+$ ,  $\log_a y \neq 0$ , then  $\frac{\log_a X}{\log_a y} = \dots\dots\dots$

- (a)  $\log_a \frac{X}{y}$  (b)  $\log_a (X-y)$  (c)  $\log_a X - \log_a y$  (d)  $\log_y X$



- 10**  $\frac{1}{\log_2 30} + \frac{1}{\log_3 30} + \frac{1}{\log_5 30} = \dots\dots\dots$   
 (a) 1 (b)  $\log_6 5$  (c)  $\log 30$  (d) 30
- 
- 11** In  $\Delta ABC$ ,  $m(\angle A) = 112^\circ$ ,  $m(\angle B) = 33^\circ$ ,  $c = 19$  cm.  
 , then  $b$  to the nearest cm. =  $\dots\dots\dots$  cm.  
 (a) 16 (b) 17 (c) 18 (d) 20
- 
- 12** If  $2^X = 20$ ,  $n < X < n + 1$ ,  $n$  is an integer, then  $n = \dots\dots\dots$   
 (a) 4 (b) 5 (c) 6 (d) 10
- 
- 13** In  $\Delta XYZ$ ,  $y^2 + z^2 - x^2 = 2yz \times \dots\dots\dots$   
 (a)  $\cos X$  (b)  $\sin Z$  (c)  $\cos Z$  (d)  $\sin X$
- 
- 14**  $\lim_{x \rightarrow 1} \frac{x^2 + 5x - 6}{x^2 - 1} = \dots\dots\dots$   
 (a) 1 (b) 5 (c) 6 (d) 3.5
- 
- 15** The exponential function whose base is  $a$ , is increasing if  $\dots\dots\dots$   
 (a)  $a > 0$  (b)  $a > 1$  (c)  $0 < a < 1$  (d)  $a = 1$
- 
- 16**  $\lim_{x \rightarrow 2} \frac{x^5 - 32}{x^4 - 16} = \dots\dots\dots$   
 (a) 2 (b) 20 (c)  $\frac{5}{4}$  (d)  $\frac{5}{2}$
- 
- 17** If  $f$  is an odd function,  $a \in$  the domain of  $f$ , then  $f(a) + f(-a) = \dots\dots\dots$   
 (a)  $2f(a)$  (b)  $2f(-a)$  (c) zero (d)  $f(a)$
- 
- 18** The solution set in  $\mathbb{R}$  of the equation:  $|x - 3| = |9 - 2x|$  equals  $\dots\dots\dots$   
 (a)  $\{4\}$  (b)  $\{4, 6\}$  (c)  $\{6\}$  (d)  $\{2, 6\}$
- 
- 19** The range of the function  $f : f(x) = \begin{cases} 2x + 3 & , \quad x > 3 \\ 9 & , \quad x < 3 \end{cases}$  is  $\dots\dots\dots$   
 (a)  $\{3\}$  (b)  $\mathbb{R}$  (c)  $]9, \infty[$  (d)  $[9, \infty[$
- 
- 20** Diameter length of the circumcircle of equilateral triangle whose side length  $10\sqrt{3}$  cm.  
 equals  $\dots\dots\dots$  cm.  
 (a) 5 (b) 10 (c) 15 (d) 20
- 
- 21**  $\lim_{x \rightarrow 0} \frac{(x+1)^{12} - 1}{x} = \dots\dots\dots$   
 (a) 1 (b) 6 (c) zero (d) 12

- 22** If the area of  $\Delta ABC$  is " $X$ " and the radius length of its circumcircle is " $r$ " , then  $\frac{4 r X}{a b c} = \dots\dots\dots$
- (a)  $\frac{a}{\sin A}$  (b)  $\cos A$  (c) 1 (d)  $r$
- 
- 23** If  $f(X) = 7^{X+1}$  , then the value of  $X$  which satisfies :  $f(2X-1) + f(X-2) = 50$  equals  $\dots\dots\dots$
- (a) 1 (b) 7 (c) zero (d) 2
- 
- 24** If  $L, M$  are the roots of the equation :  $X^2 - 4X + 4 = 0$  , then  $\log_2 L + \log_2 M = \dots\dots\dots$
- (a) 2 (b) -2 (c) -4 (d) 4
- 
- 25** If  $\sqrt{X^2 - 2X + 1} > 4$  , then  $X \in \dots\dots\dots$
- (a)  $[-3, 5]$  (b)  $] -3, 5[$  (c)  $\mathbb{R} - ] -3, 5[$  (d)  $\mathbb{R} - [-3, 5]$
- 
- 26** In triangle  $ABC$  ,  $a = 4$  cm. ,  $b = 7$  cm. ,  $m(\angle A) = 112^\circ$  , then the number of triangles satisfy these conditions equals  $\dots\dots\dots$
- (a) 1 (b) 2 (c) 0 (d) infinite number.
- 
- 27** In triangle  $ABC$  ,  $m(\angle A) : m(\angle B) : m(\angle C) = 2 : 3 : 4$  ,  $AB = 12$  cm. , then the length of  $\overline{AC} \approx \dots\dots\dots$  cm.
- (a) 10 (b) 11 (c) 16 (d) 18
- 
- 28** In  $\Delta ABC$  :  $\frac{c^2 - a^2 - b^2}{2ab} = \dots\dots\dots$
- (a)  $\cos(A+B)$  (b)  $\cos C$  (c)  $\sin(C+90^\circ)$  (d)  $\cos(B+C)$

## Second Essay questions

**Answer the following questions :**

- 1** Find :  $\lim_{x \rightarrow 2} \frac{(X-1)^6 - 1}{X-2}$
- 
- 2** Without using the calculator prove that :  $\log_5 \frac{15}{7} + \log_5 \frac{35}{3} - \log_5 \frac{1}{5} = \log_2 8$
- 
- 3** Determine the type of the function  $f : f(X) = X^2 + \sin X$  whether it is even , odd or otherwise.
- 
- 4**  $\lim_{x \rightarrow \infty} (X^3 + 5X^2 + 1)$



# كيفية طباعة صفحات معينة من ملف معين

## مثلا ازاي نطبع الصفحات من صفحة 4 الى صفحة 9



خطوة 1



خطوة 2  
اختيار اسم  
الطابعة  
بتاعتك

خطوة 3  
كتابة الصفحات  
المراد طباعتها  
نكتب رقم 4 ثم  
نكتب الشرطة  
دي - ثم نكتب 9

خطوة 4  
اختيار نوع الورق



خطوة 5  
اختيار A4



خطوة 6